

# Experiences in Reliability Data Analysis

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Jointly work with William Q. Meeker from  
Iowa State University

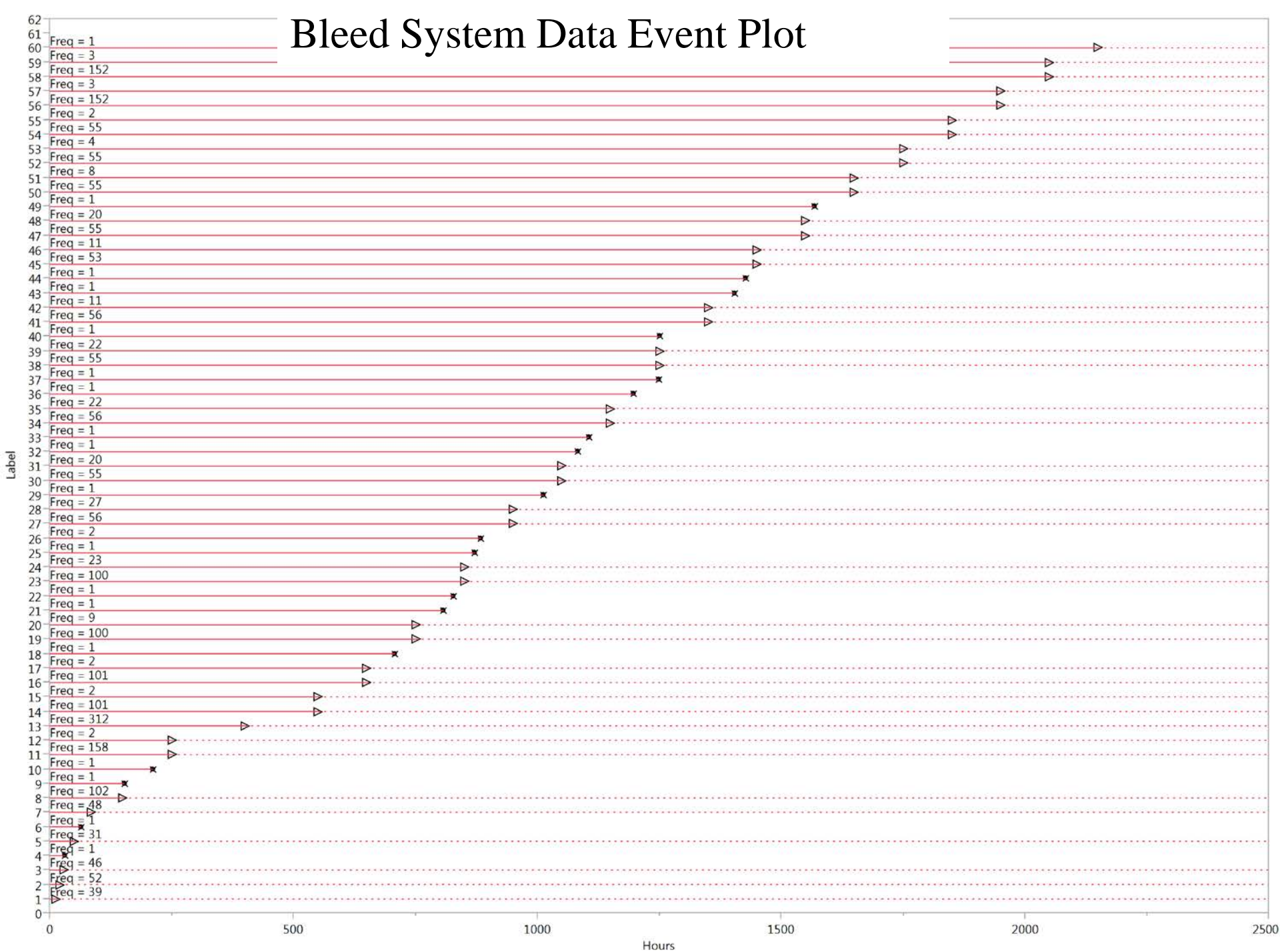
# Overview

- Analysis of Field/Warranty Data
  - Solving a reliability problem with statistics: jet engine bleed system failure
  - Using assumptions sensitivity analysis to strengthen data: bearing cage field failure data
  - Correct analysis of data with multiple failure modes: Device-G field-tracking and Shock Absorber data
  - Other examples
- Accelerated Testing
  - Accelerated life tests (Insulating structure)
  - Accelerated repeated-measures degradation tests (LEDs)
  - Accelerated destructive degradation tests (adhesive bond)
  - Other examples

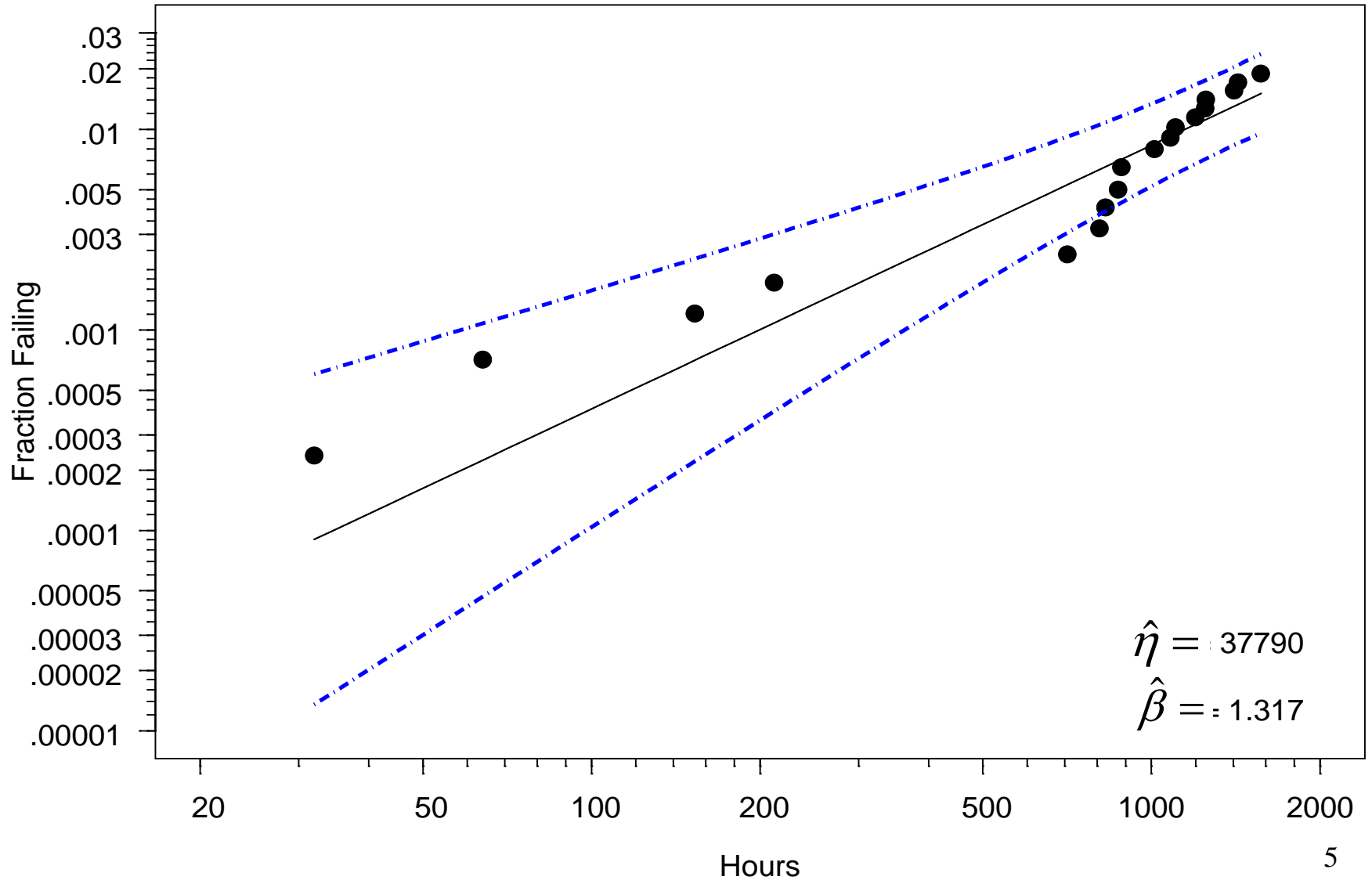
# Jet Engine Bleed System Failure

- Data from the *Weibull Handbook (1984)*
- Field data from 2256 systems in the field; staggered entry--multiple censoring
- Unexpected failures
- What is going on??

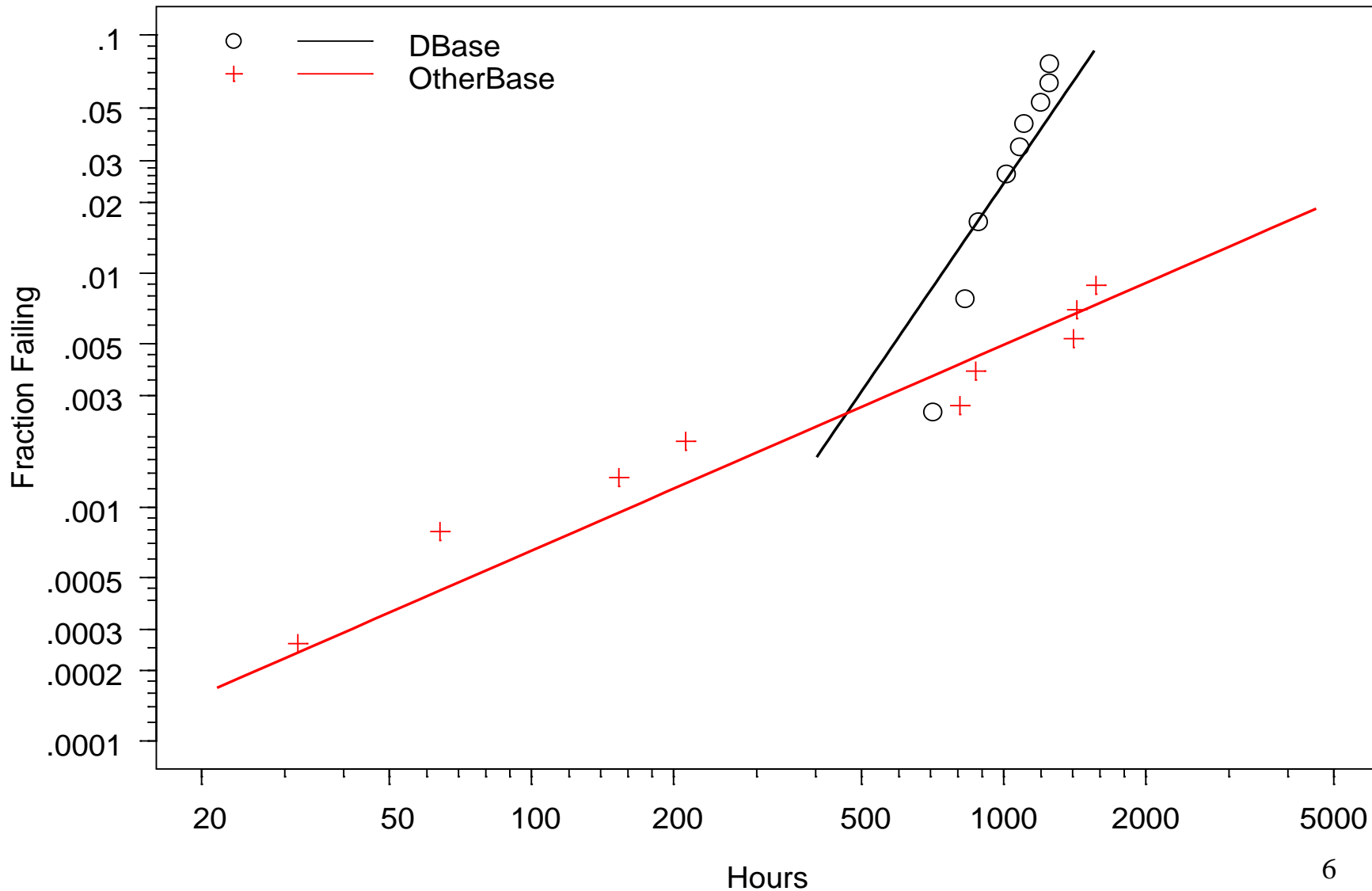
# Bleed System Data Event Plot



Bleed System Failure Data  
with Weibull ML Estimate and Pointwise 95% Confidence Intervals  
Weibull Probability Plot



# Bleed System Failure Data With Individual Weibull Distribution ML Estimates Weibull Probability Plot



# Lessons Learned

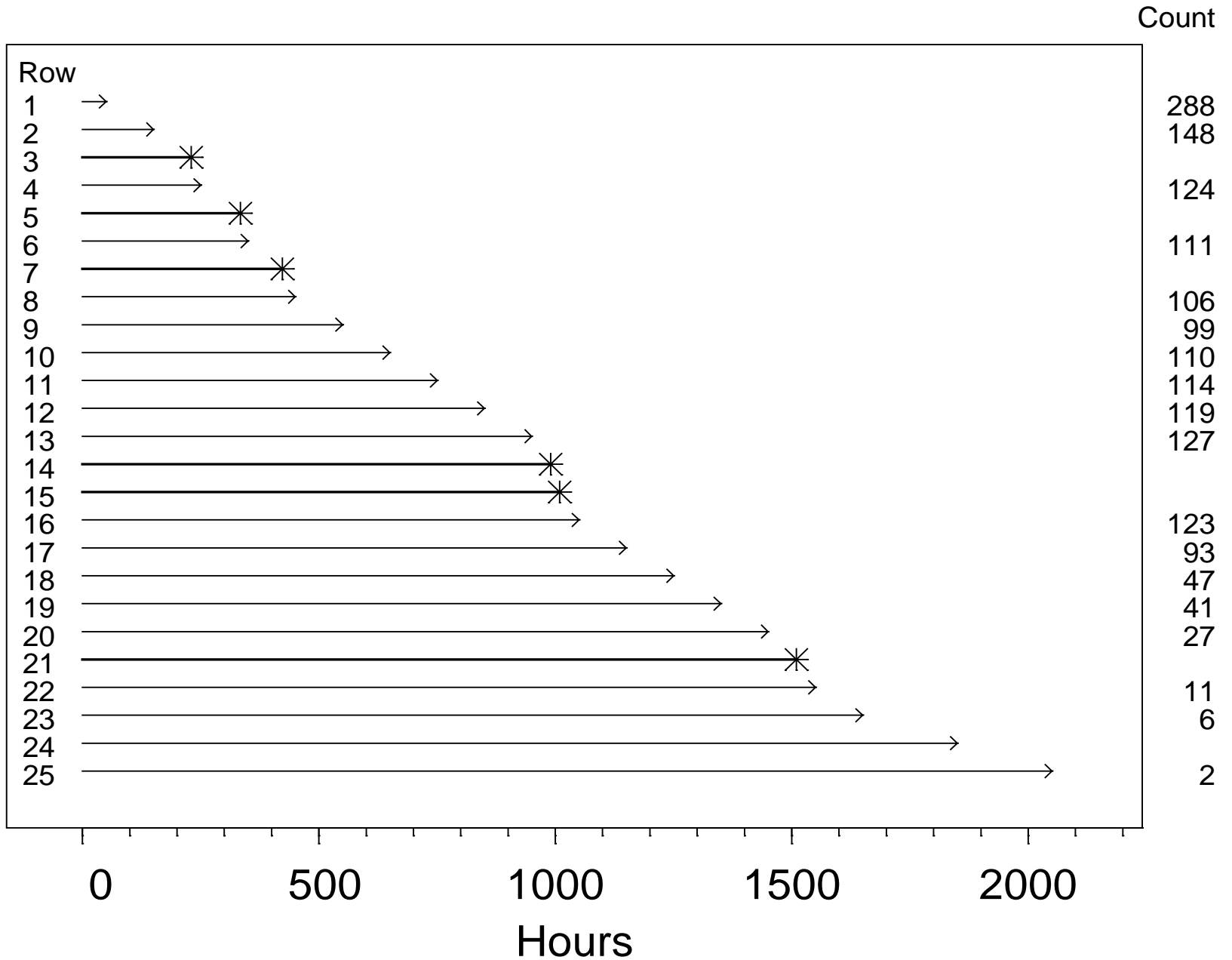
- A shift in the slope of a probability plot often indicates a different failure mode
- Look for explanatory variables to help better understand data sources

# Bearing Cage Field Failure Data

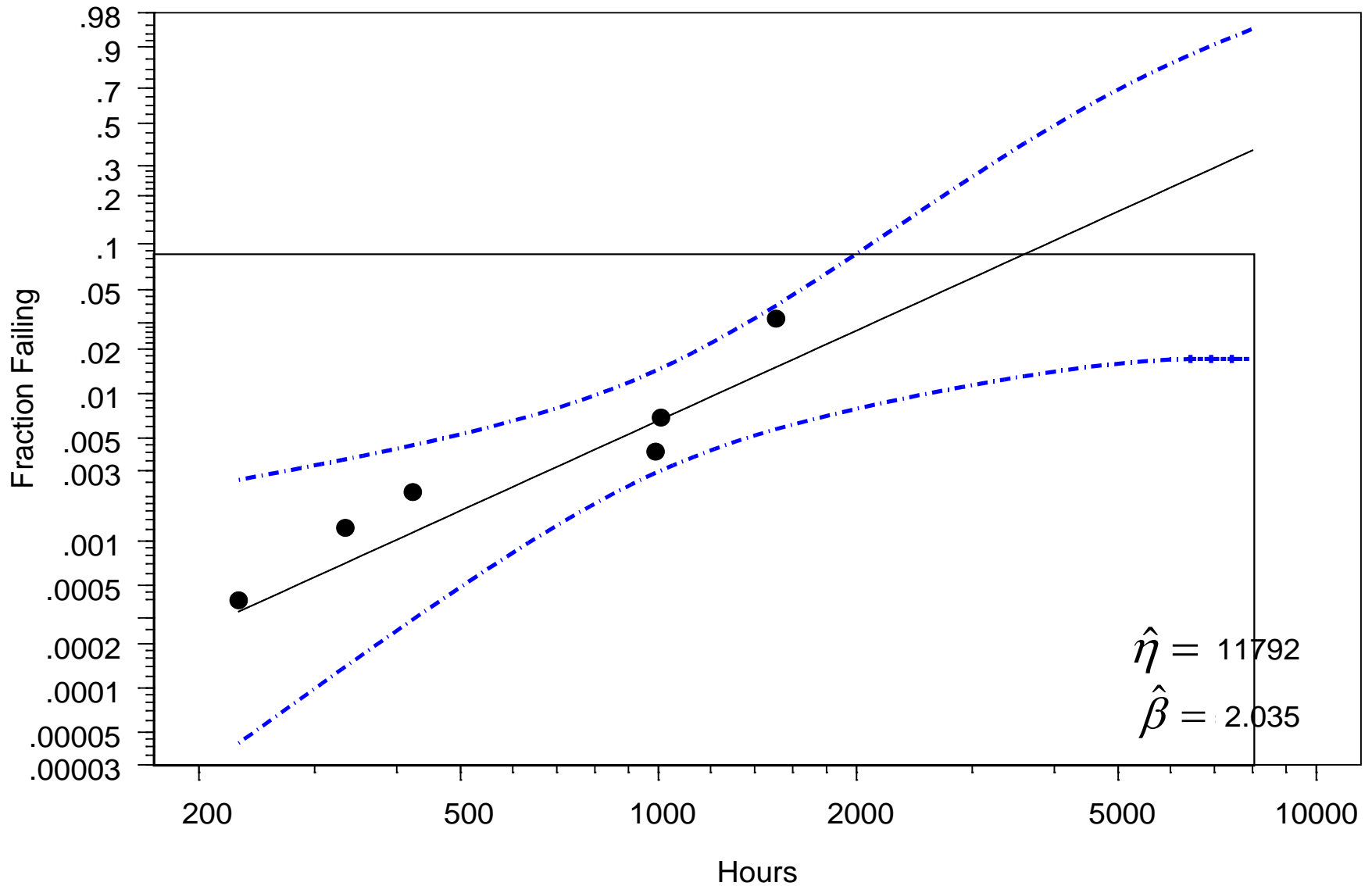
- Data from the *Weibull Handbook (1984)*
- 1703 units had been introduced into the field over time; oldest unit at 2220 hours of operation.
- 6 units had failed
- Design life specification was  $B10 = 8000$  hours of operation
- Do we have a serious problem? Re-design needed?
- How many spares needed?



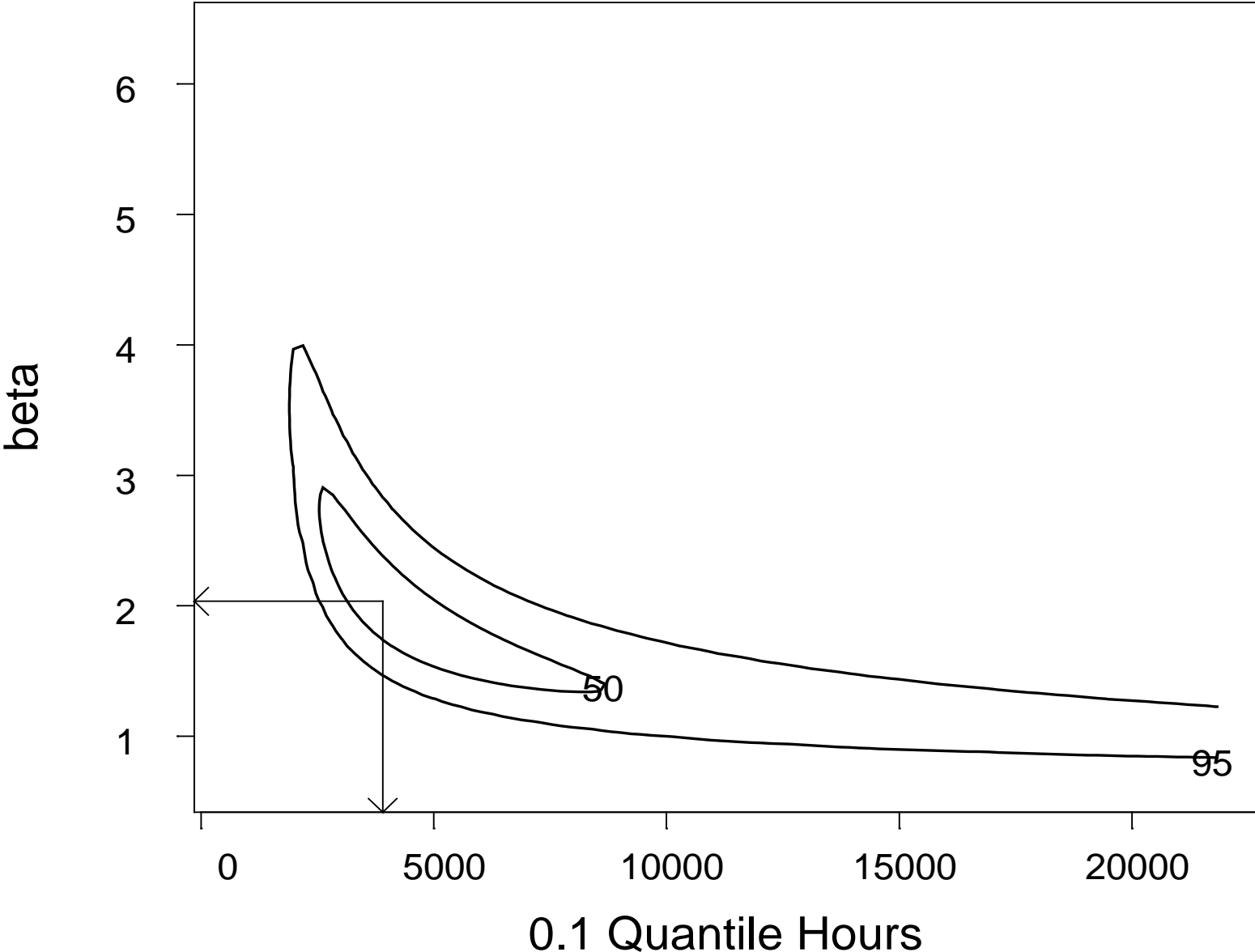
# Bearing Cage Data



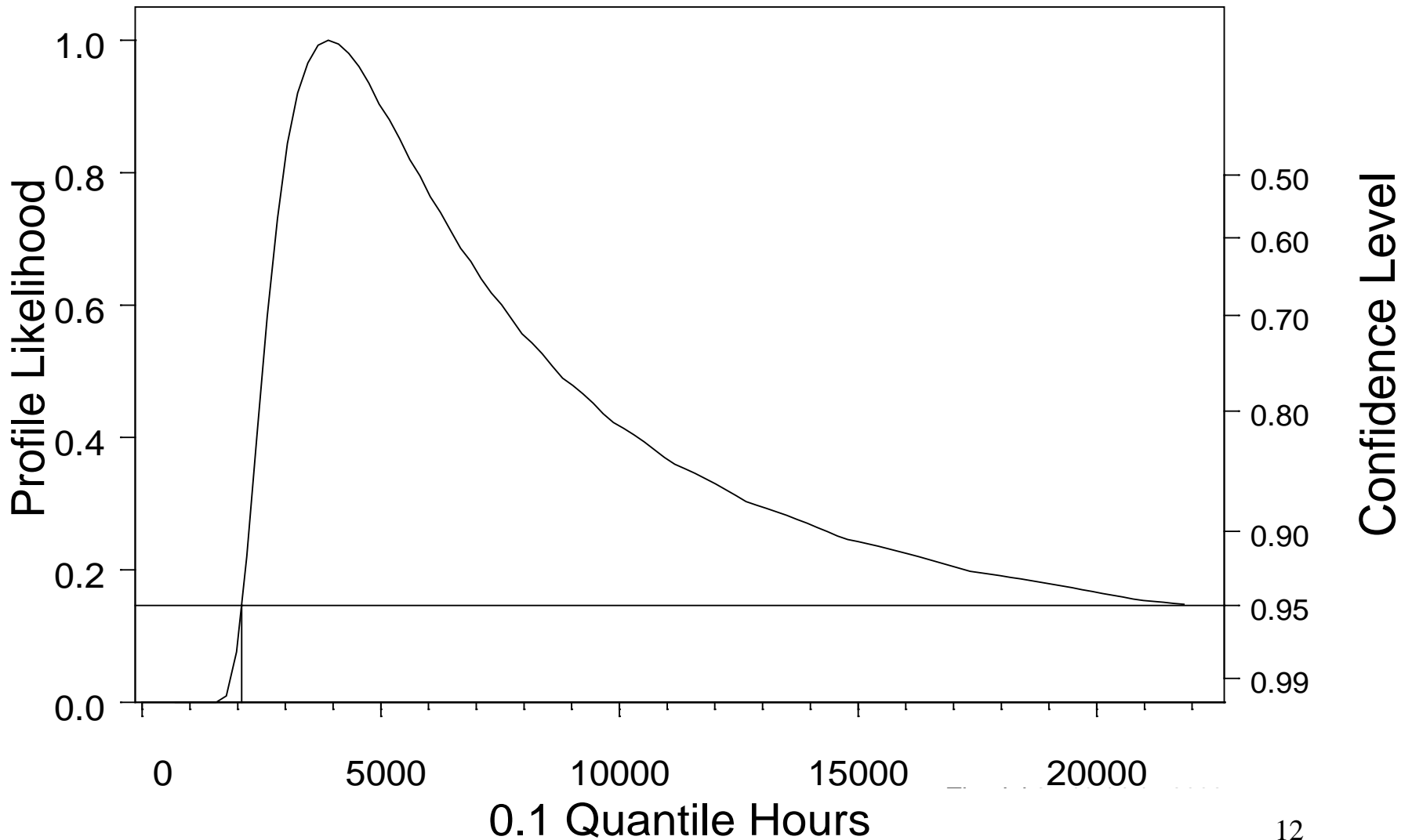
Bearing Cage Data  
with Weibull ML Estimate and Pointwise 95% Confidence Intervals  
Weibull Probability Plot



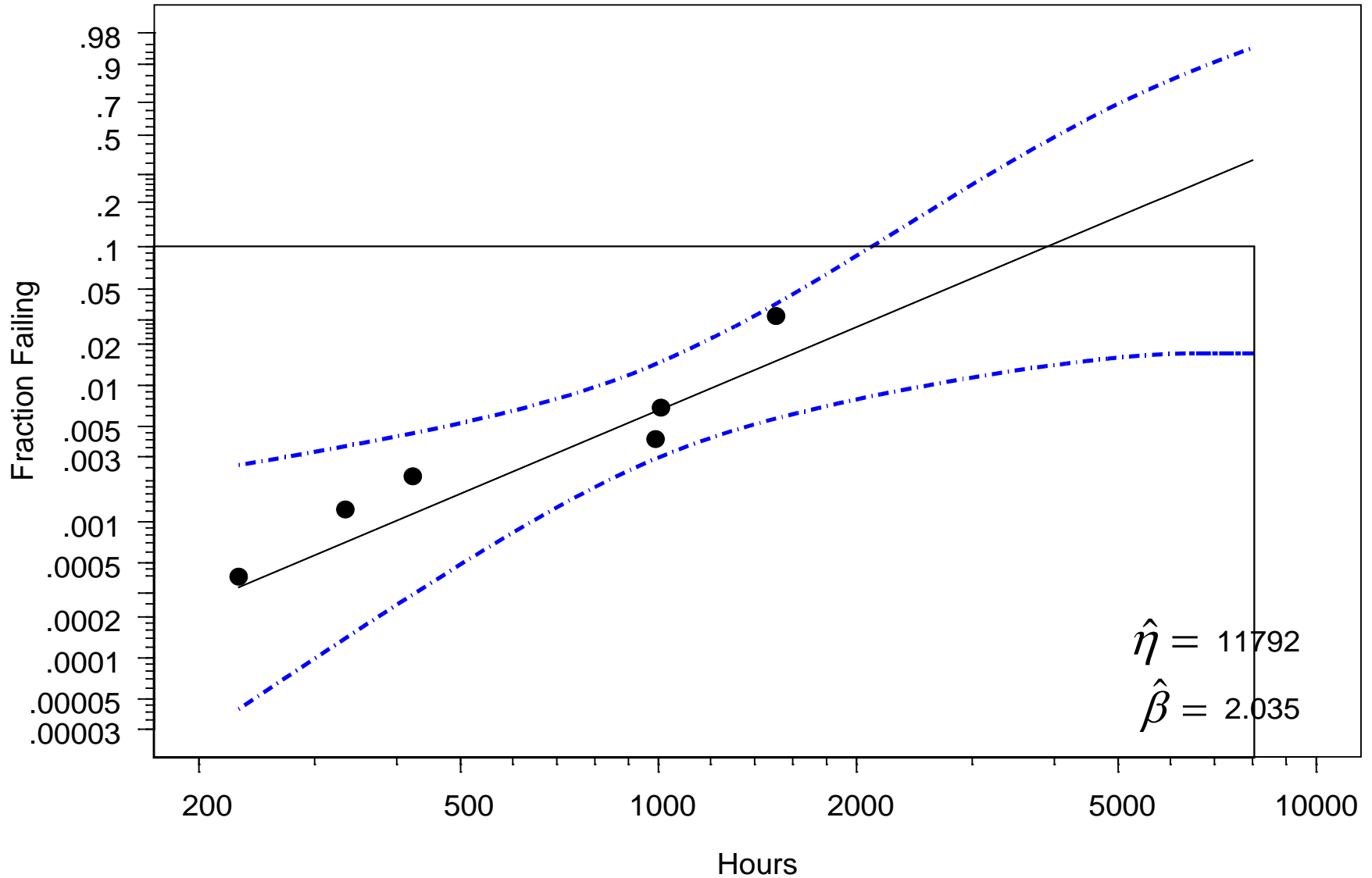
Bearing Cage Data  
Weibull Distribution Joint Confidence Region



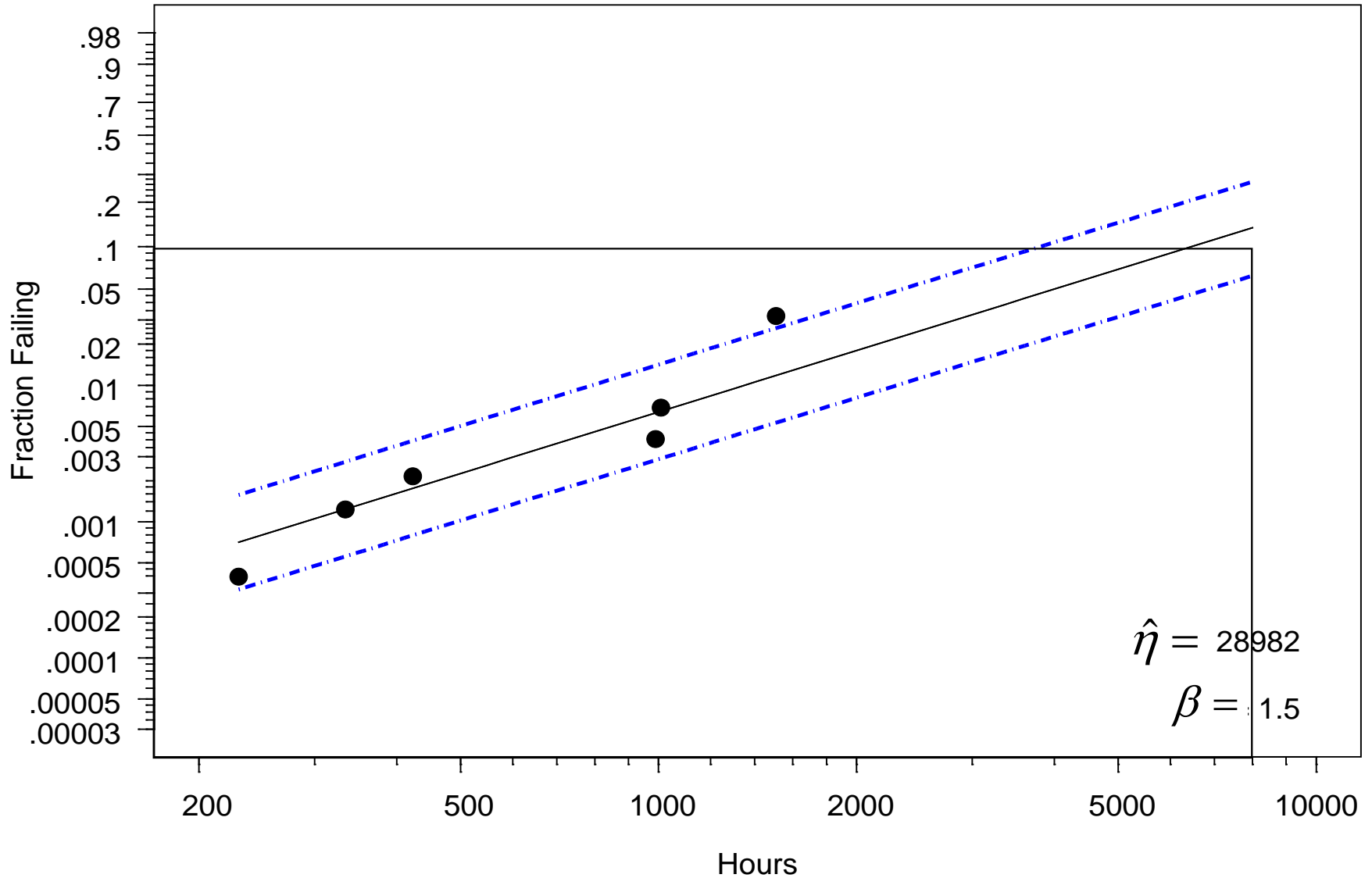
Bearing Cage Data  
Profile Likelihood and 95% Confidence Interval  
for 0.1 Quantile Hours from the Weibull Distribution



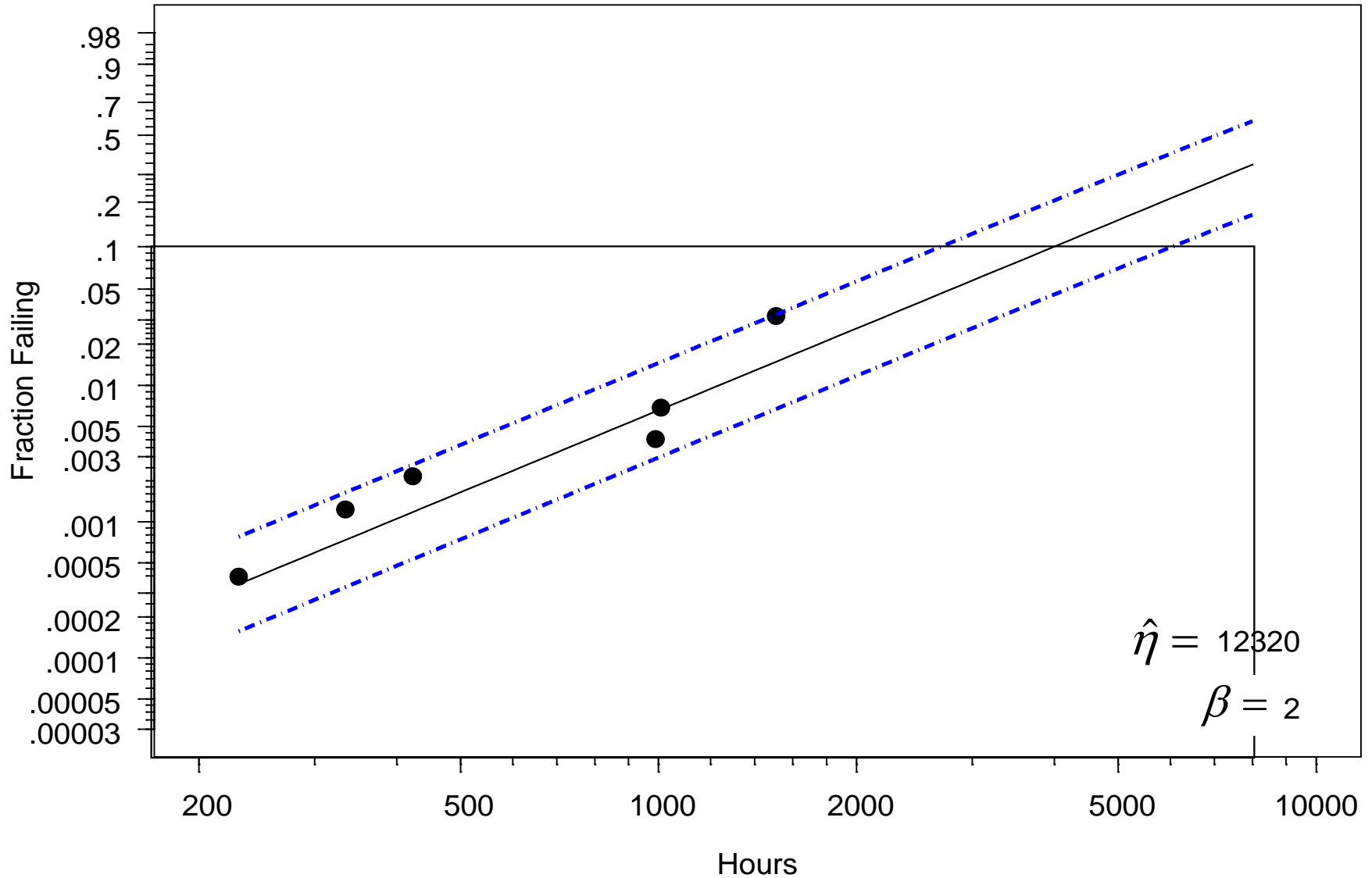
Bearing Cage Failure Data  
with Weibull ML Estimate and Pointwise 95% Confidence Intervals  
Weibull Probability Plot



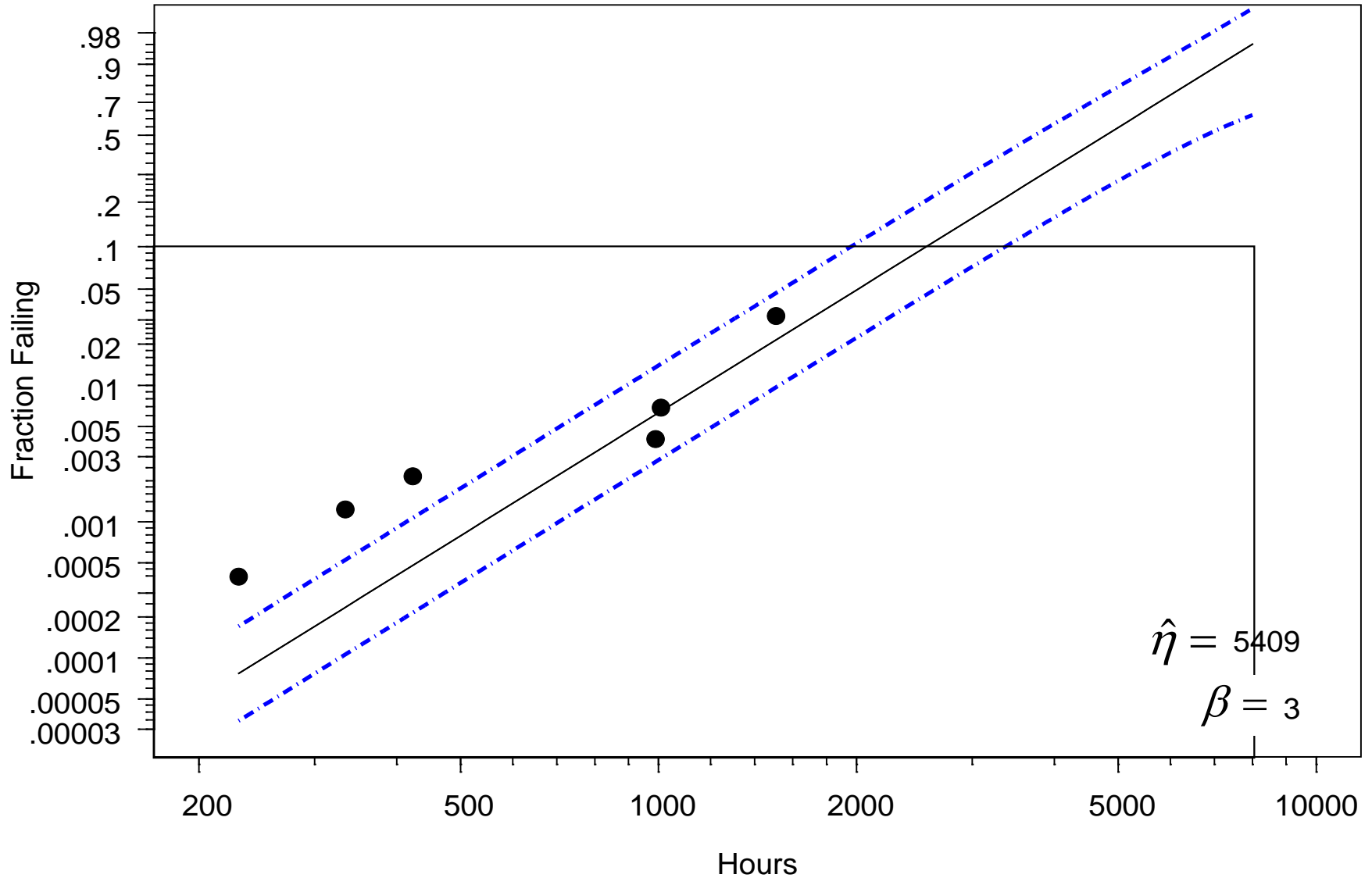
Bearing Cage Failure Data  
with Weibull ML Estimate and Pointwise 95% Confidence Intervals  
Weibull Probability Plot



Bearing Cage Failure Data  
with Weibull ML Estimate and Pointwise 95% Confidence Intervals  
Weibull Probability Plot

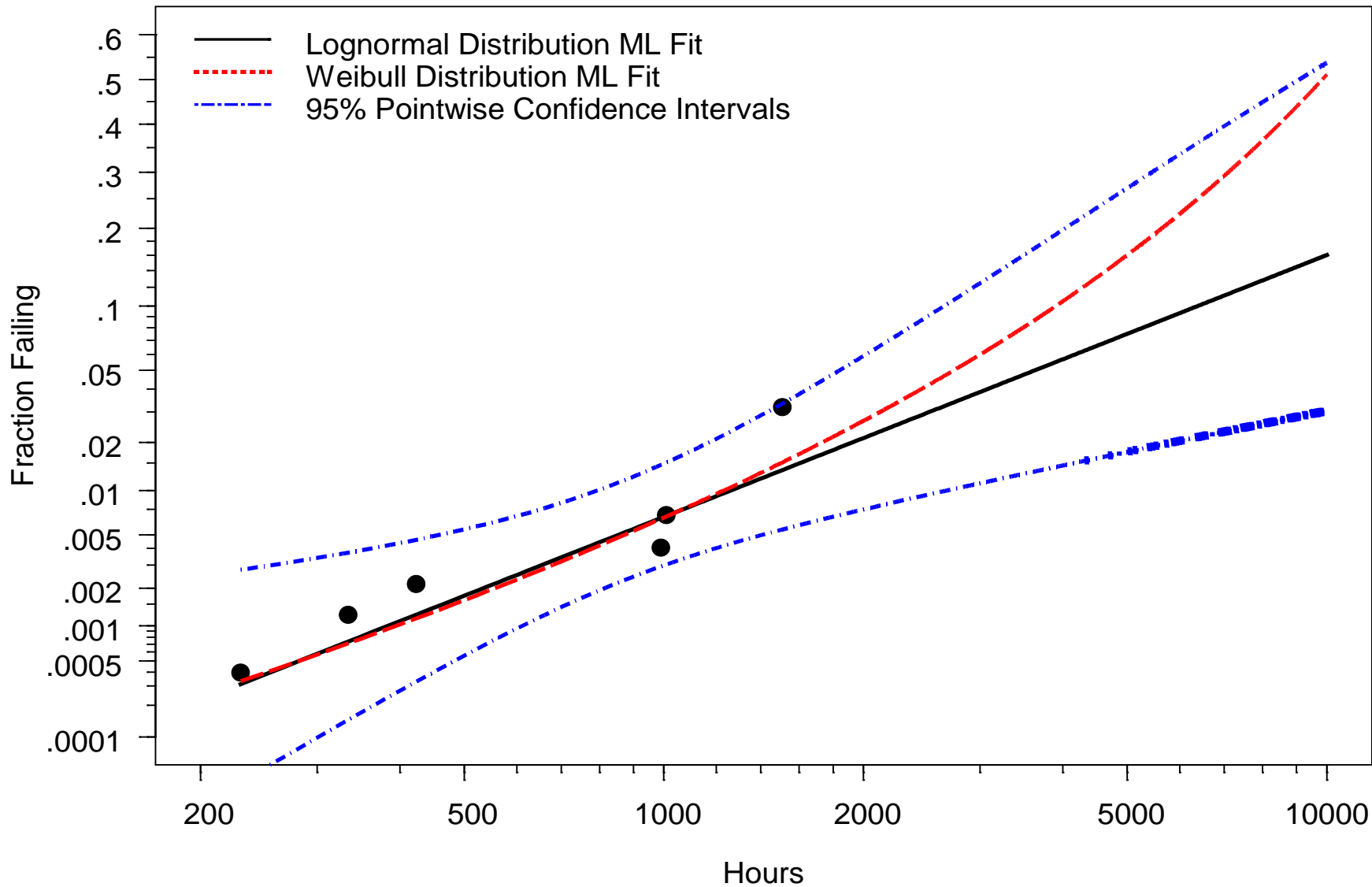


Bearing Cage Failure Data  
with Weibull ML Estimate and Pointwise 95% Confidence Intervals  
Weibull Probability Plot





# Bearing Cage Failure Data Lognormal Probability Plot



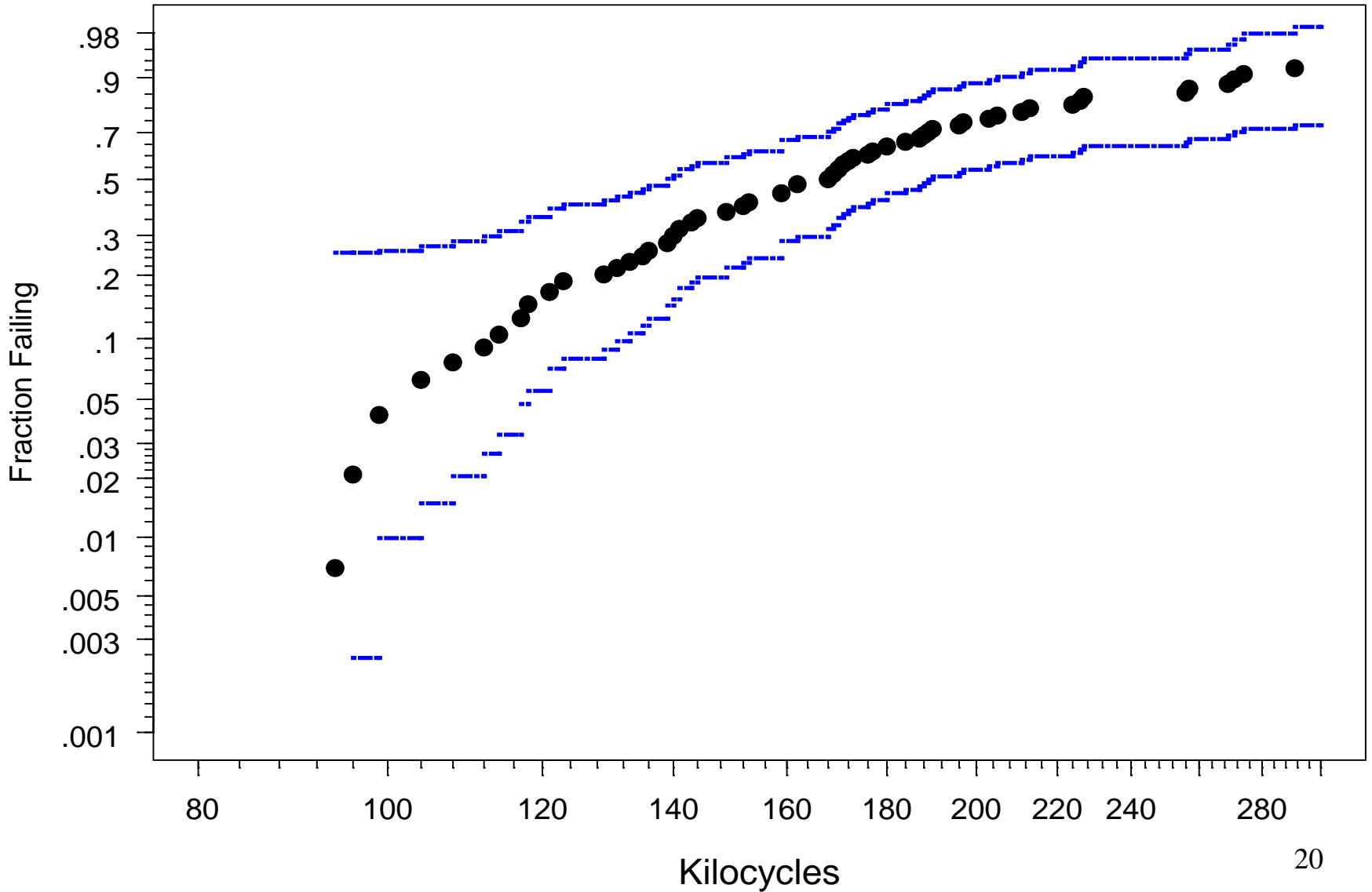
# Lessons Learned

- When data are not sufficient to answer the question, it is important to seek external information (e.g., on the Weibull shape parameter) from past experience or engineering/physical/chemical knowledge about failure mechanisms
- Sensitivity analysis provides insight and assessment of uncertainty

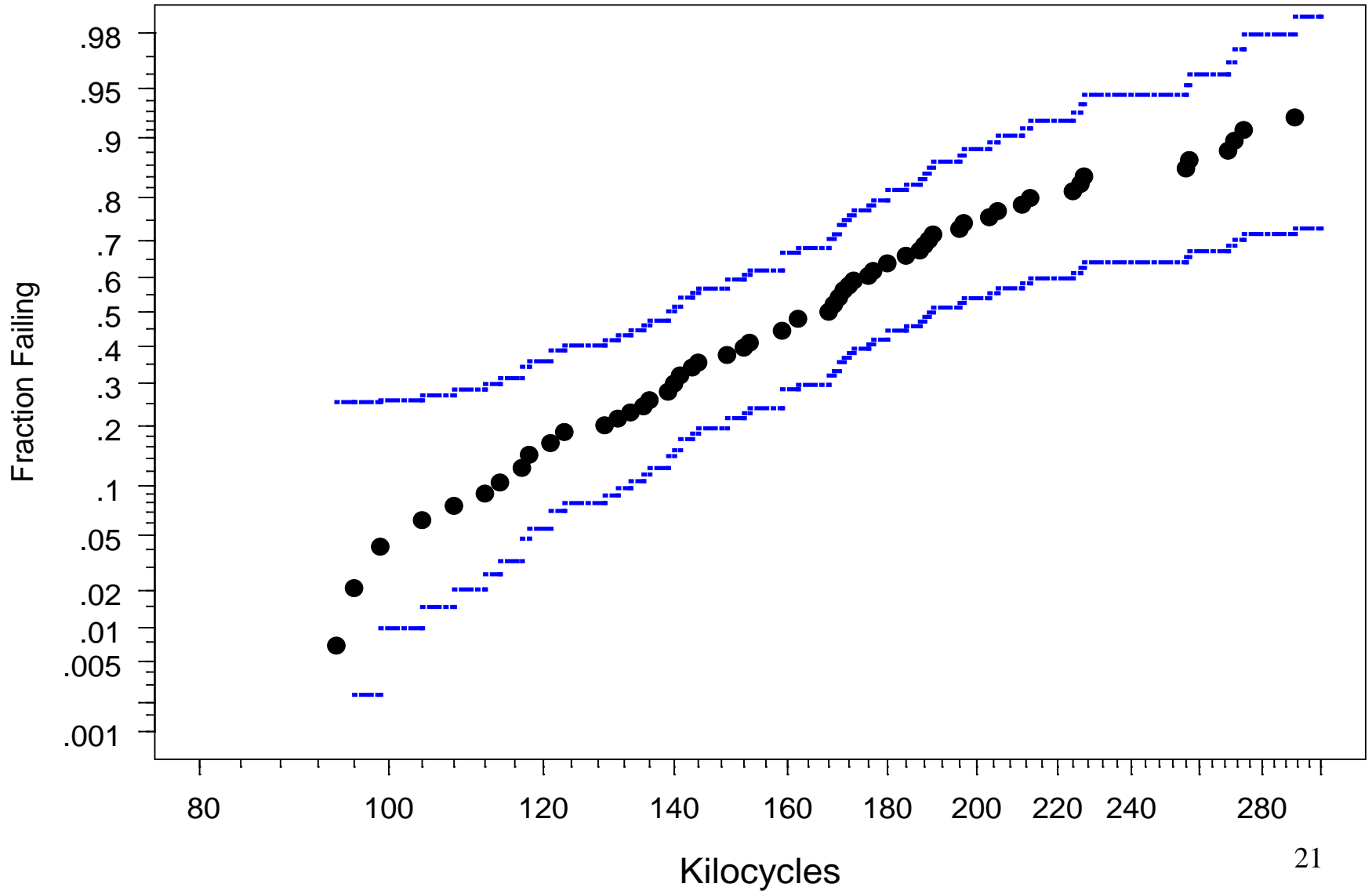
# Alloy T7987 Fatigue Data

- Data from Meeker and Escobar (1998)
- Dogbone shaped specimens
- Test run until 300 thousand cycles.
  - 67 failures;
  - 5 right-censored observations
- Need to estimate cycles-to-failure distribution.
- Primary interest in the lower tail of the distribution.

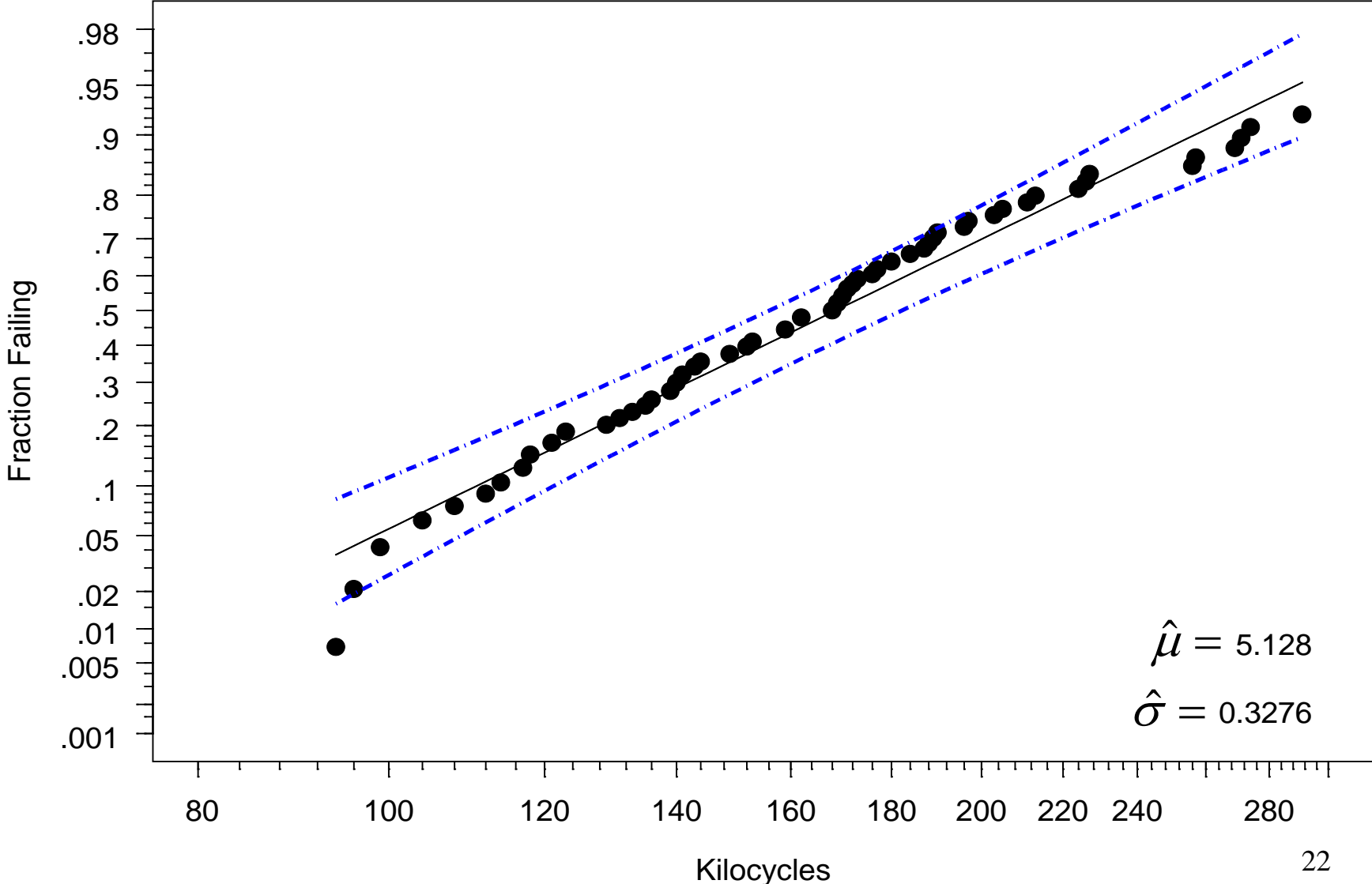
Alloy T7987 Fatigue Data  
with Nonparametric Simultaneous 95% Confidence Bands  
Weibull Probability Plot



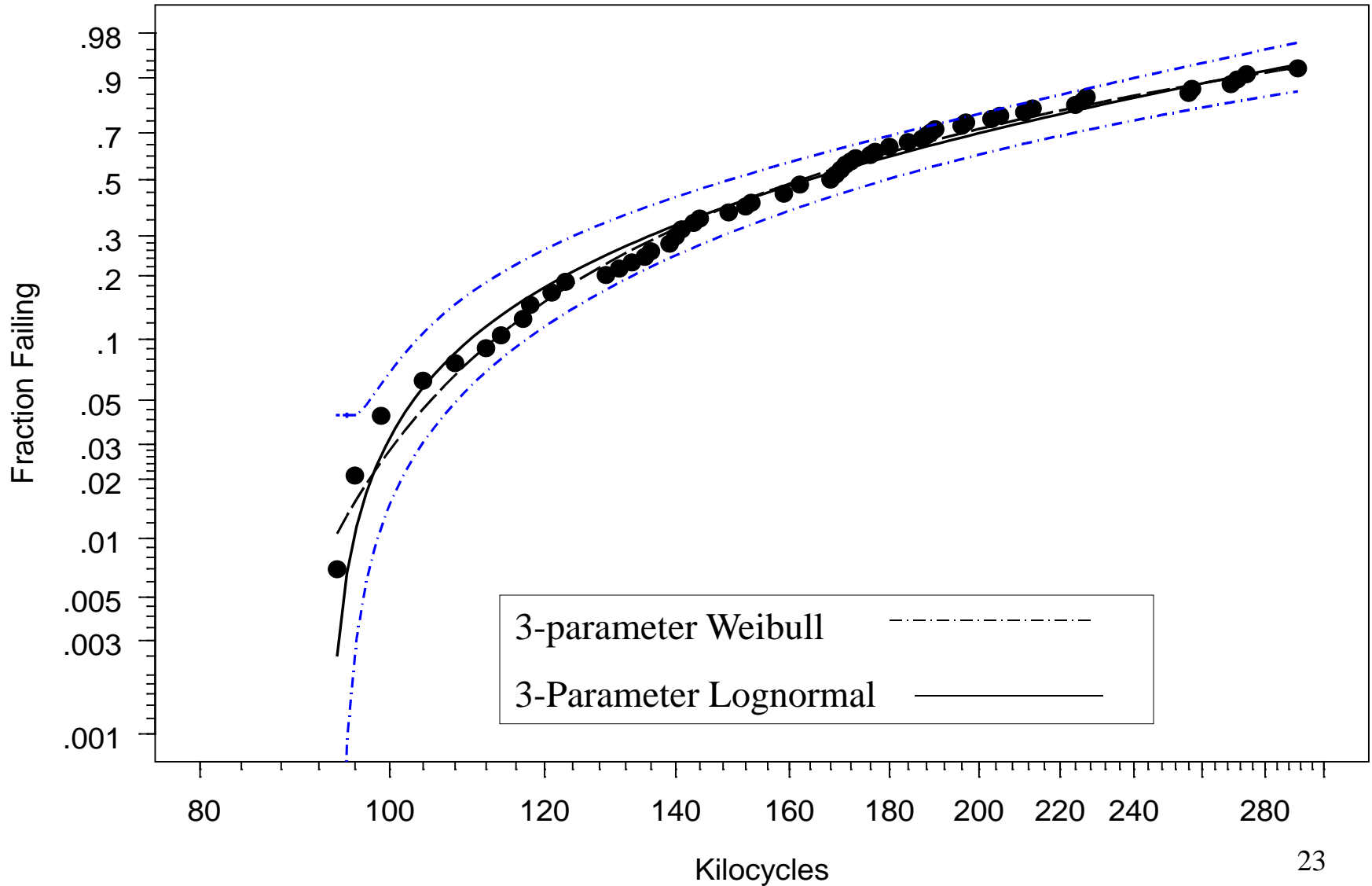
Alloy T7987 Fatigue Data  
with Nonparametric Simultaneous 95% Confidence Bands  
Lognormal Probability Plot



Alloy T7987 Fatigue Data  
with Lognormal ML Estimate and Pointwise 95% Confidence Intervals  
Lognormal Probability Plot



# Alloy T7987 Fatigue Data Weibull Probability Plot



# Lessons Learned

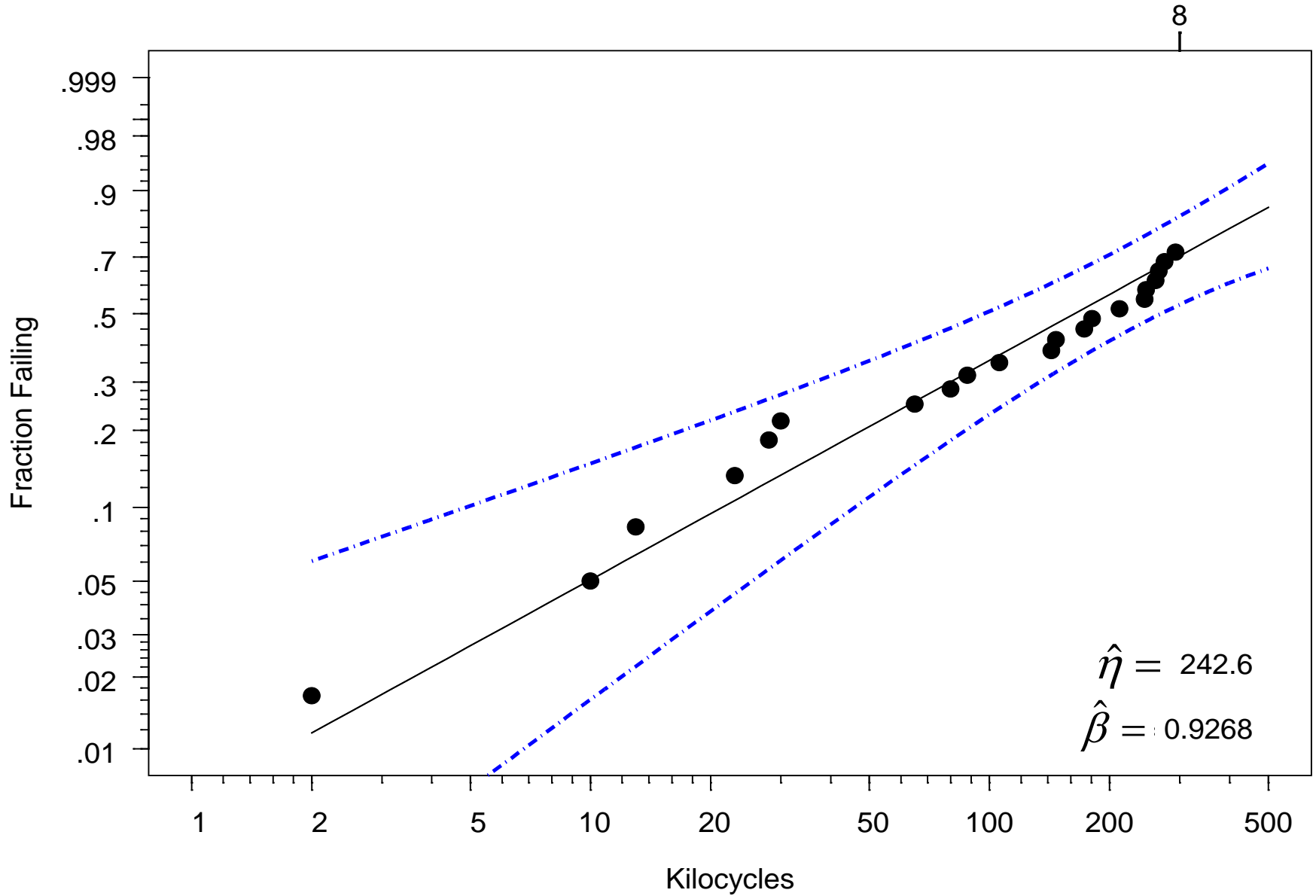
- Fitting a three-parameter Weibull or Lognormal distribution might provide a better fit
- In some cases the use of a three-parameter distribution can be justified because it is known that there is an initial period where the probability of a failure is 0
- Fitting a three-parameter distribution can lead to anti-conservative inferences



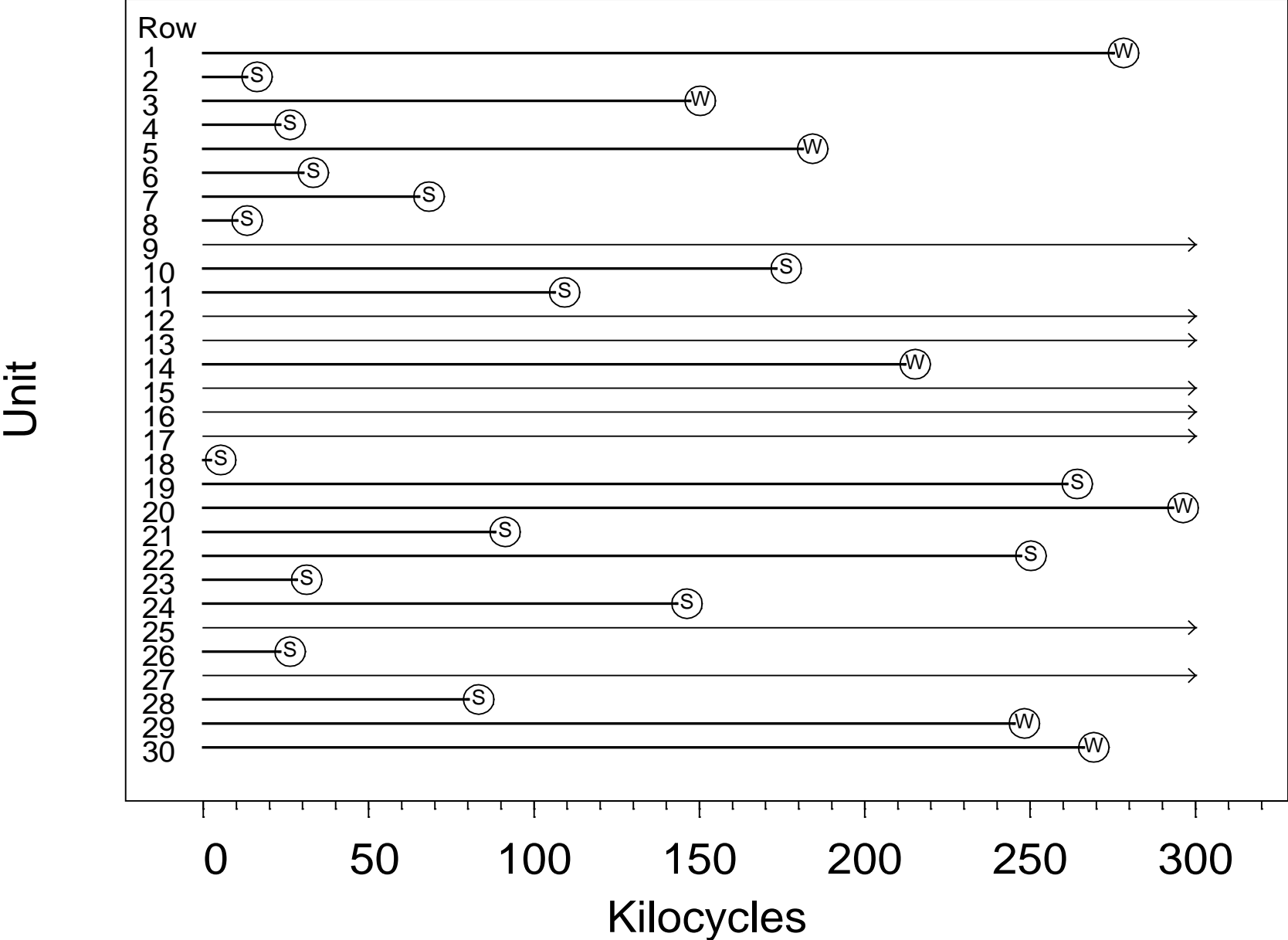
# Device-G Field-Tracking Data

- Data from Meeker and Escobar (1998)
- Design life of 300 thousand cycles
- Units were failing in the field more rapidly than had been expected.
- Needs: information on how to improve reliability and an estimate of device MTTF.
- Two failure modes: surge and wear

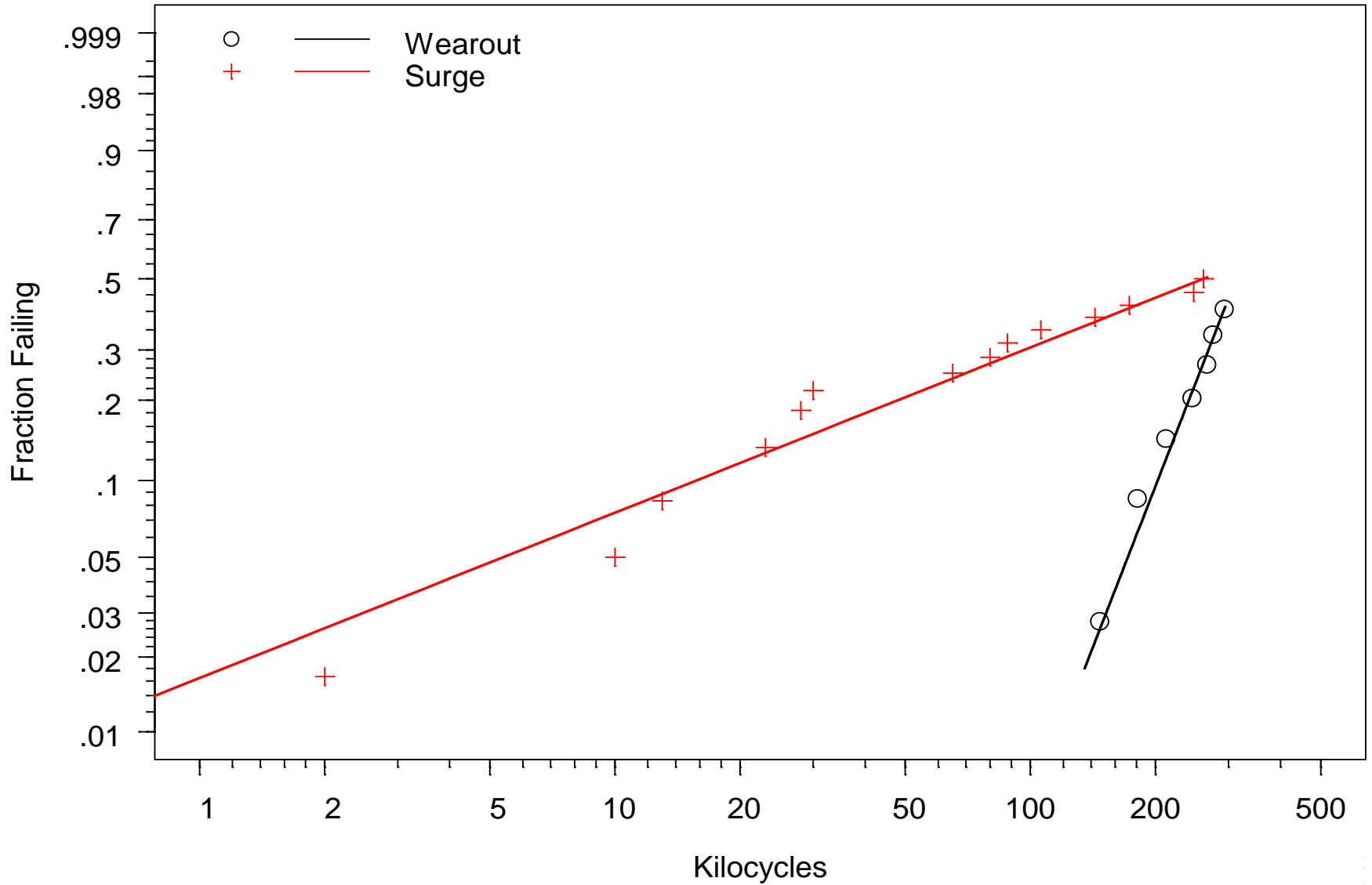
Device-G Field Data  
with Weibull ML Estimate and Pointwise 95% Confidence Intervals  
Weibull Probability Plot



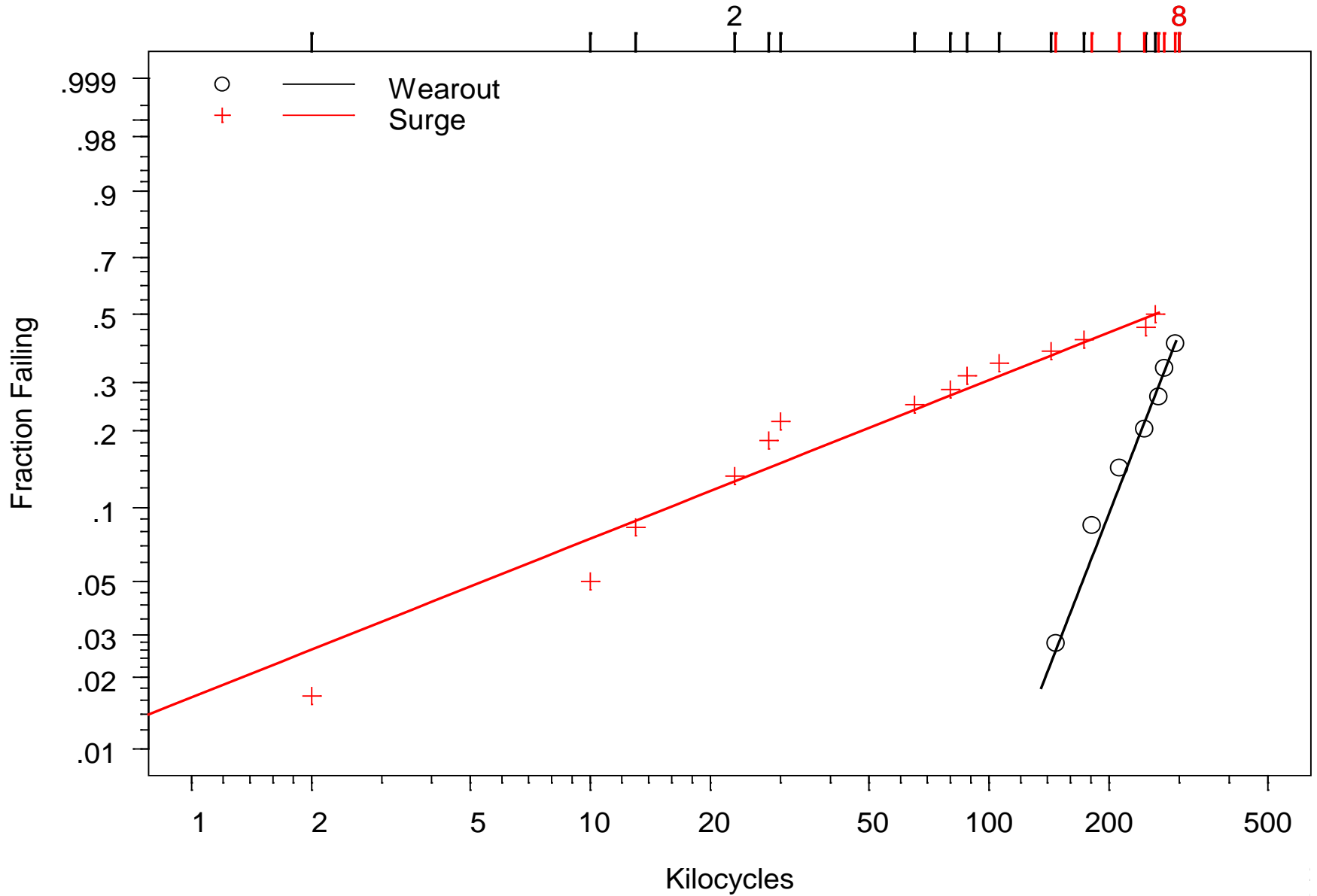
# Device-G Field Data



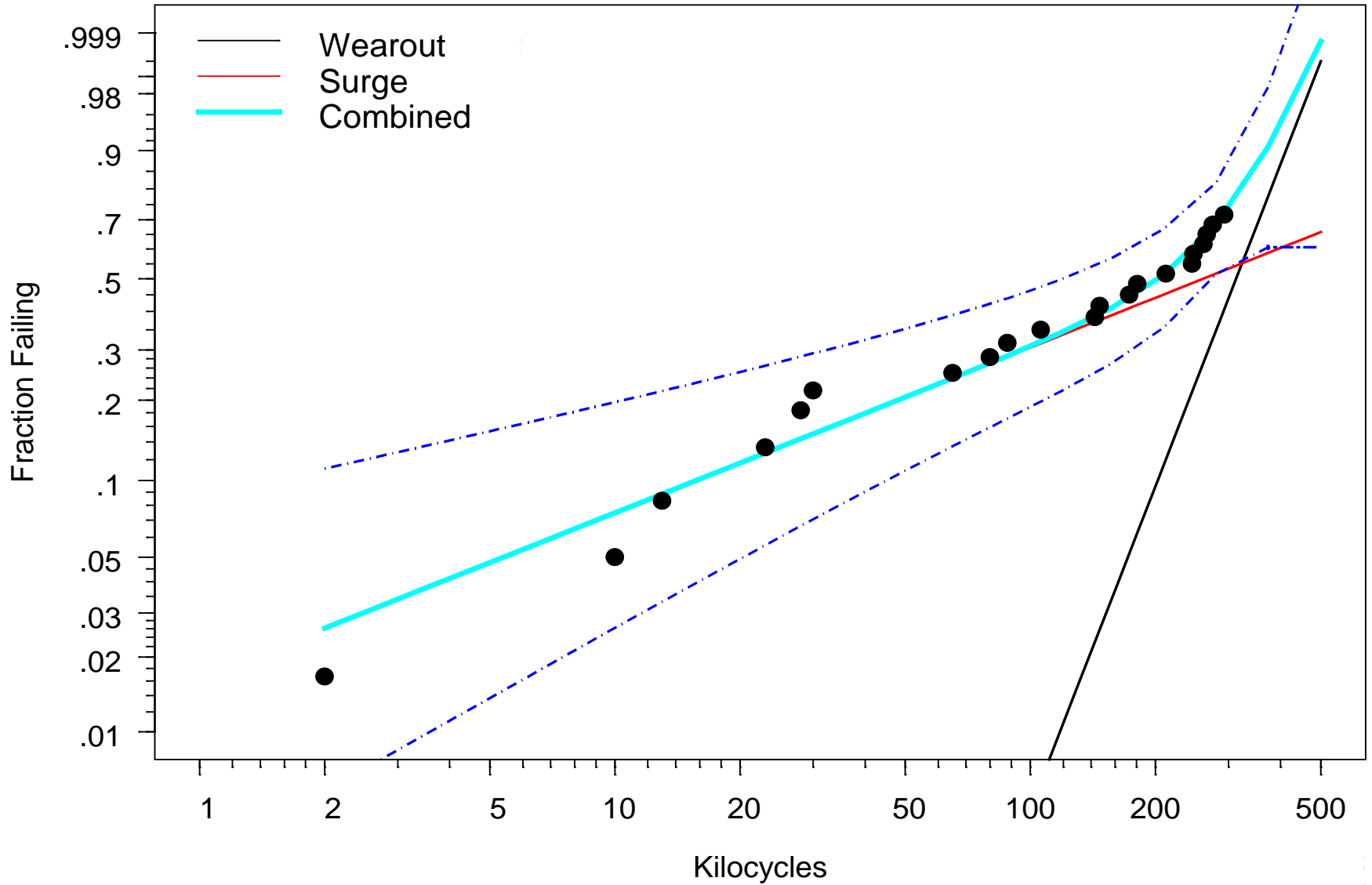
# Individual Device-G Field Data Failure Mode Weibull MLE's Weibull Probability Plot



# Individual Device-G Field Data Failure Mode Weibull MLE's Weibull Probability Plot



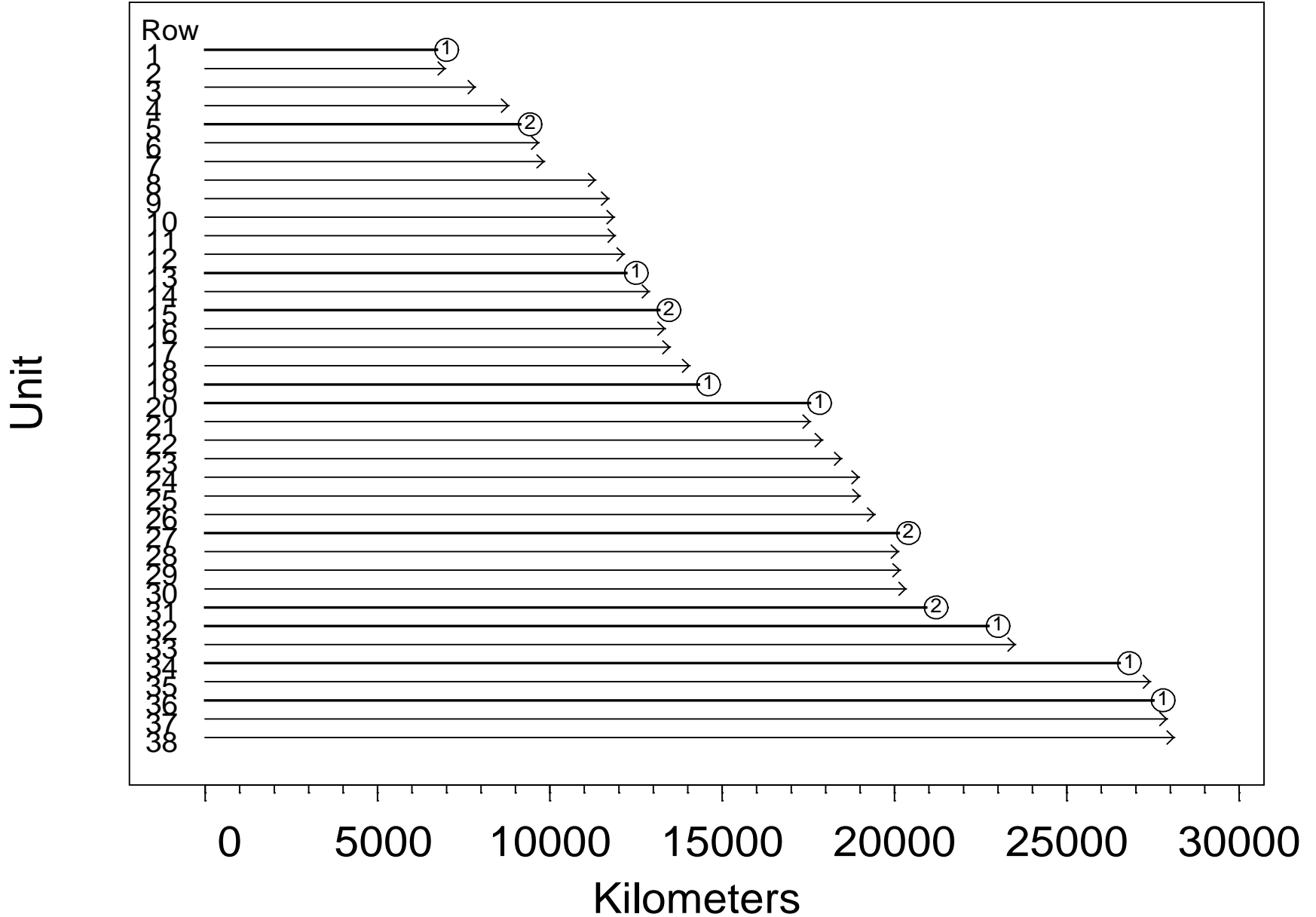
# Series System Combined Failure Mode ML Estimates and Pointwise Approximate 95% Confidence Intervals Device-G Field Data Weibull Probability Plot



# Shock Absorber Field Data

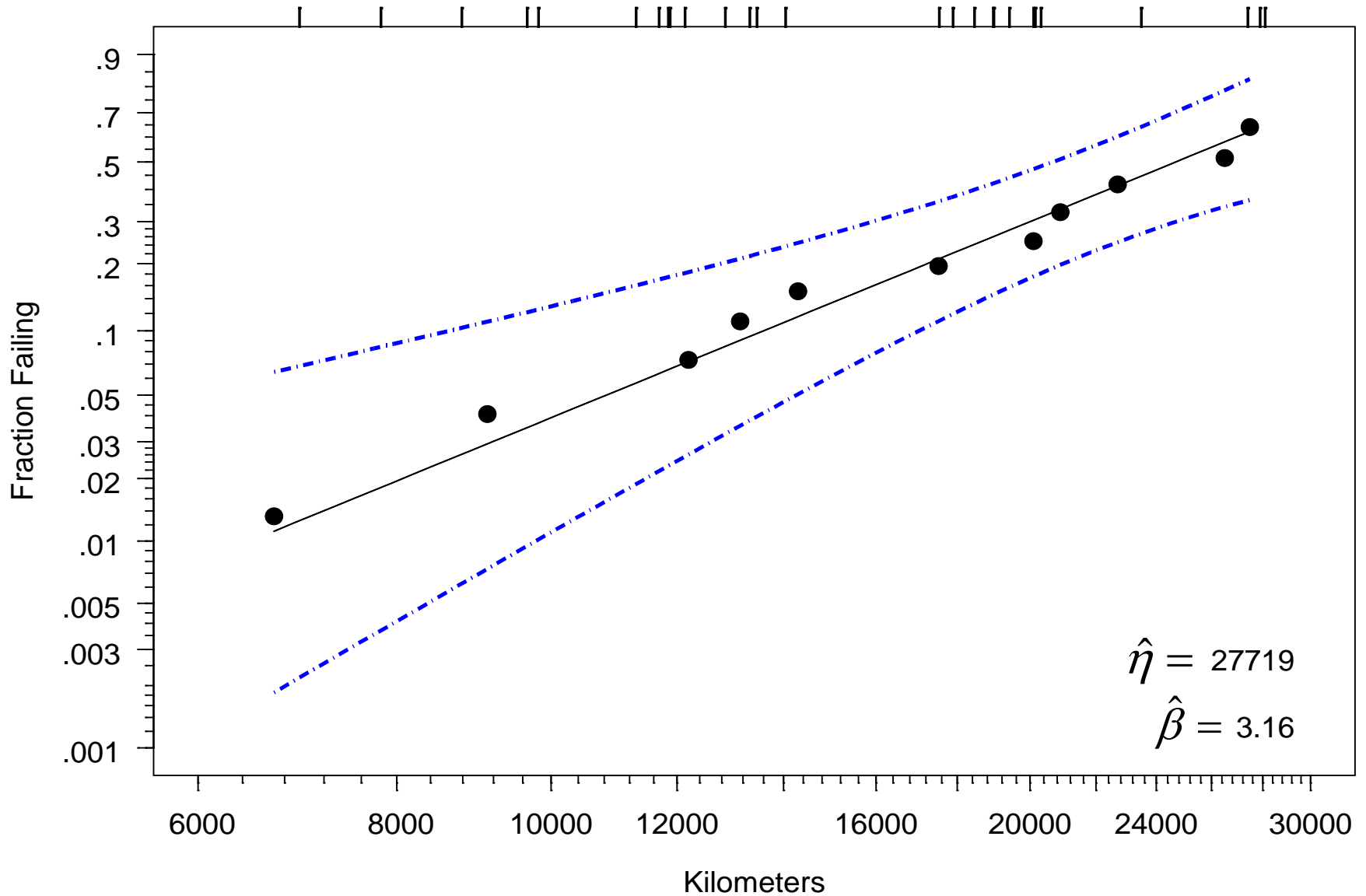
- Data from O'Connor (1985)
- Two failure modes (identified as Mode 1 and Mode 2)
- Need to estimate the failure-time distribution for the shock absorbers

# Shock Absorber Data (Both Failure Modes)

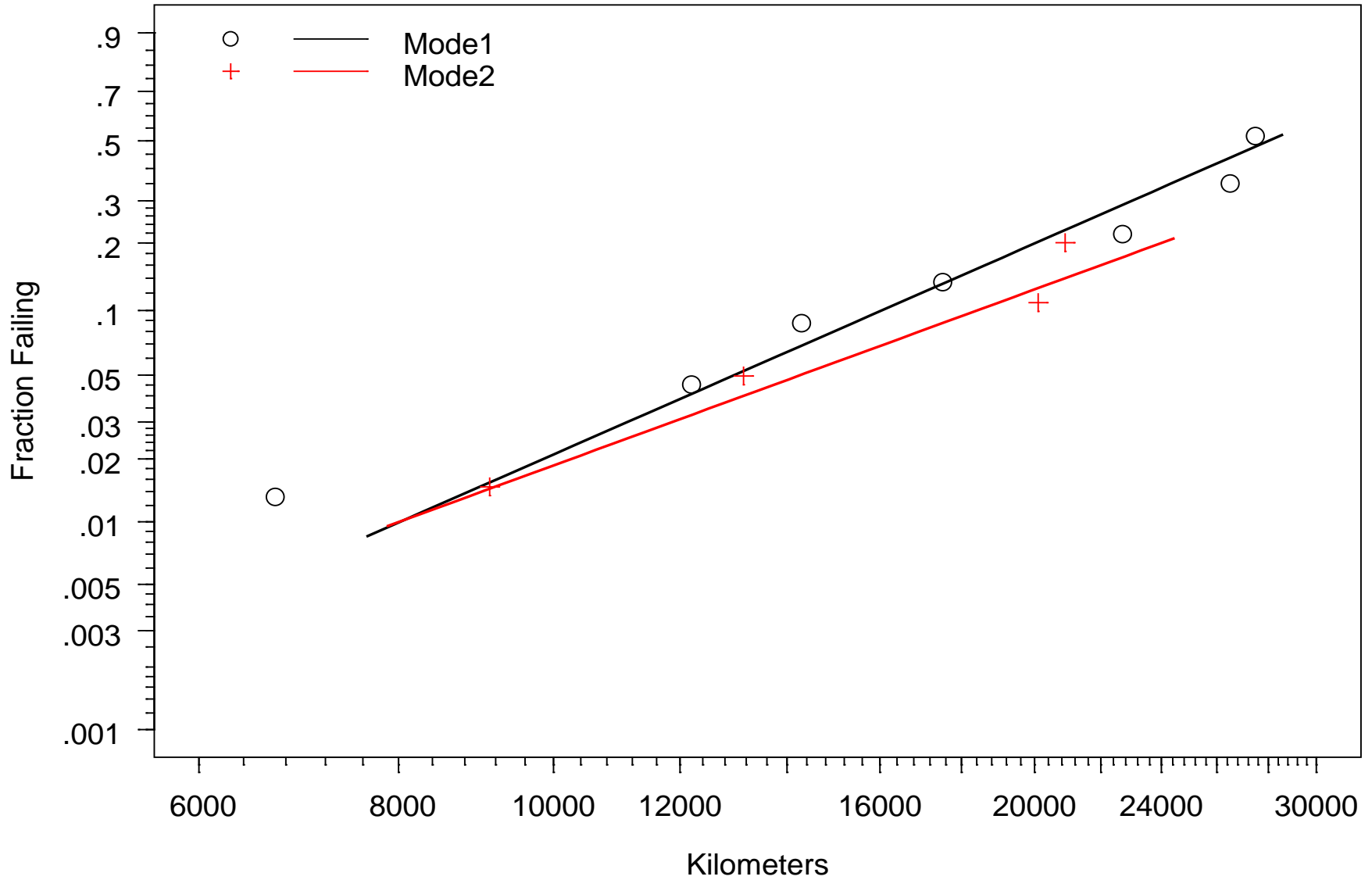




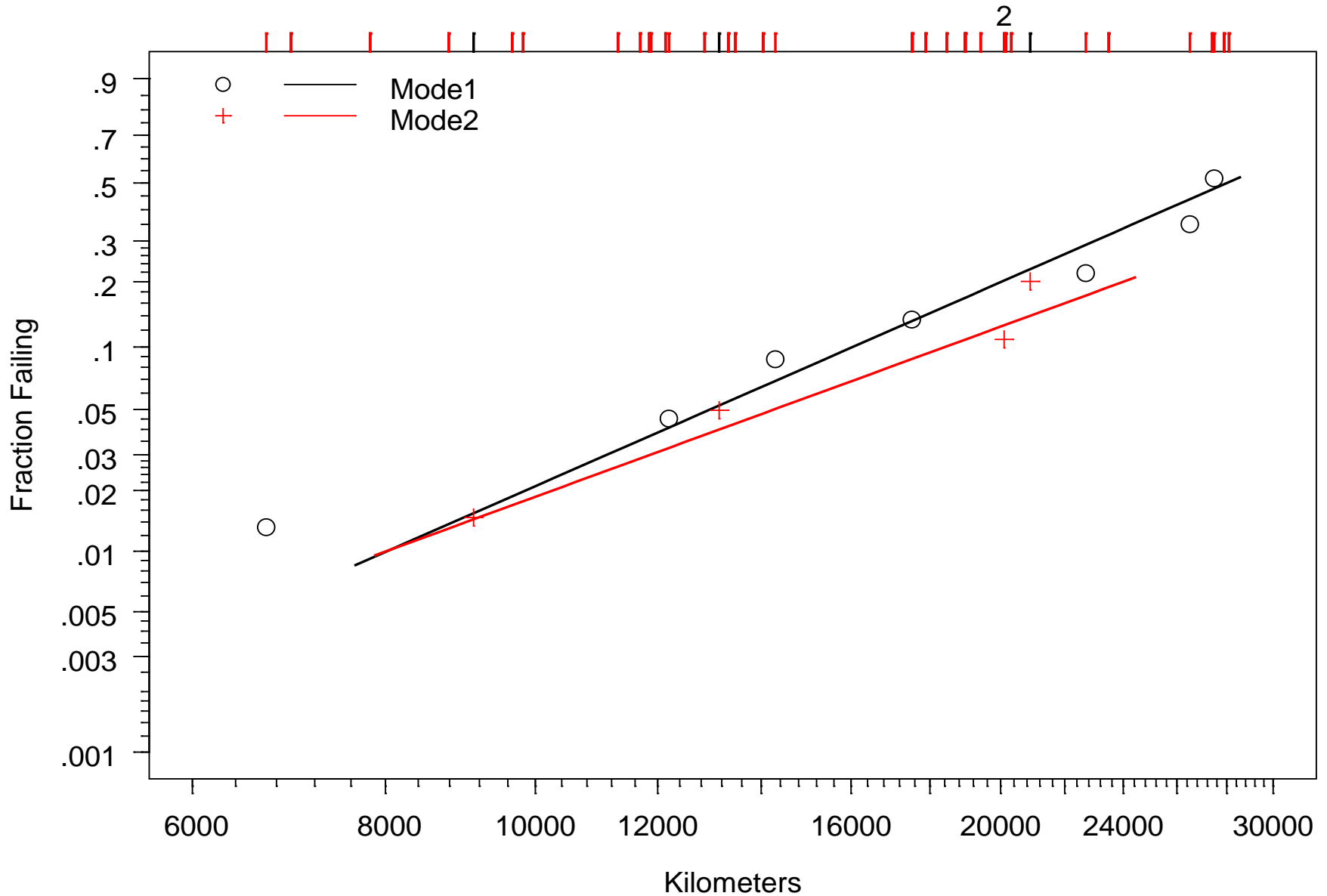
Shock Absorber Data (Both Failure Modes)  
with Weibull ML Estimate and Pointwise 95% Confidence Intervals  
Weibull Probability Plot



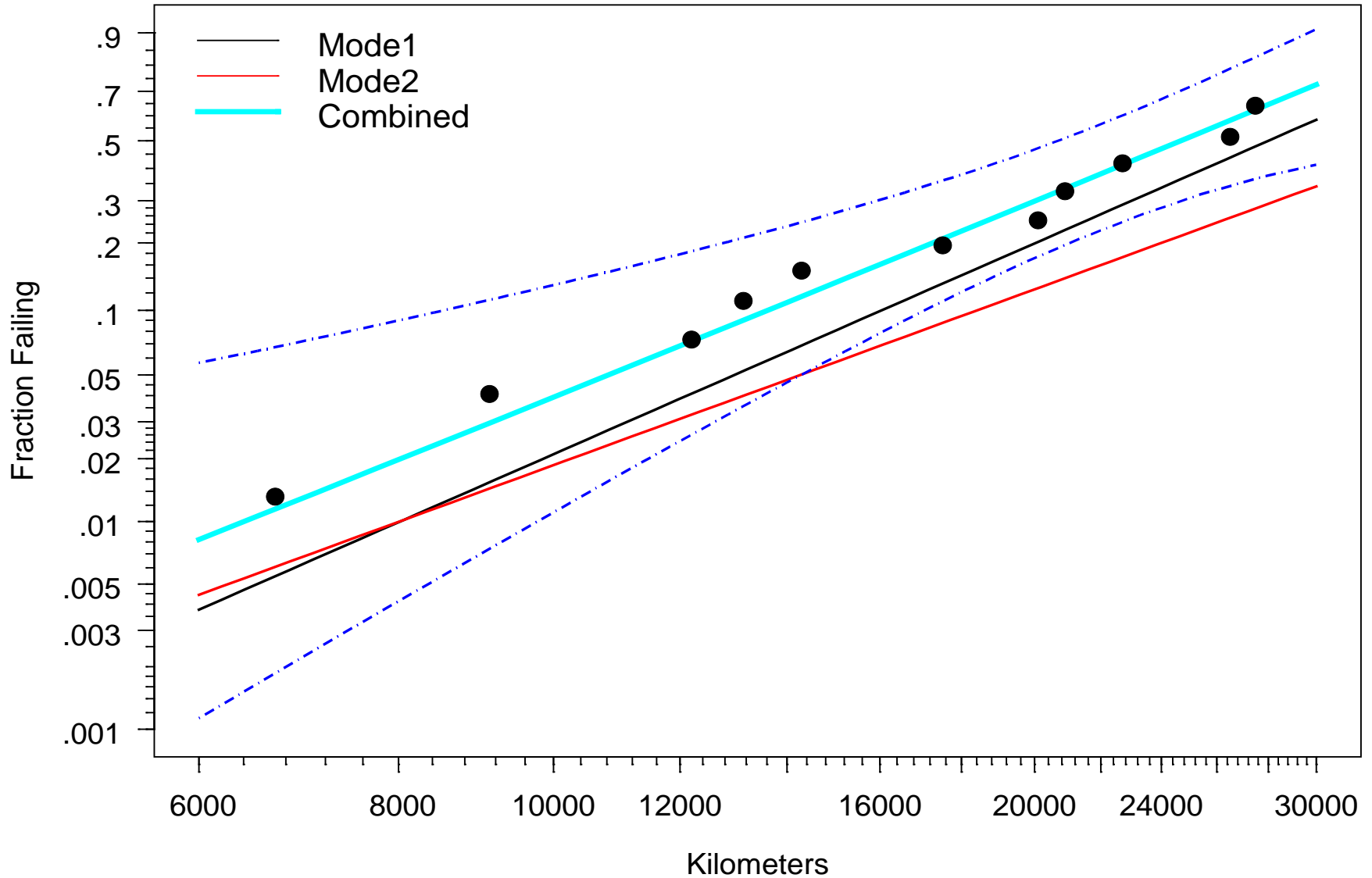
# Individual Shock Absorber Data (Both Failure Modes) Failure Mode Weibull MLE's Weibull Probability Plot



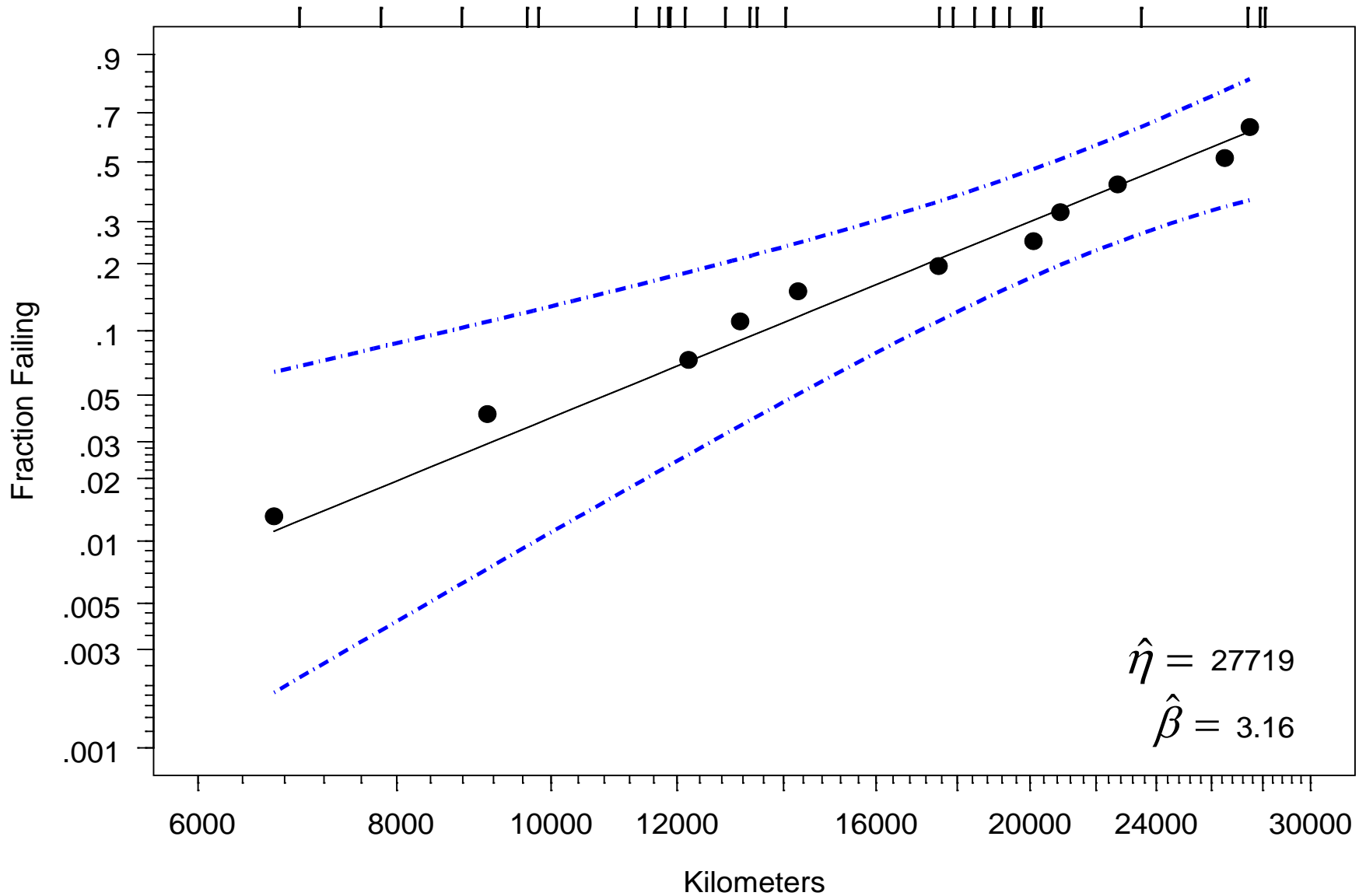
# Individual Shock Absorber Data (Both Failure Modes) Failure Mode Weibull MLE's Weibull Probability Plot



Series System Combined Failure Mode ML Estimates  
and Pointwise Approximate 95% Confidence Intervals Shock Absorber Data (Both Failure M  
Weibull Probability Plot



Shock Absorber Data (Both Failure Modes)  
with Weibull ML Estimate and Pointwise 95% Confidence Intervals  
Weibull Probability Plot

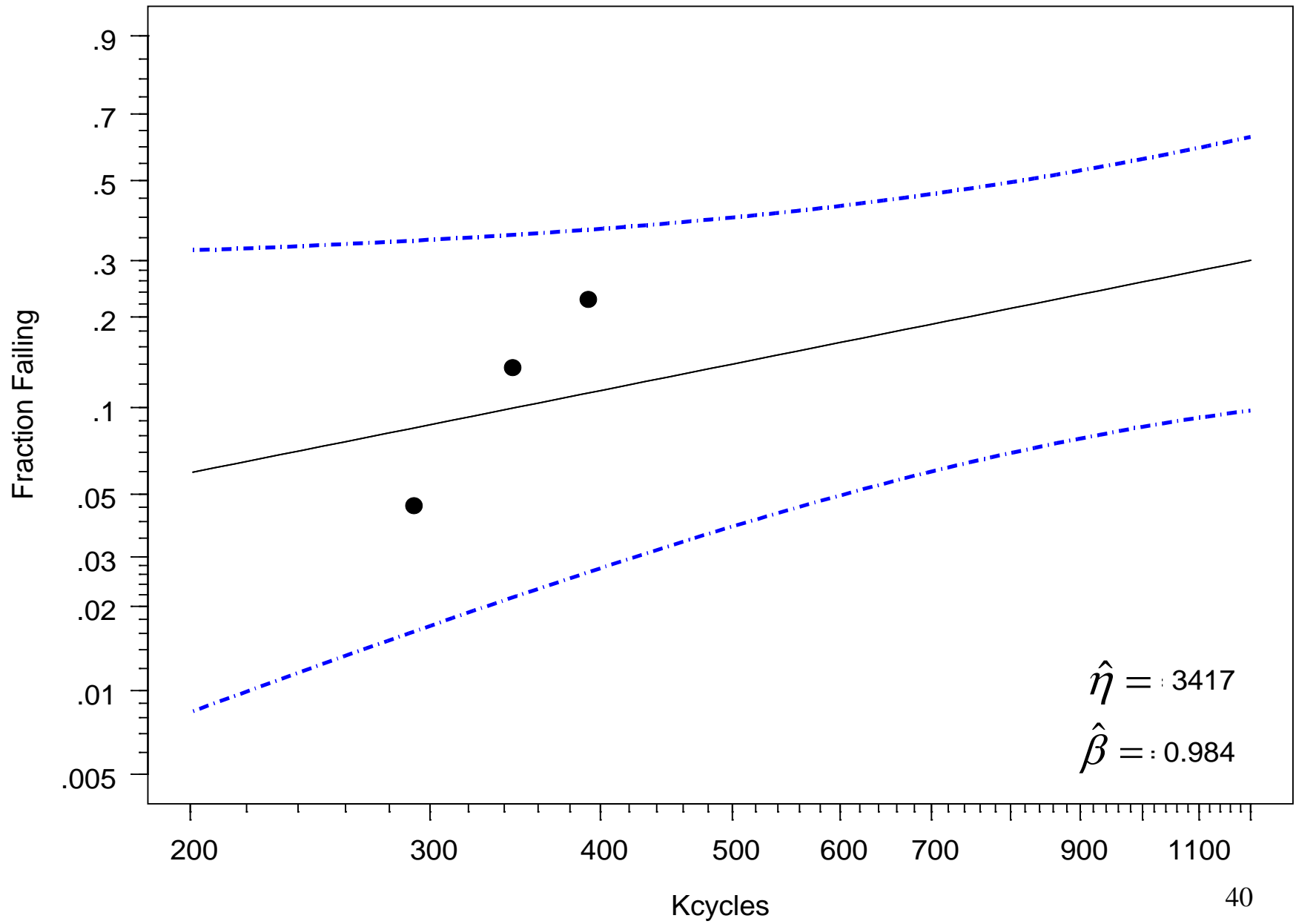


# Lessons Learned

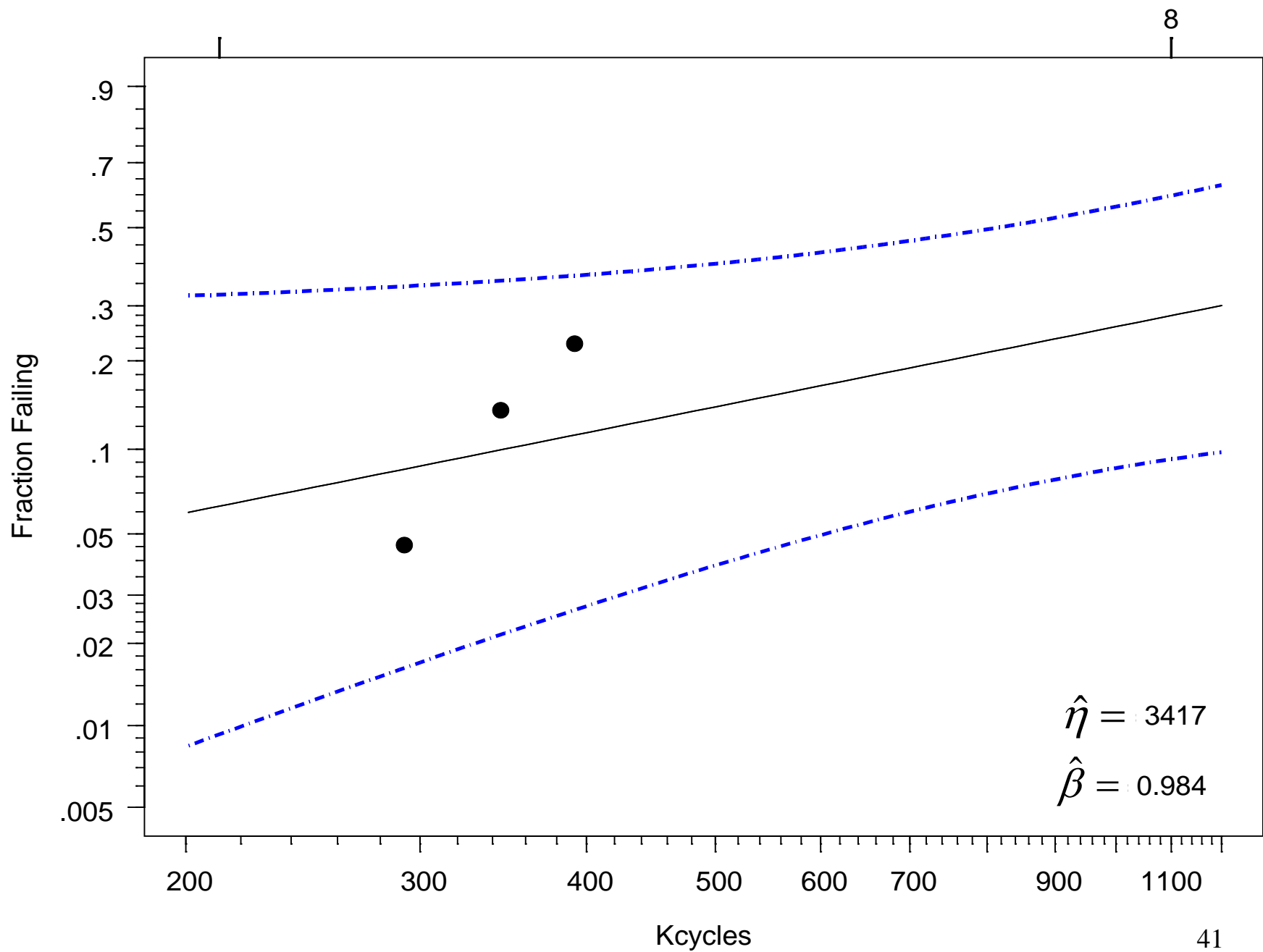
- If there is more than one failure mode, it is important to separate and analyze failure modes separately when
  - Shape parameters are very different
  - There is need to assess the impact of eliminating a failure mode

# Bearing-A Bench Test Results

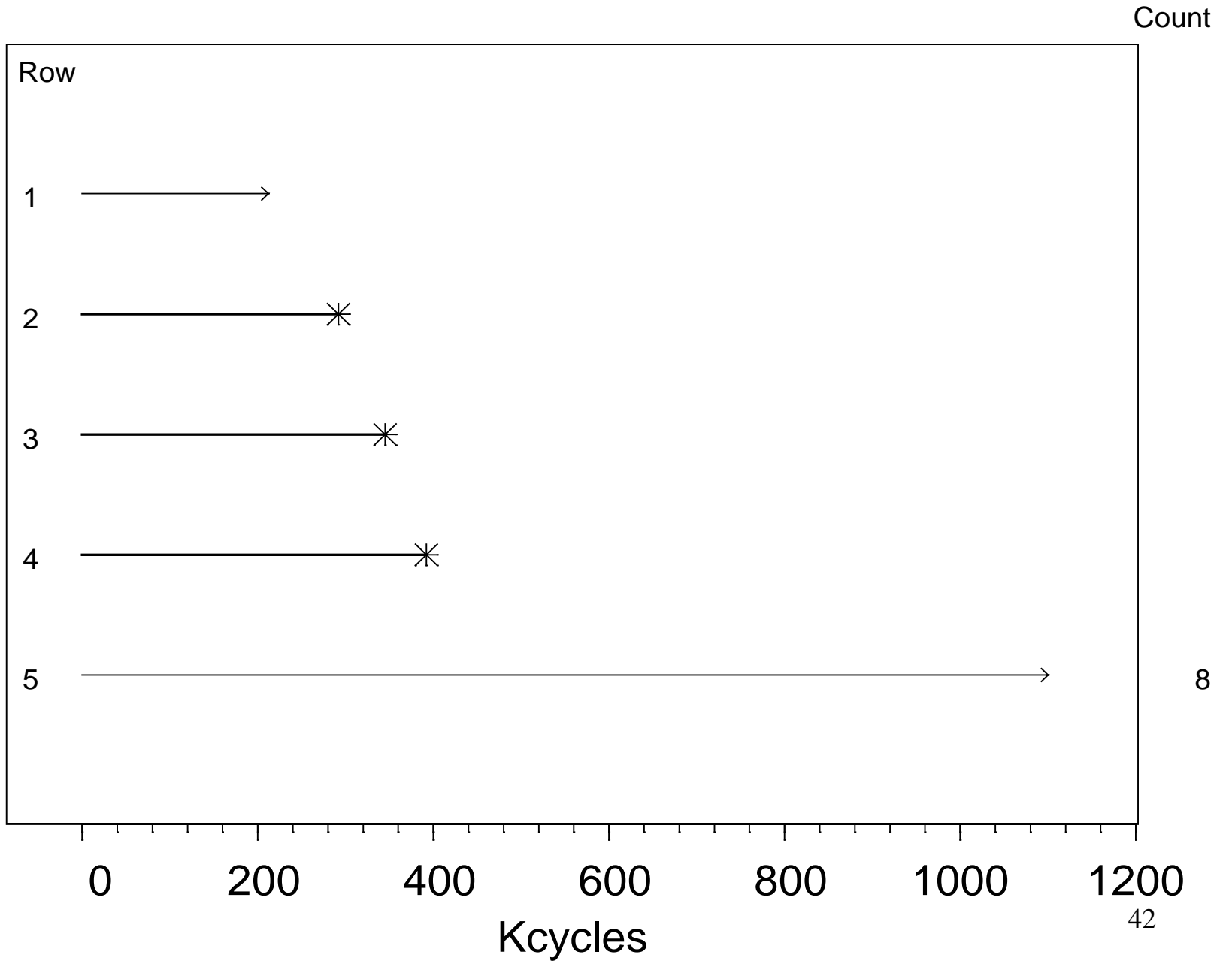
- Data from student in 1999 FTC short course
- Continuous-run test for a newly designed bearing
- Sample of 12 units put on test; one early removal; 3 failures.
- Test terminated at 1100 thousand cycles







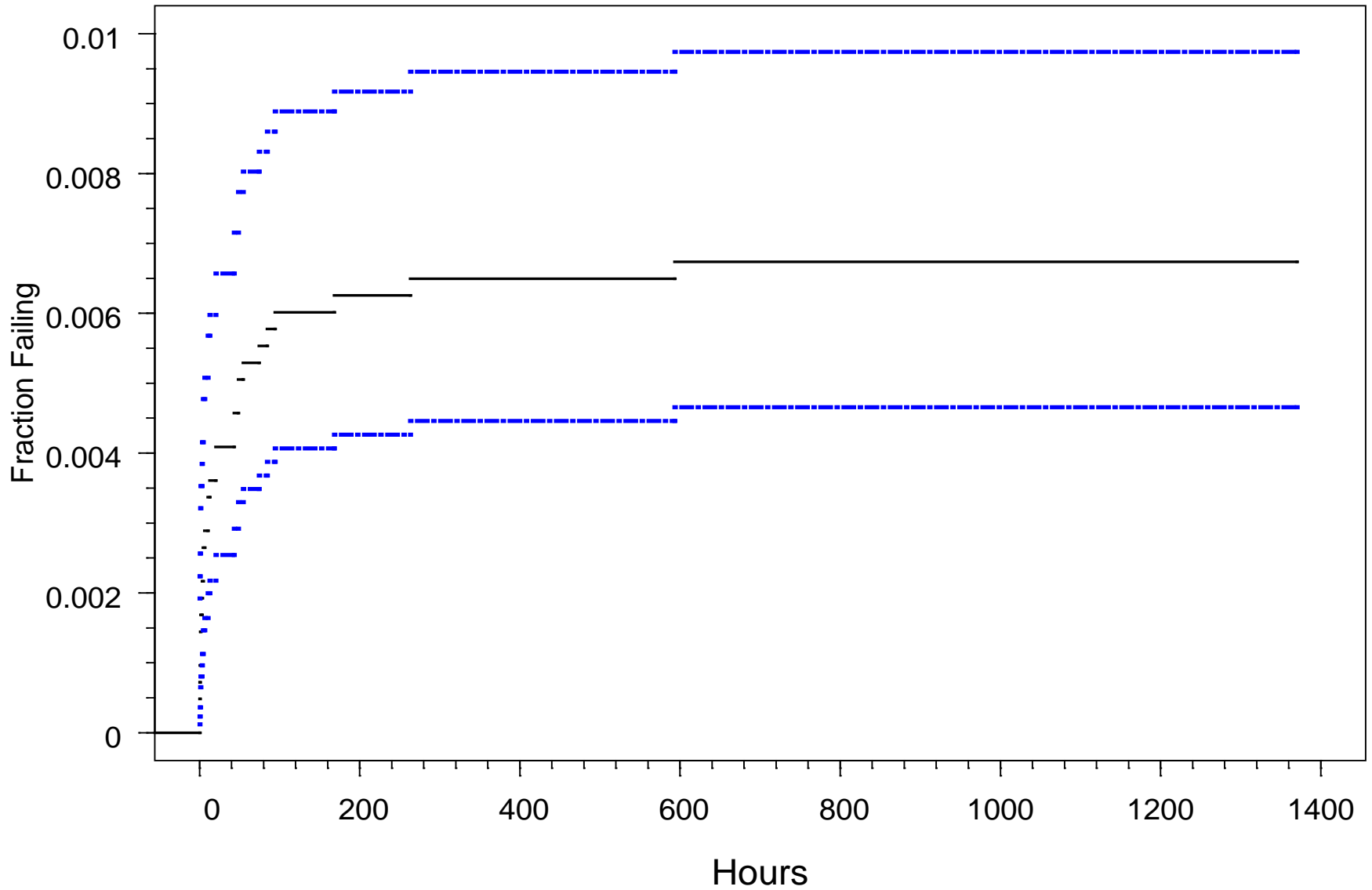
# BearingA data



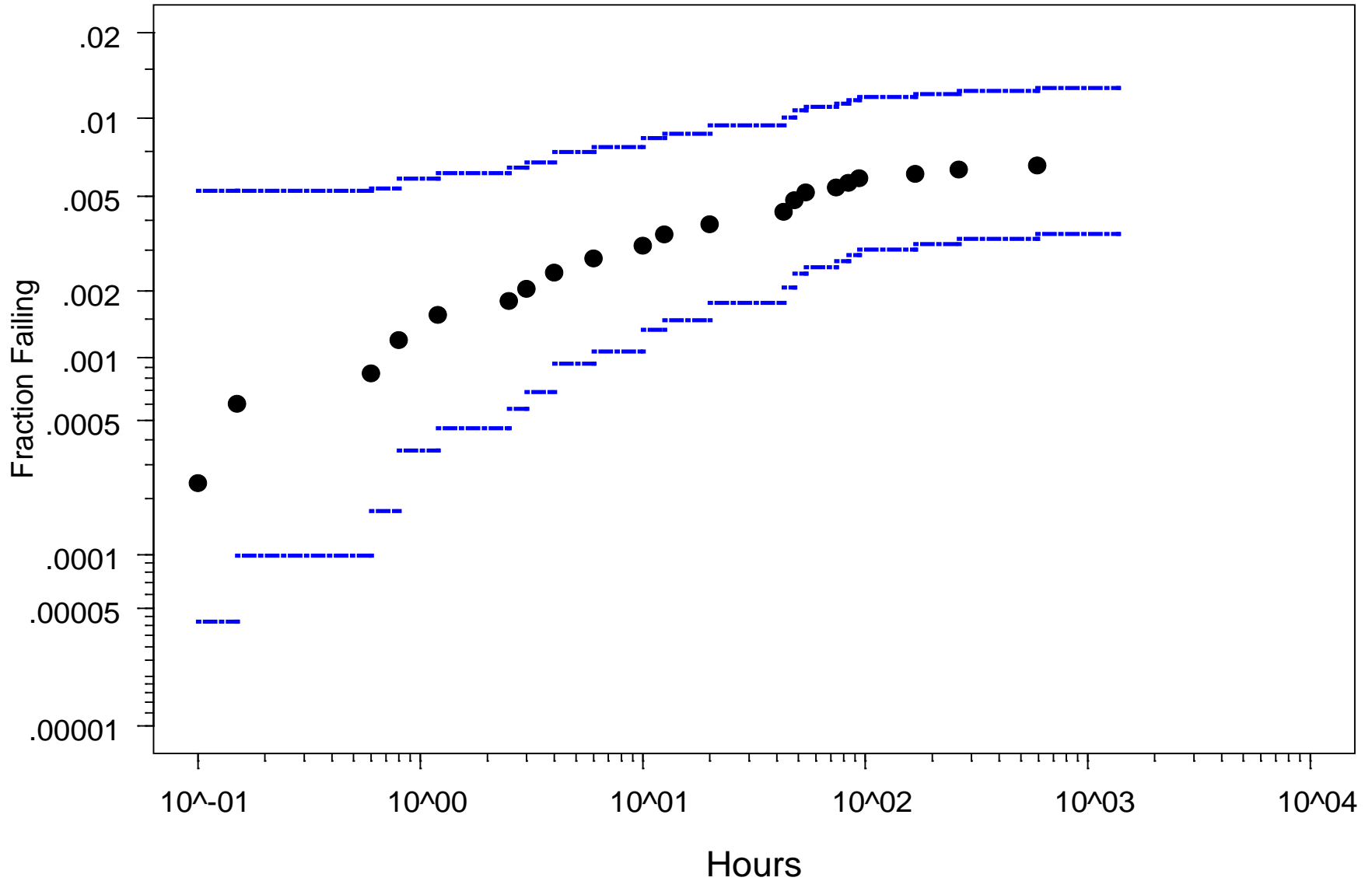
# IC Device Accelerated Life Test

- Data from Meeker (1987)
- 4156 units tested for 1370 hours
- 28 failures; last failure at 593 hours
- Needed information: fraction failing at 20,000 hours

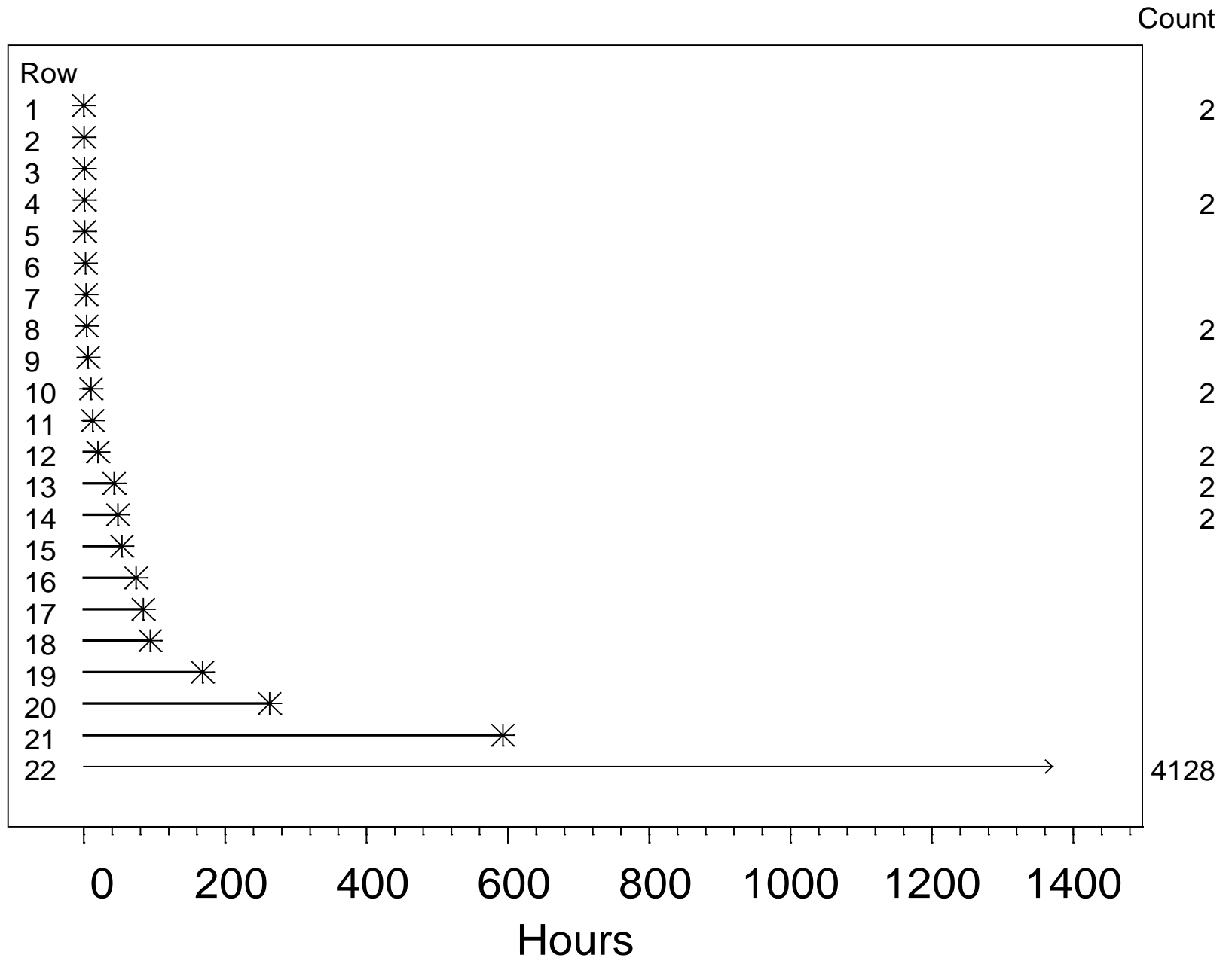
Integrated Circuit Failure Data After 1370 Hours  
with Nonparametric Pointwise 95% Confidence Bands



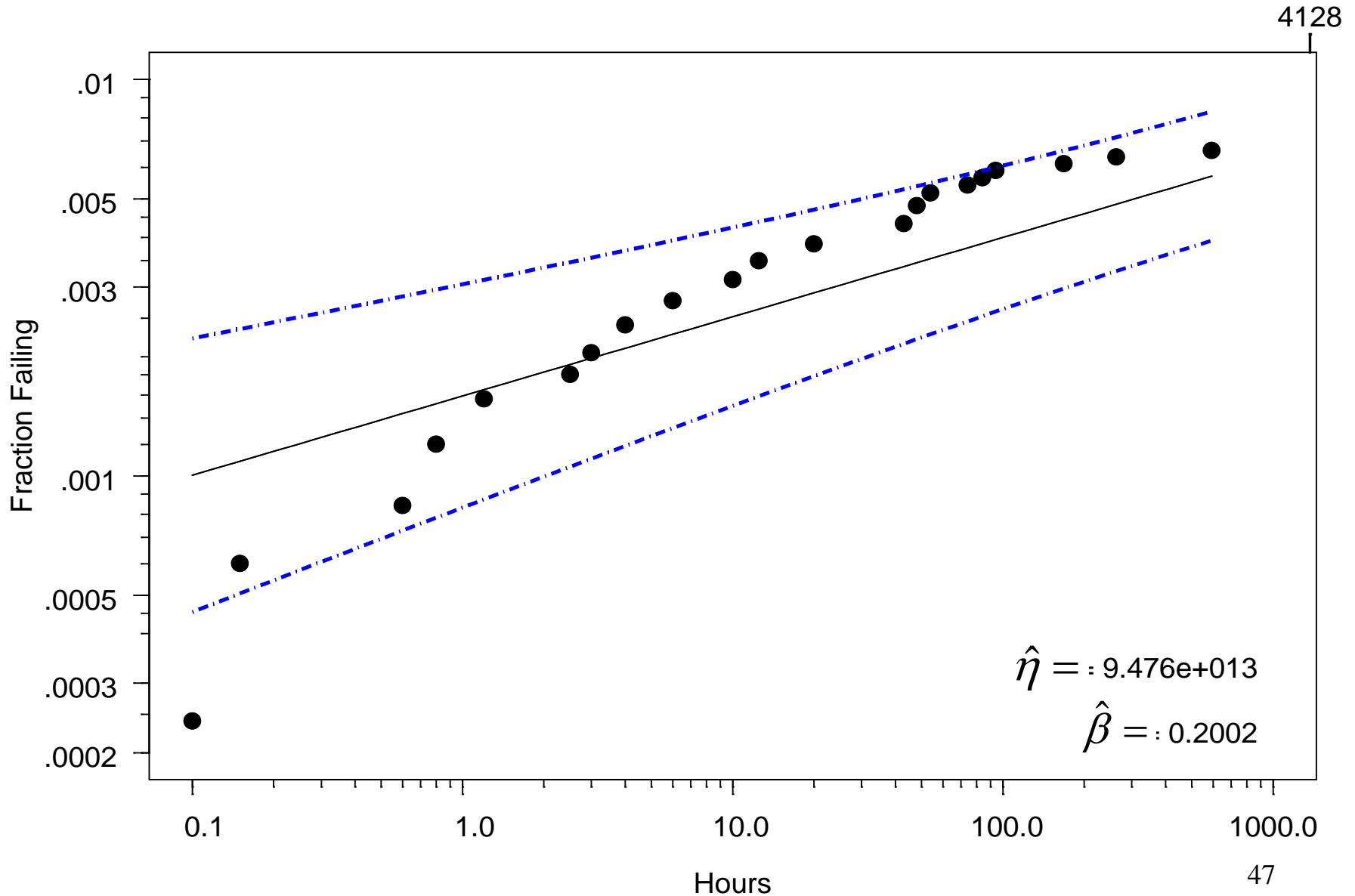
Integrated Circuit Failure Data After 1370 Hours  
with Nonparametric Simultaneous 95% Confidence Bands  
Lognormal Probability Plot



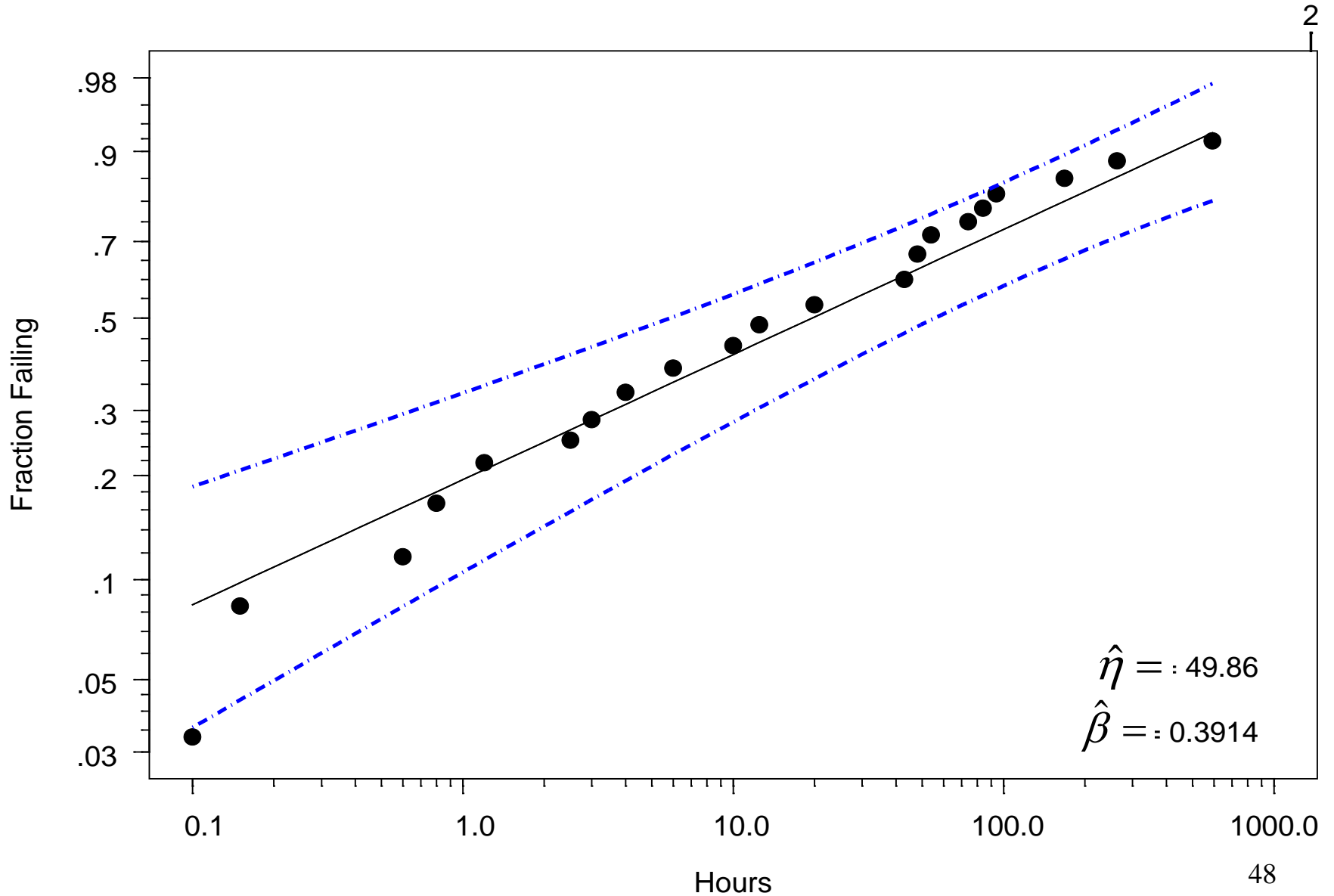
# Integrated Circuit Failure Data After 1370 Hours



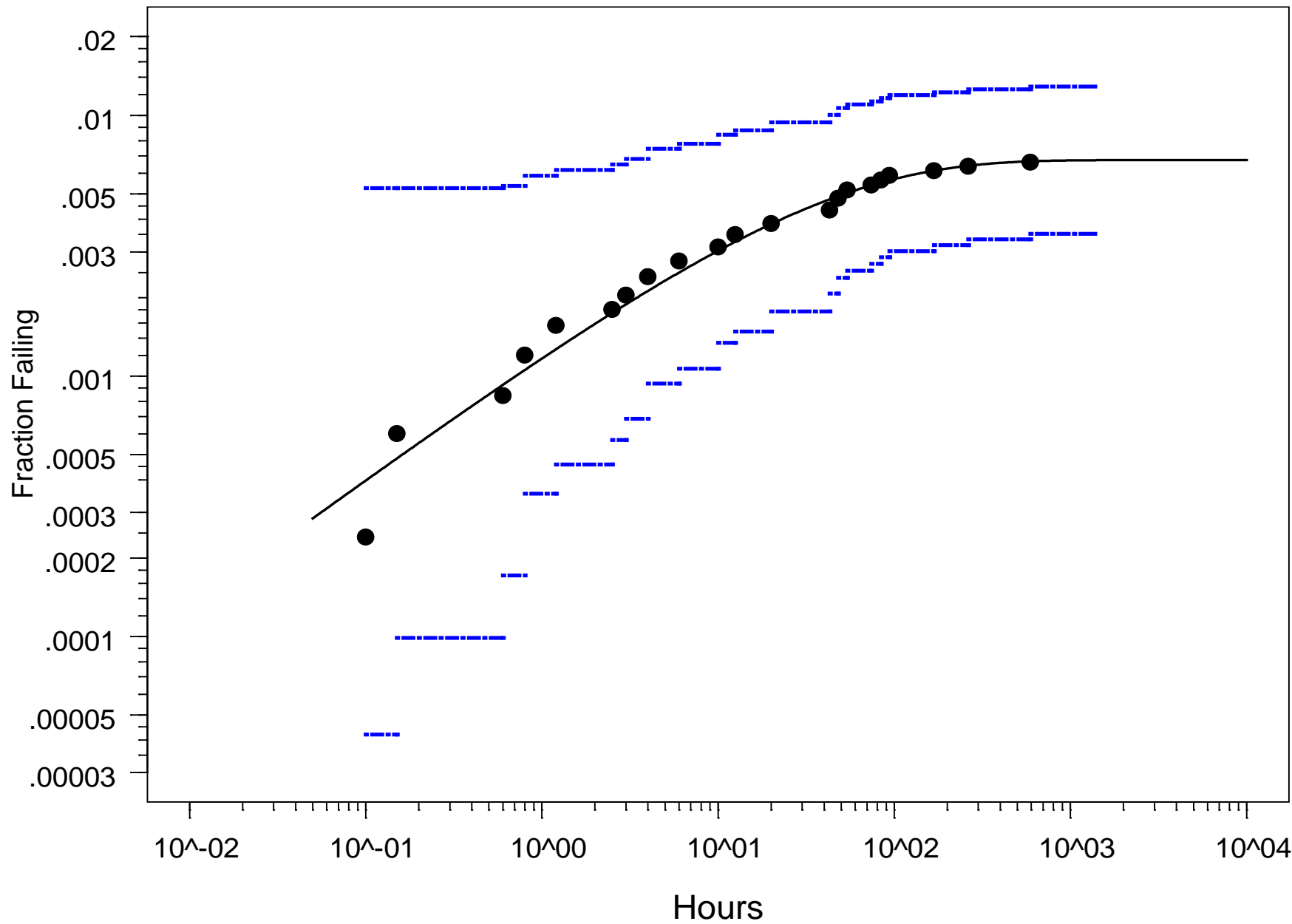
Integrated Circuit Failure Data After 1370 Hours  
with Weibull ML Estimate and Pointwise 95% Confidence Intervals  
Weibull Probability Plot



Ifp1370Fix2 data  
with Weibull ML Estimate and Pointwise 95% Confidence Intervals  
Weibull Probability Plot







# Lessons Learned

- Leveling of a probability plot usually implies a “limited failure population.”
- If you do not wait long enough
  - You cannot decide if you have many units failing slowly or a small fraction failing early.
  - Conclusions will depend strongly on the assumed distribution model

# Motivation for Accelerated Testing

Today manufactures need to develop newer, higher technology products in record time while improving productivity, reliability, and quality.

- Rapid product development.
- Changing technologies/new materials
- More complicated products with more components
- Higher customer expectations for better reliability

# Levels of Accelerated Testing

- Materials
- Components
- Subsystem
- Full system

Usually testing at higher levels of integration will result in less acceleration

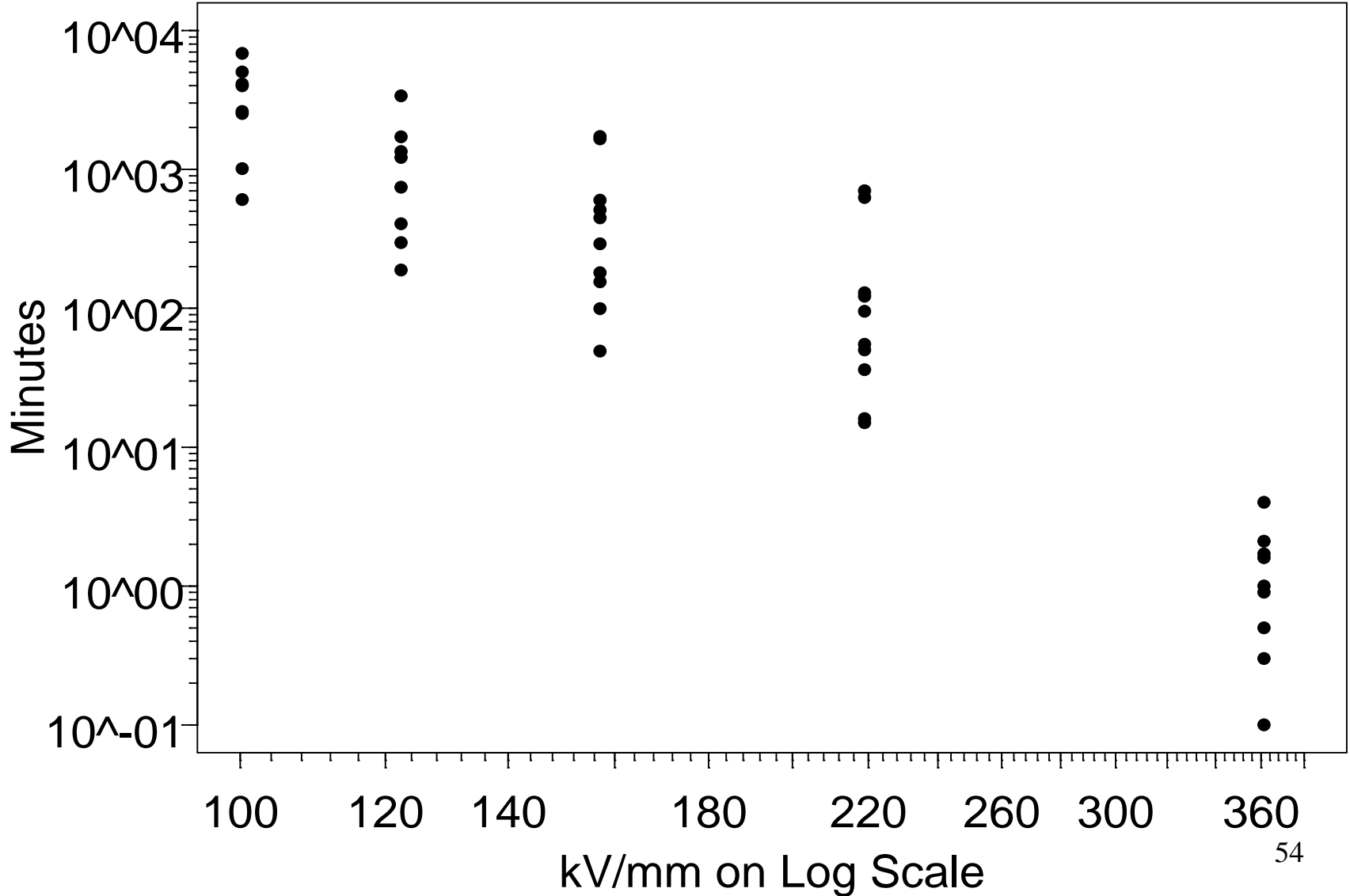
Most accelerated tests are run at lower levels of a product

# Voltage-Accelerated Life Test of a Mylar-Polyurethane Laminated Direct Current High Voltage Insulating Structure

- Data from Kalkanis and Rosso (1989)
- Time to dielectric breakdown of units tested at 100.3, 122.4, 157.1, 219.0, and 361.4 kV/mm.
- Needed to evaluate the reliability of the insulating structure and to estimate the life distribution at system design voltages (e.g. 50 kV/mm).

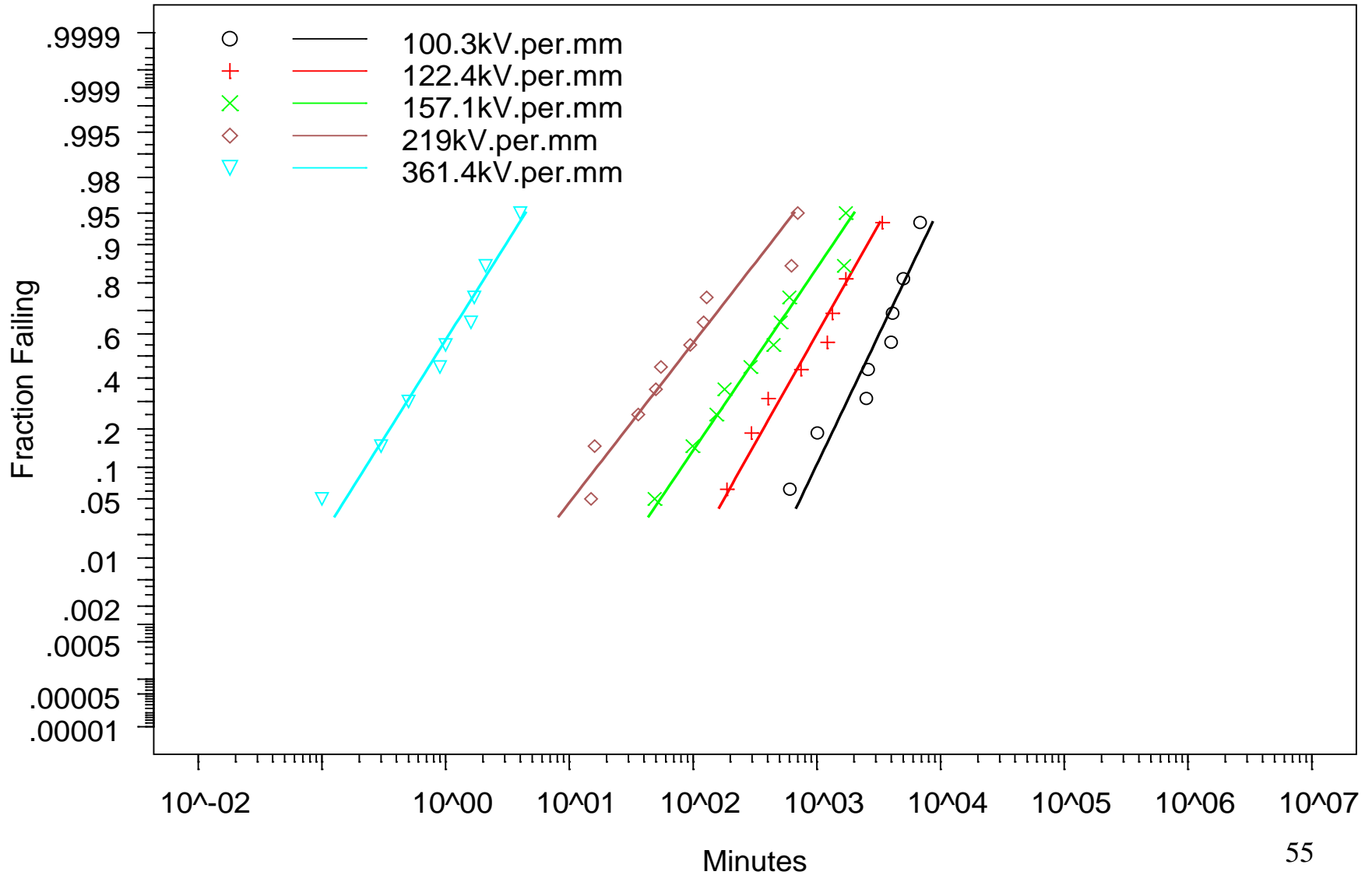
Mylar-Polyurethane Laminated Direct Current High  
Voltage Insulating Structure

# Cross Plot on Log-Log Paper



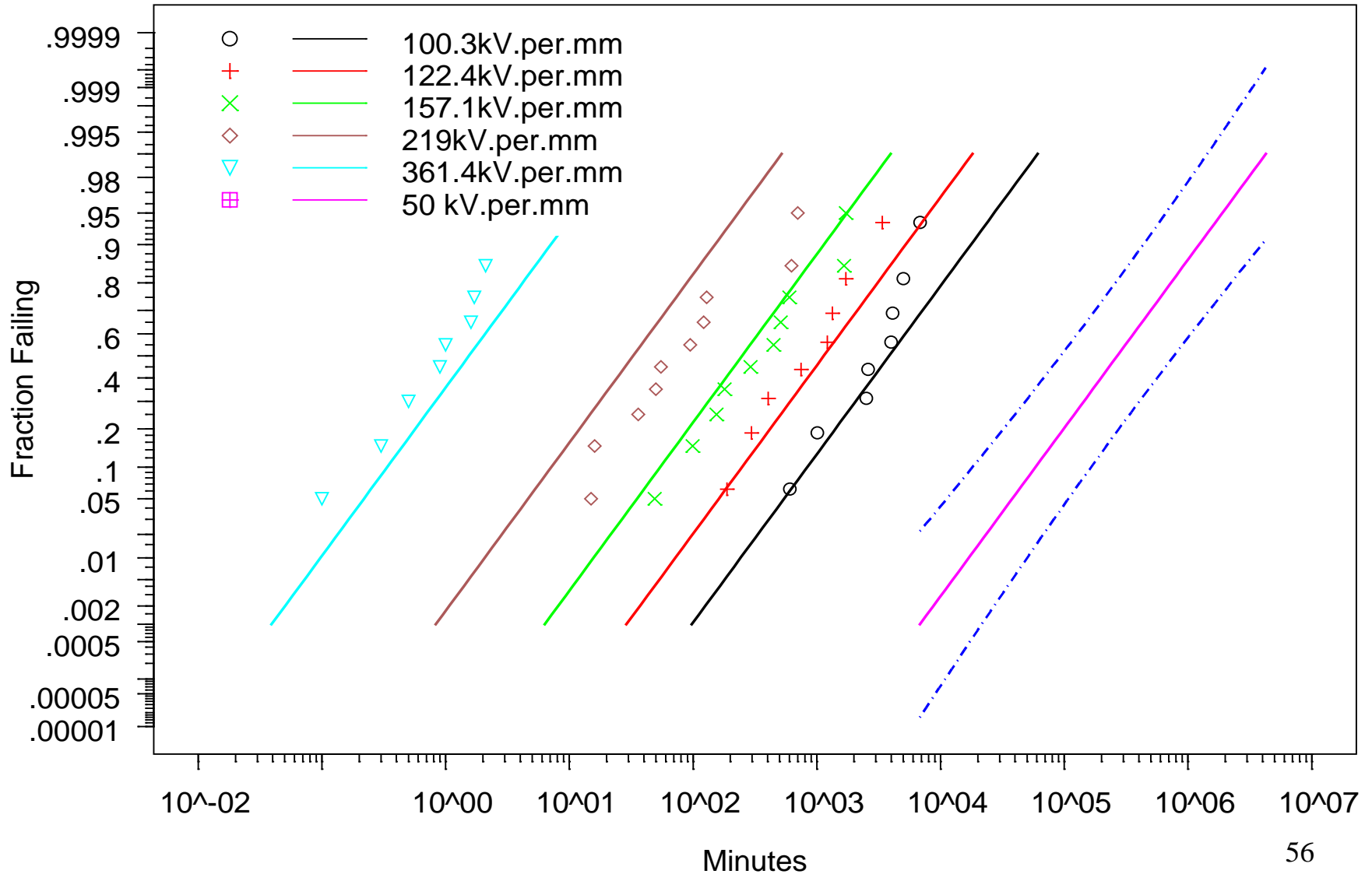
# Mylar Polyurethane Insulating Structure

## Data Analysis at Individual Conditions



# Mylar Polyurethane Insulating Structure Data

## Inverse Power Regression Model **All Data**





# The Inverse Power Law/Lognormal Model for Insulation Lifetimes

- Life =  $CV^{\beta_1}$
- The probability of failure as a function of time is

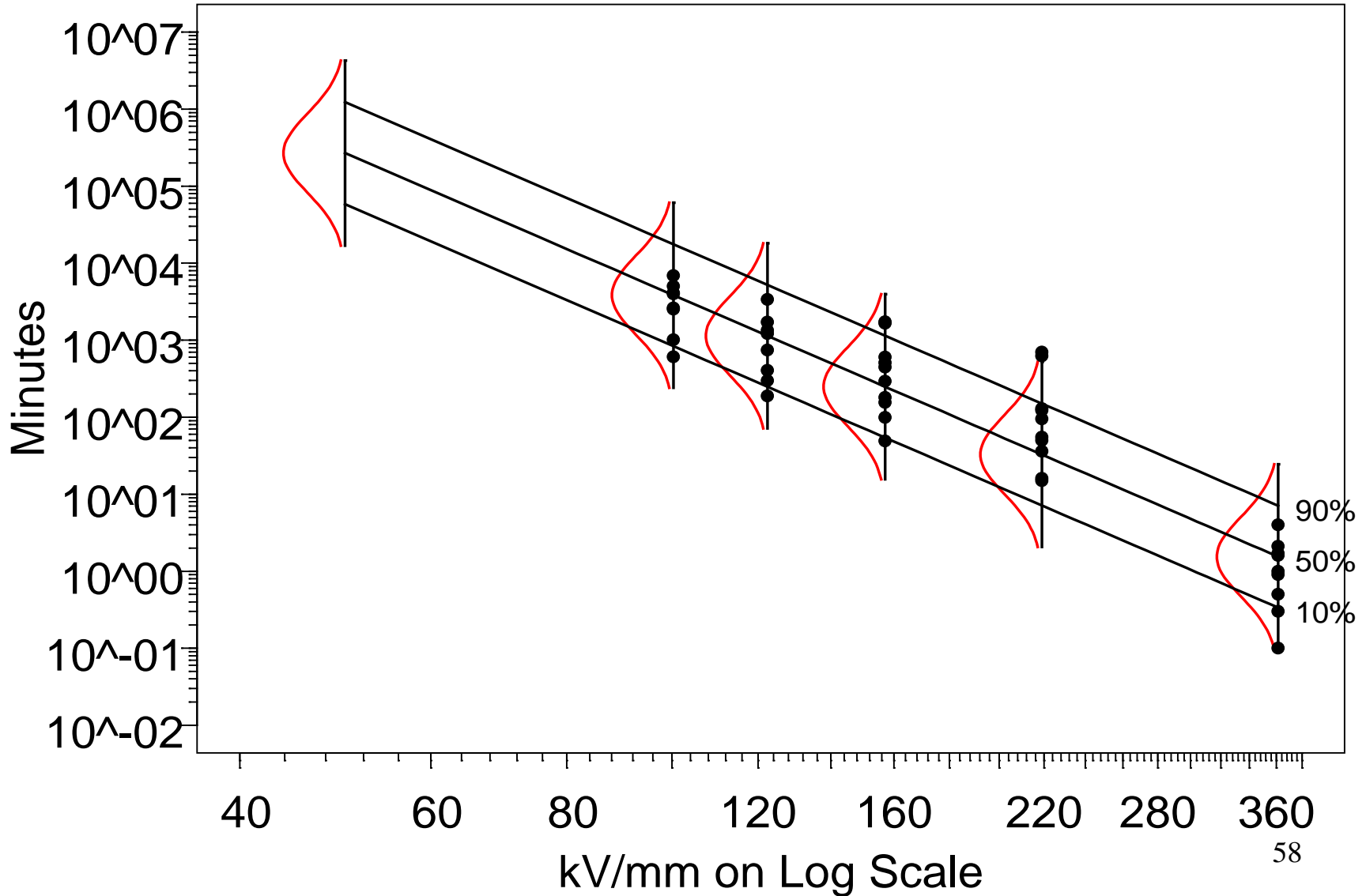
$$\Pr[T(\text{temp}) \leq t] = \Phi_{\text{NOR}} \left[ \frac{\log(t) - \mu(x)}{\sigma} \right]$$

$$\mu(x) = \beta_0 + \beta_1 x$$

- $x = \log(\text{Voltage Stress})$
- $\beta_1$  is negative because life is shorter at higher levels of voltage stress
- $\sigma$  is assumed not to depend on voltage stress
- Similar relationships used for pressure and cycling rate

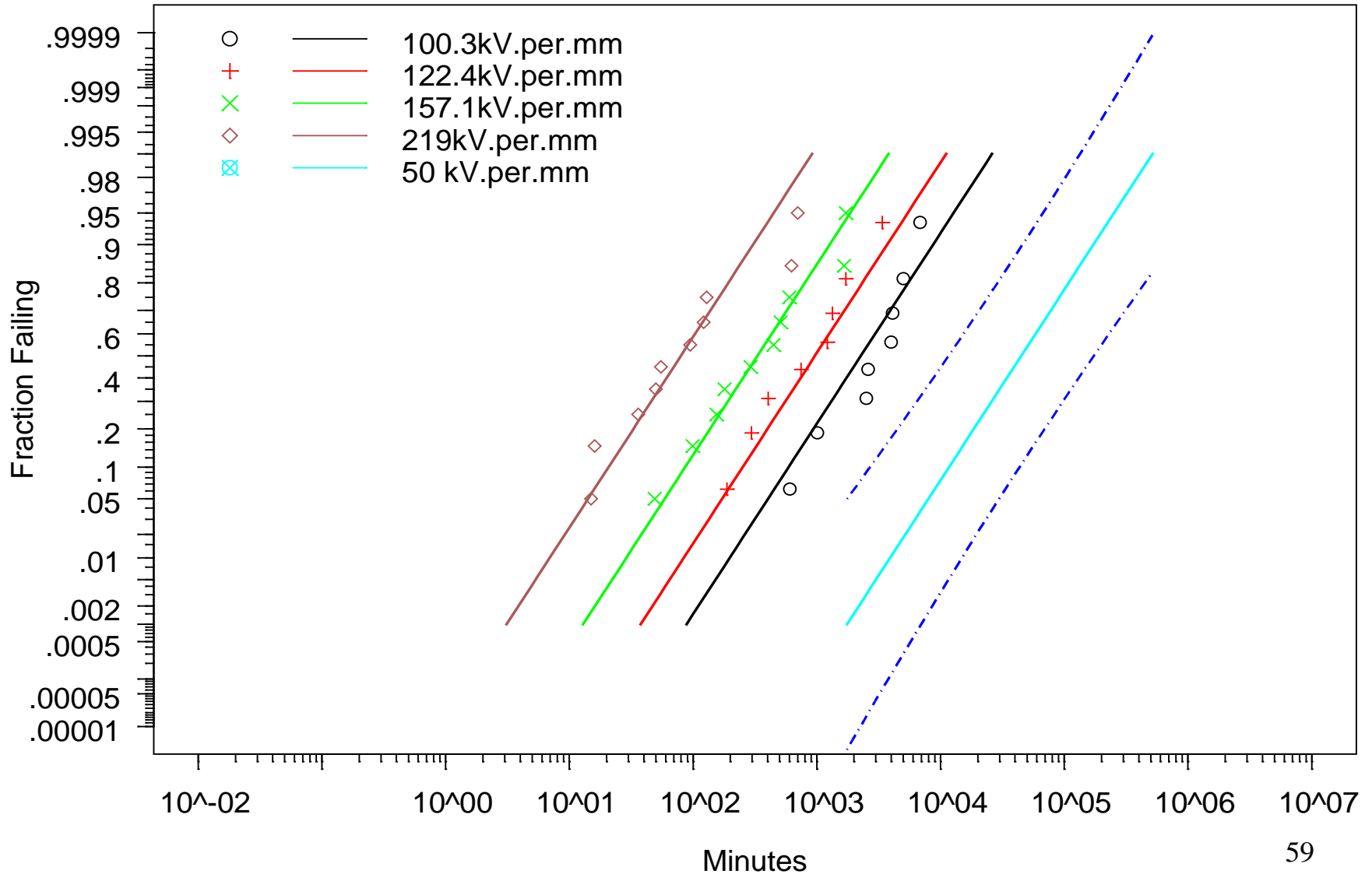
# Mylar Polyurethane Insulating Structure Data

## Inverse Power Regression Model **All Data**



# Mylar Polyurethane Insulating Structure Data

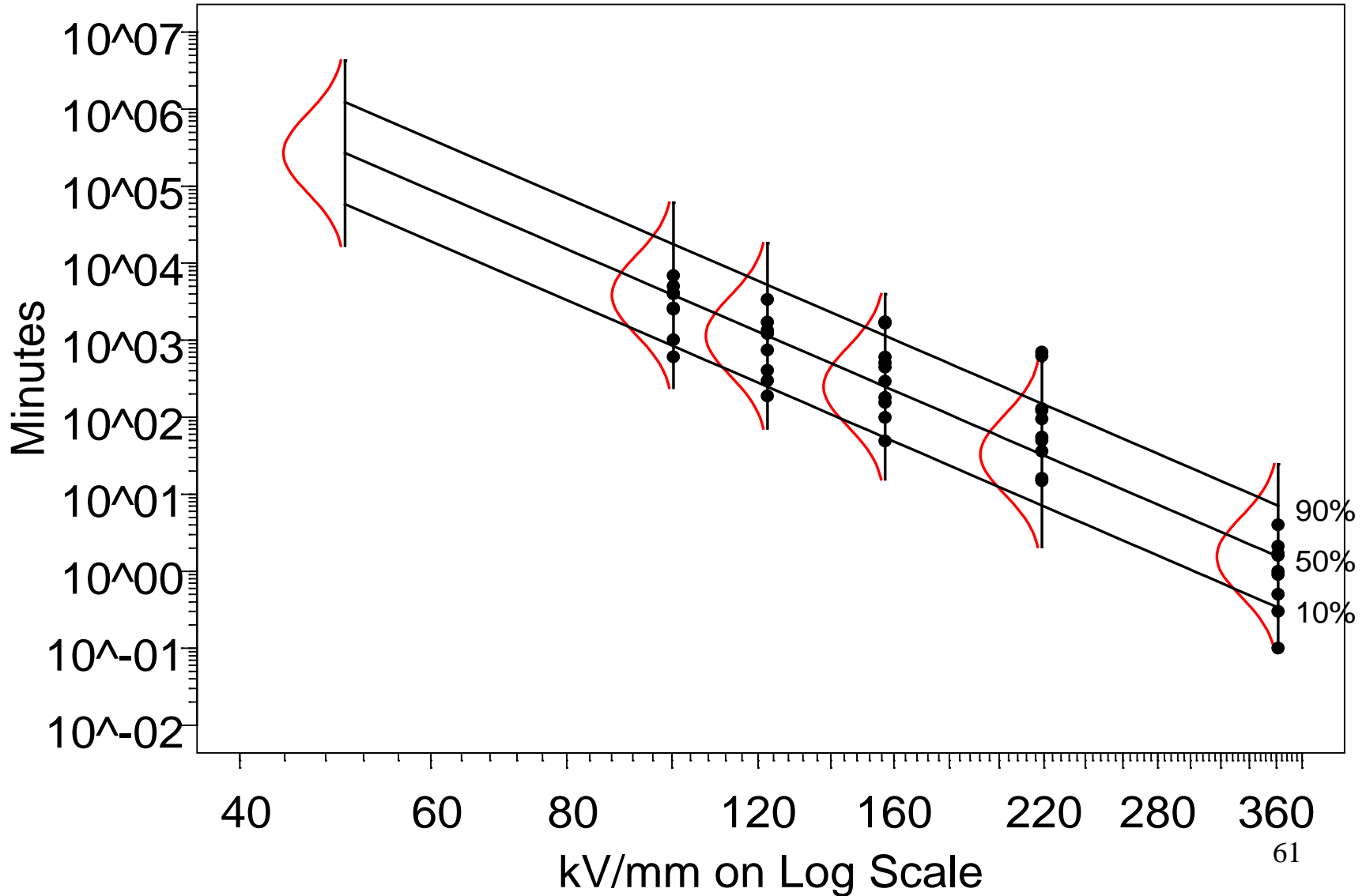
## Inverse Power Regression Model **Good Data**





# Mylar Polyurethane Insulating Structure Data

## Inverse Power Regression Model **All Data**



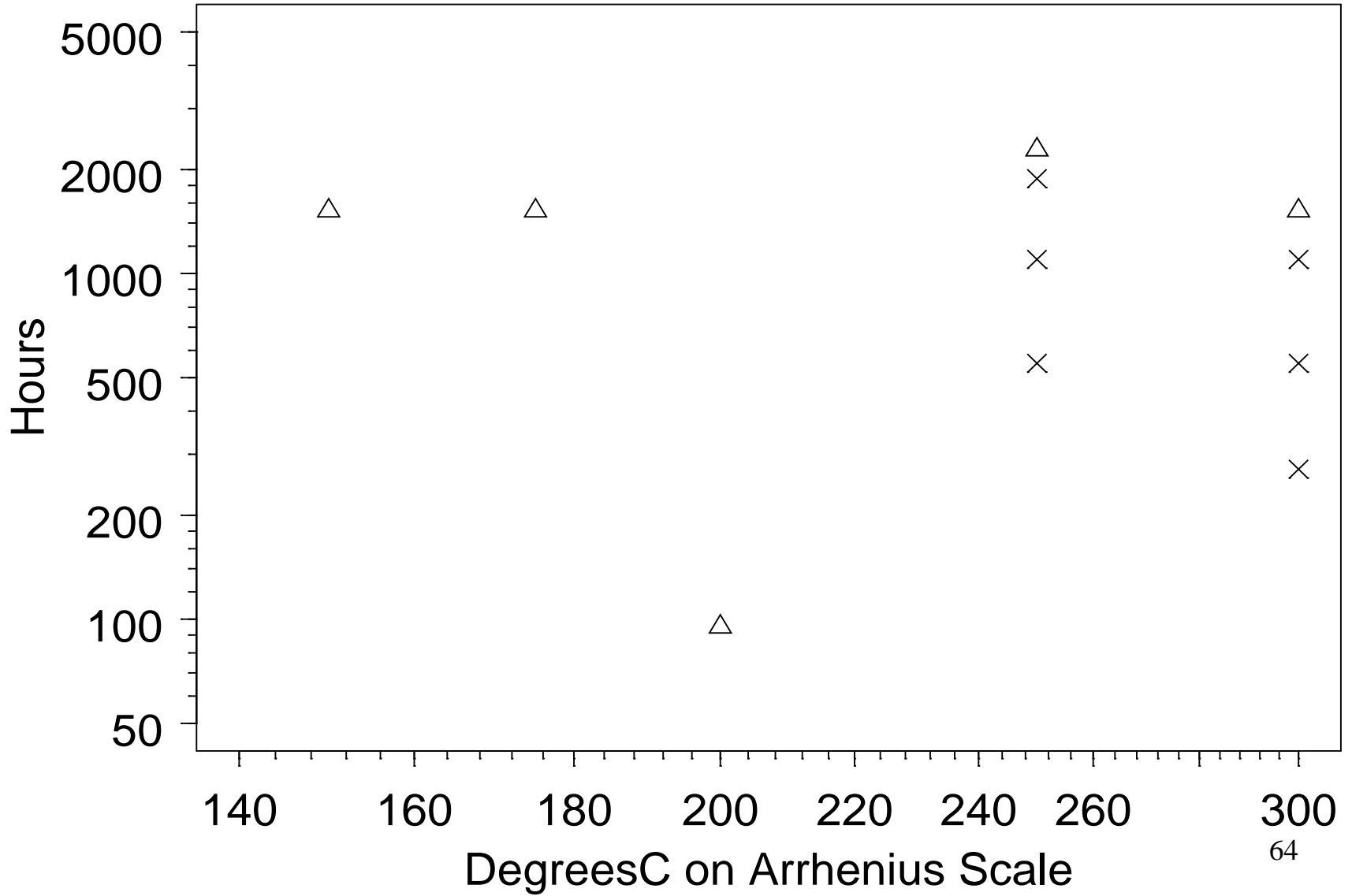
# Lessons Learned

- Transformation of data can simplify modeling
- The inverse power relationship [log life is linear in  $\log(\text{Voltage Stress})$ ] may be useful for modeling dielectric life
- Testing at a voltage stress that is too high can cause new failure modes
- New failure modes at the higher levels of stress, if unrecognized, leads to incorrectly optimistic conclusions
- Structure on a data plot can hide important information

# New Technology IC Device ALT

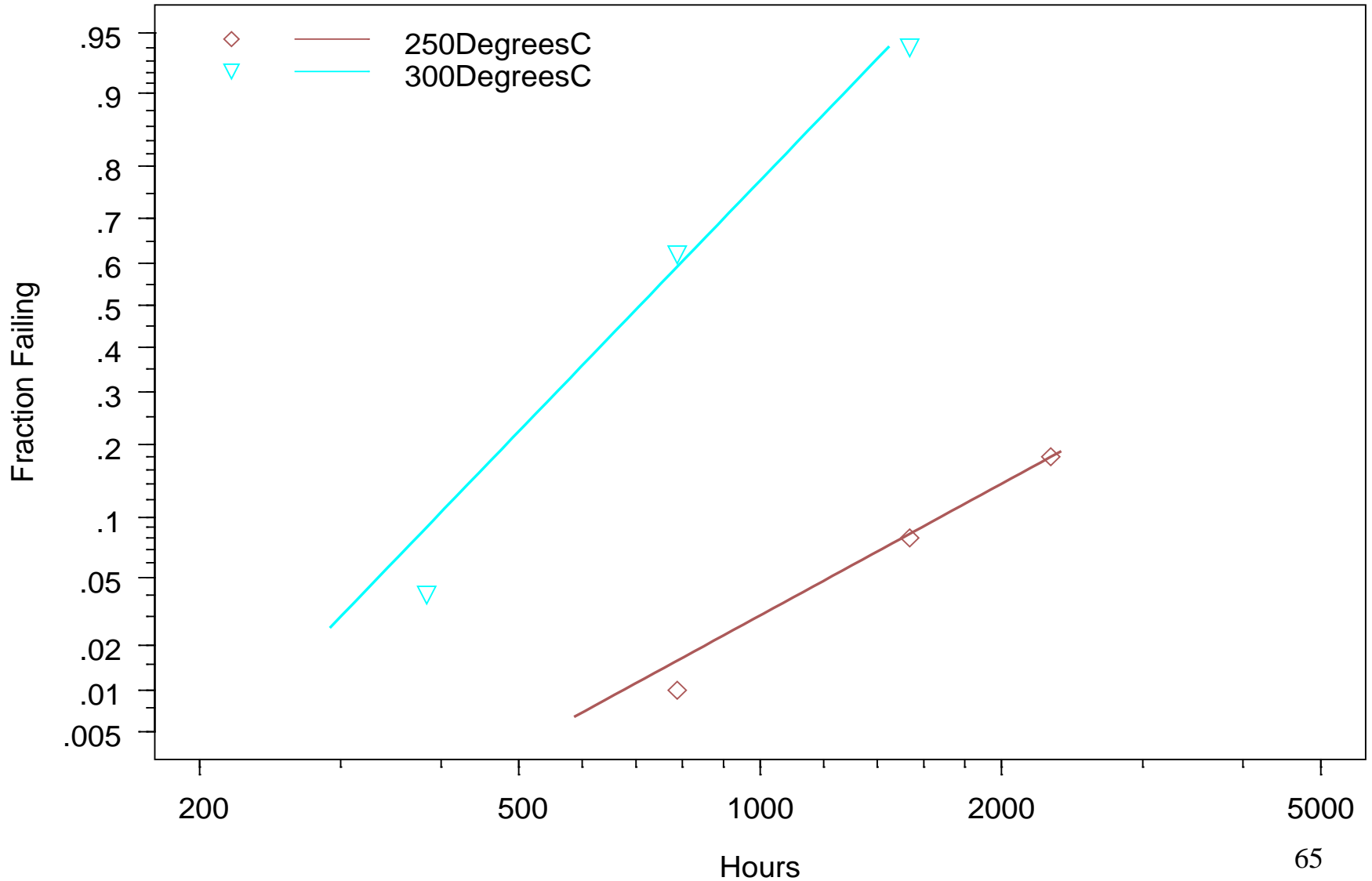
- Data from Meeker and Escobar (1998)
- 50 devices tested at each of 150, 175, 200, 250, and 300 degrees C
- Interval censoring (inspection of devices approximately every four days)
- Failures seen only at 250 and 300 degrees C
- Need to estimate the life distribution at 100 degrees C

# New Technology Device ALT





New Technology Device ALT  
With Individual Lognormal Distribution ML Estimates  
Lognormal Probability Plot



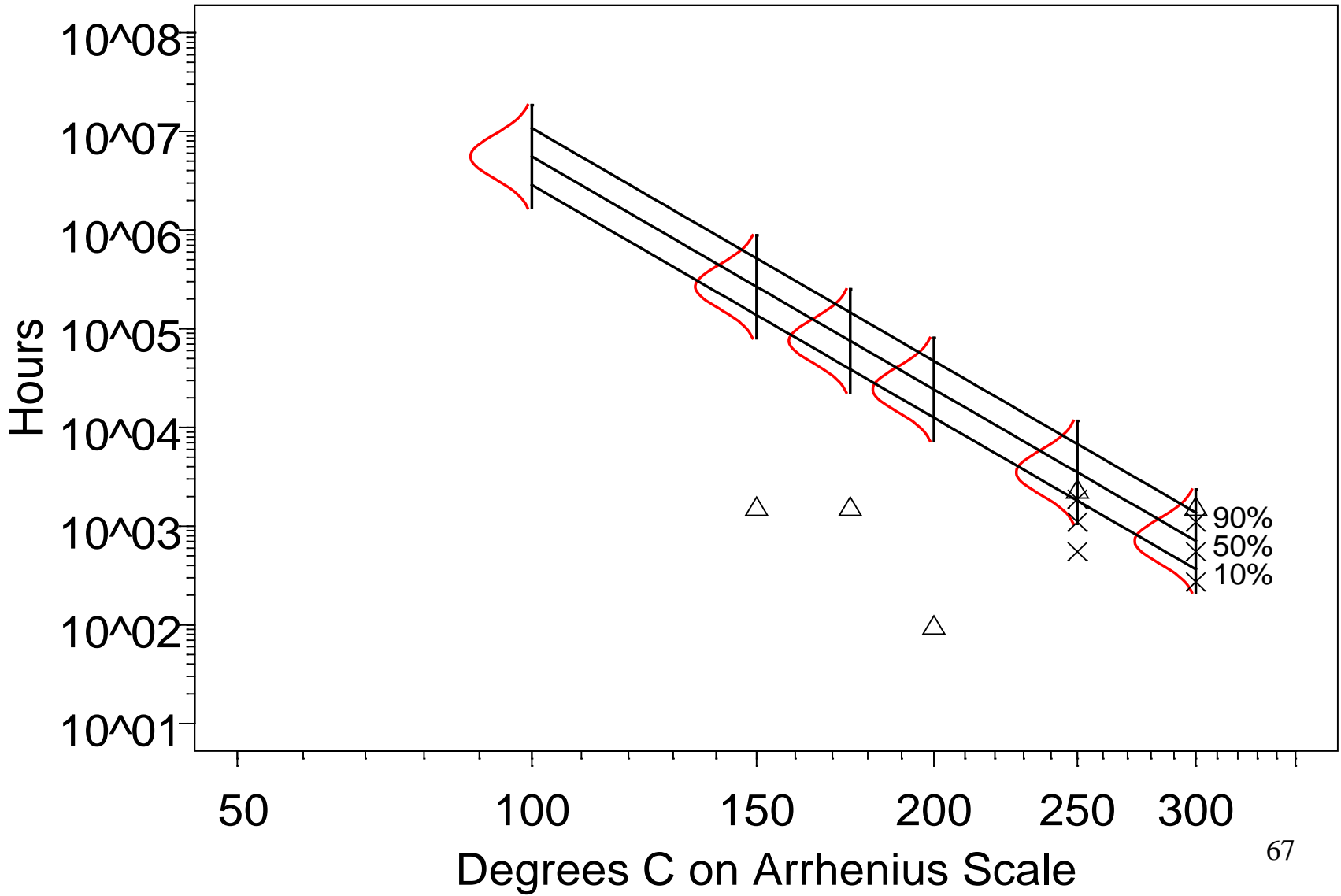
# The Arrhenius/Lognormal Model for Temperature Acceleration

- Log life is inversely proportional to reciprocal Kelvin temperature
- The probability of failure as a function of time is

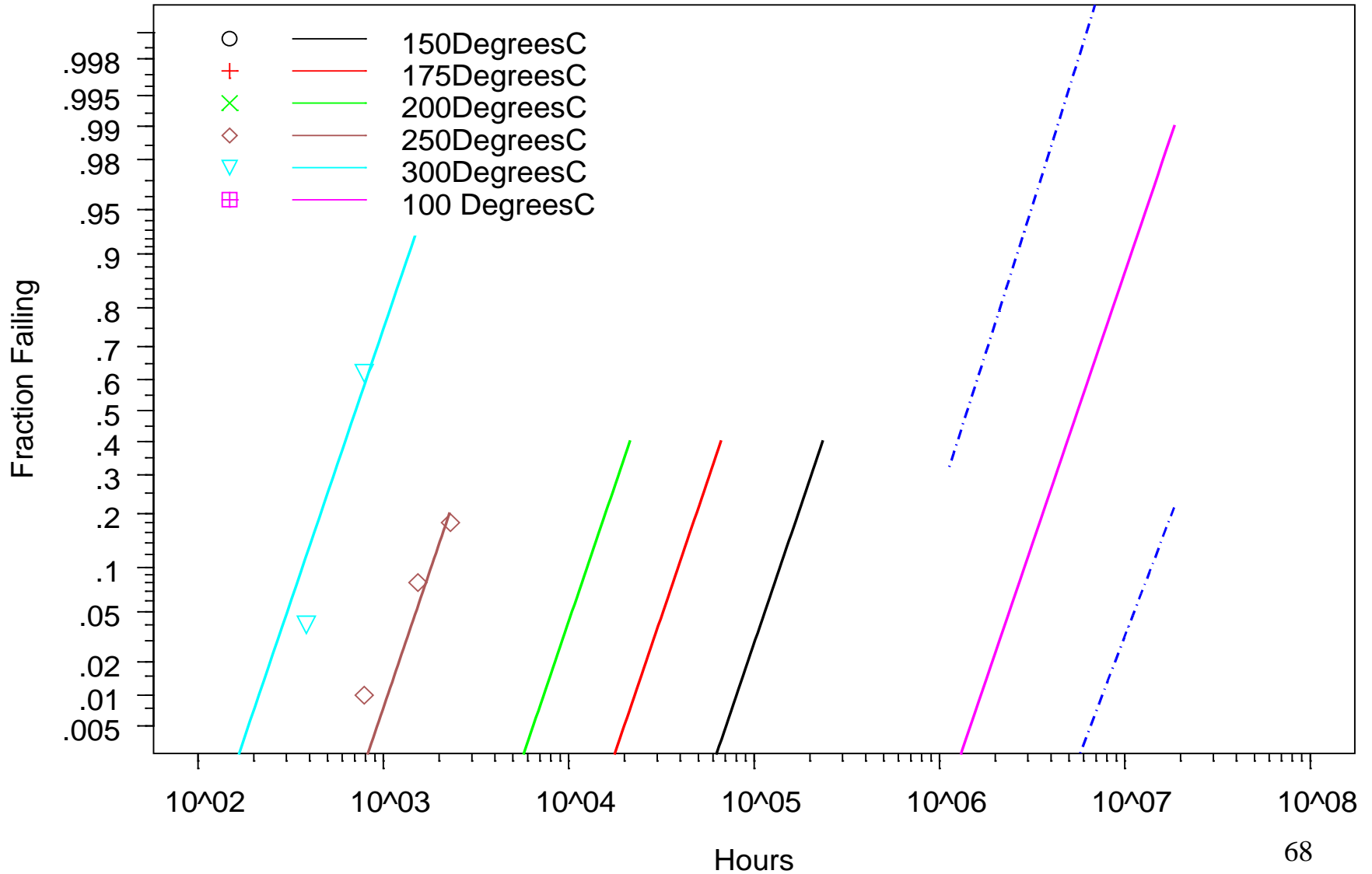
$$\Pr[T(\text{temp}) \leq t] = \Phi_{\text{NOR}} \left[ \frac{\log(t) - \mu(x)}{\sigma} \right]$$
$$\mu(x) = \beta_0 + \beta_1 x$$

- $x = 11605/(\text{Degrees C} + 273.15)$
- $\beta_1$  is the “effective activation energy”
- $\sigma$  does not to depend on temperature
- Widely used in the evaluation of electronic components

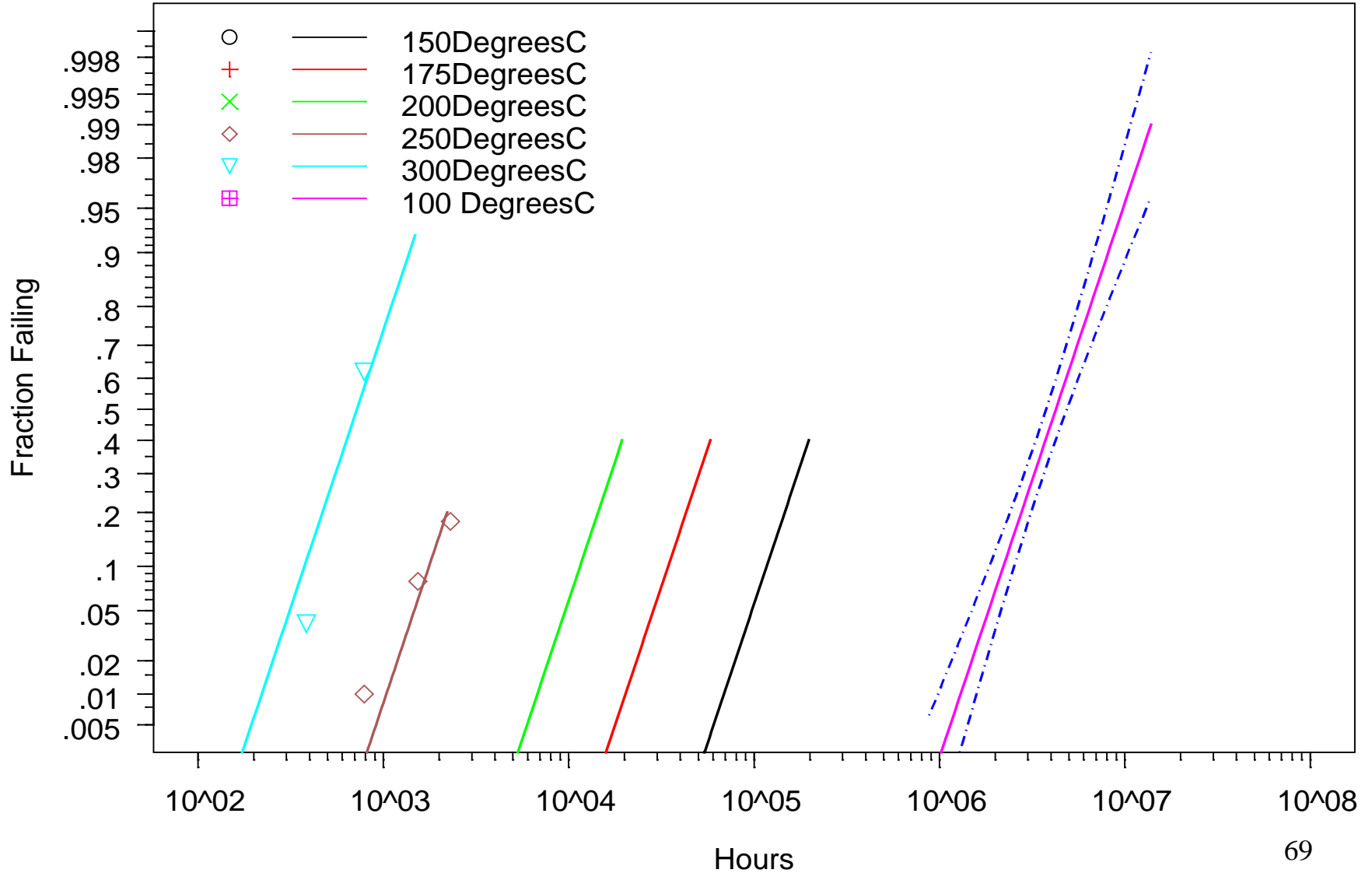
New Technology Device ALT  
DegreesCArrhenius , Dist:Lognormal



New Technology Device ALT Model MLE  
 DegreesC Arrhenius, Dist: Lognormal  
 Lognormal Probability Plot



New Technology Device ALT Model MLE  
 DegreesC Arrhenius, Dist: Lognormal  
 Lognormal Probability Plot



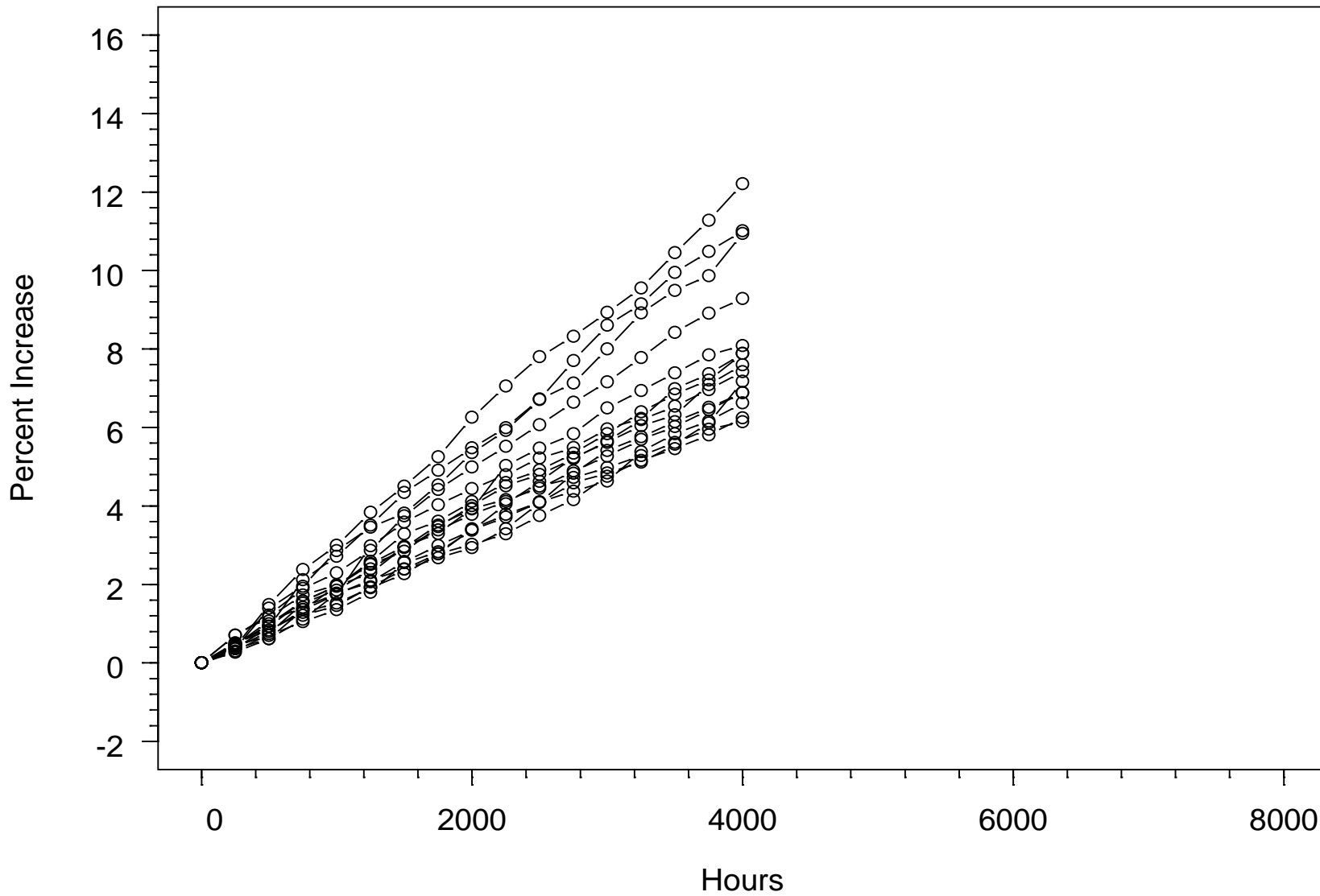
# Lessons Learned

- Maximum likelihood can easily deal with interval-censored data
- A change in the distribution slope parameter implies that simple acceleration models are not appropriate
- Too much stress can cause new failure modes
- Statistical error is greatly amplified when extrapolating
- Engineering information is important in accelerated life testing

# GaAs Laser Repeated Measures Degradation Data Analysis

- Lasers used in telecommunications applications
- Lasers tested at 80 degrees C to accelerate life
- Few failures expected even in the accelerated life test

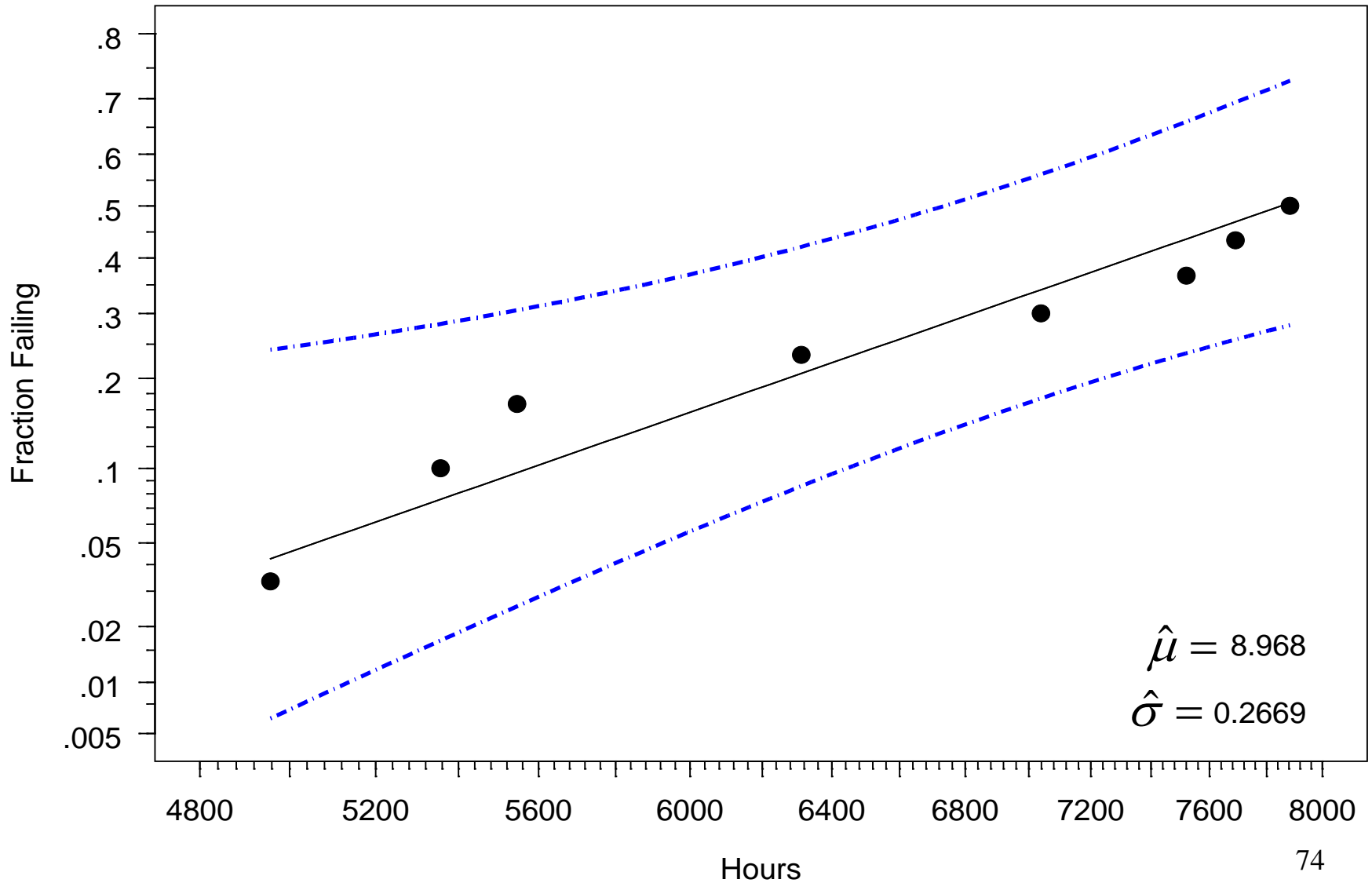
# Percent Increase in Operating Current







GaAsLaser.CurrentF15C8000.XLinear.YLinear.Id  
with Lognormal ML Estimate and Pointwise 95% Confidence Intervals  
Lognormal Probability Plot



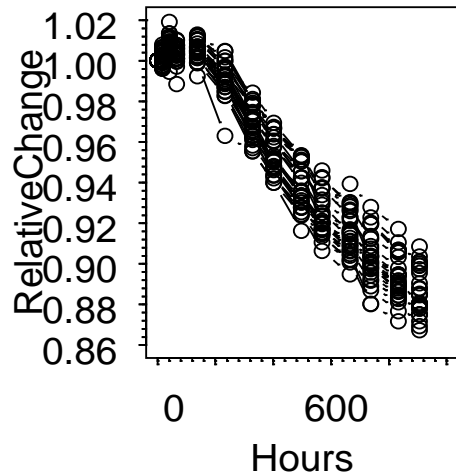
# Accelerated Repeated Measures Degradation Test of LEDs

- Tests run with 50 LEDs at each of six combinations of temperature and current (two accelerating variables)
- Measured light output on each unit periodically
- Data are messy

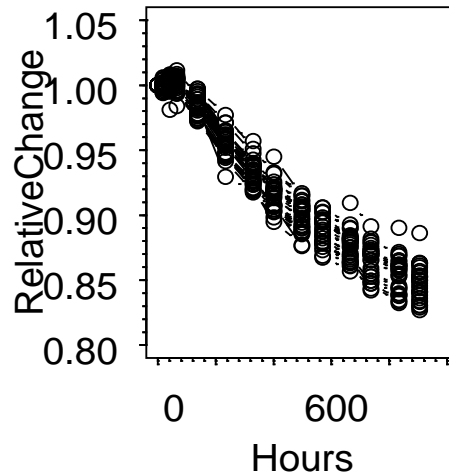
# LED Relative Change in Light Output (Zero Start)

x axis: linear    y axis: linear

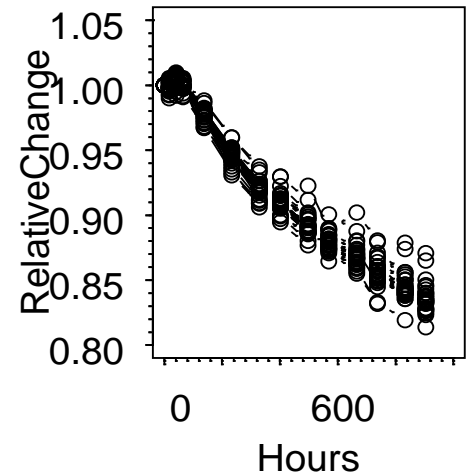
61JTemp;30Current



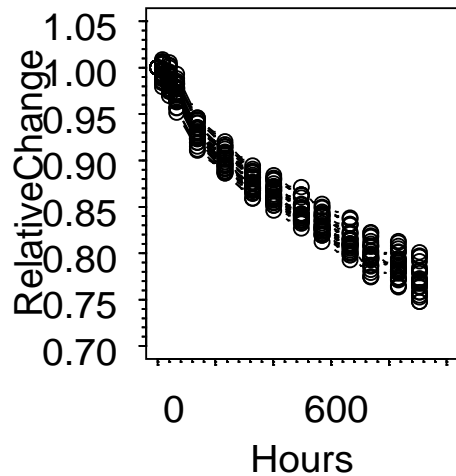
77JTemp;40Current



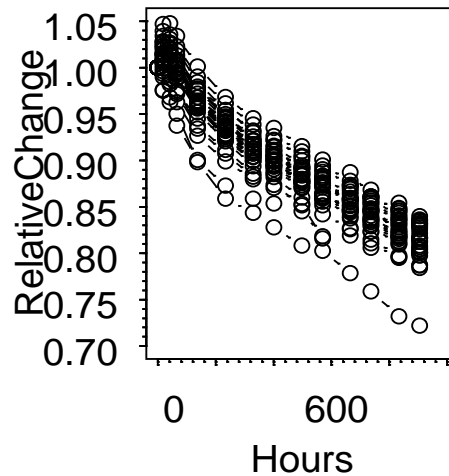
94JTemp;30Current



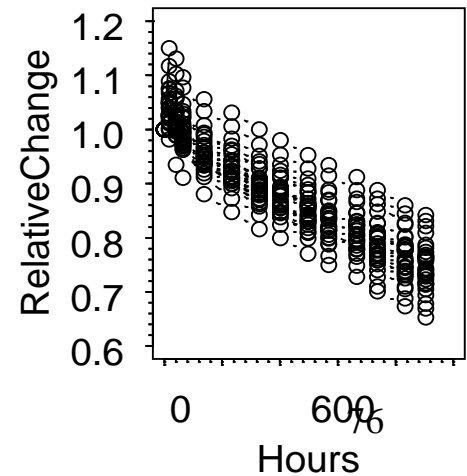
110JTemp;40Current



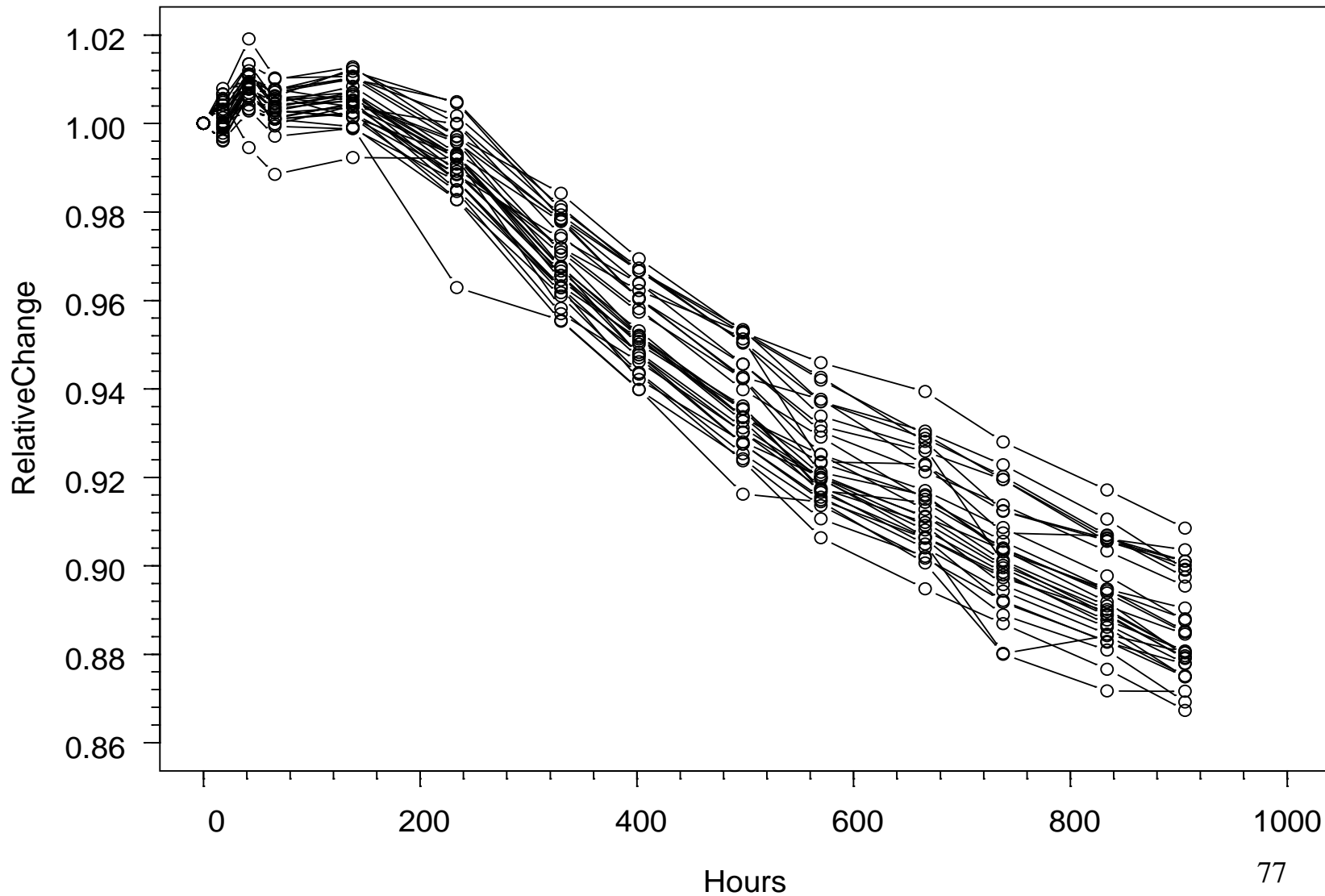
114JTemp;30Current



130JTemp;40Current

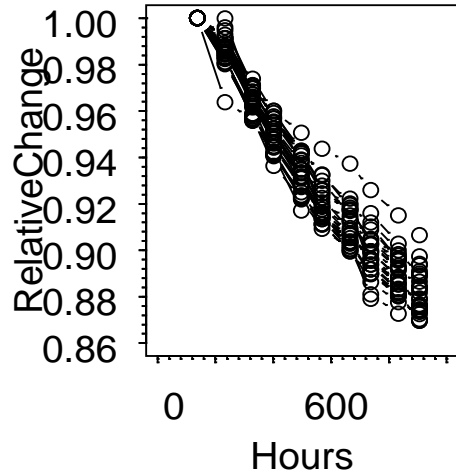


led.zero.startt61c30 RelativeChange data

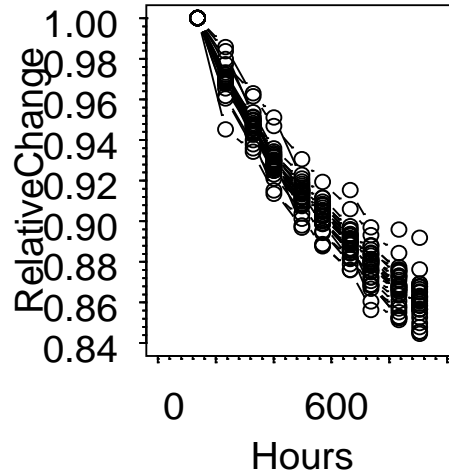


Relative Change in Light Output from 138 Hours  
x axis: linear y axis: linear

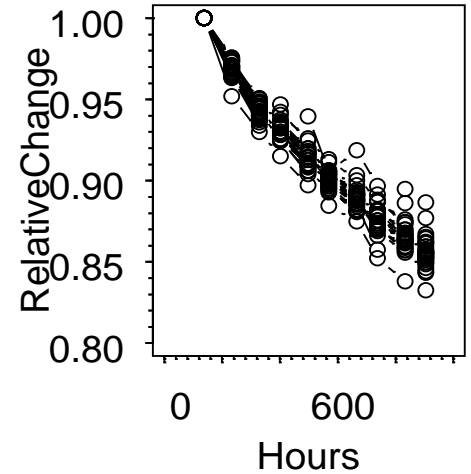
61JTemp;30Current



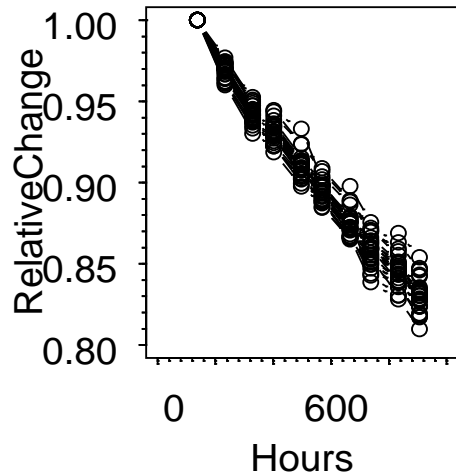
77JTemp;40Current



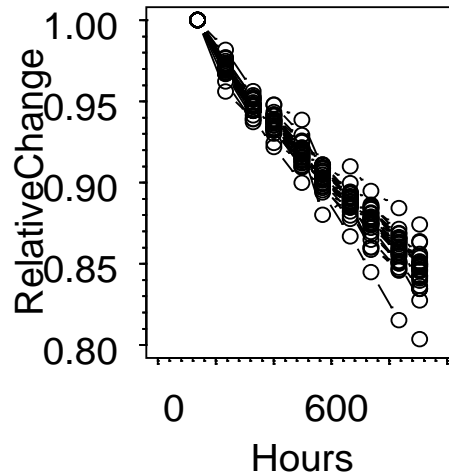
94JTemp;30Current



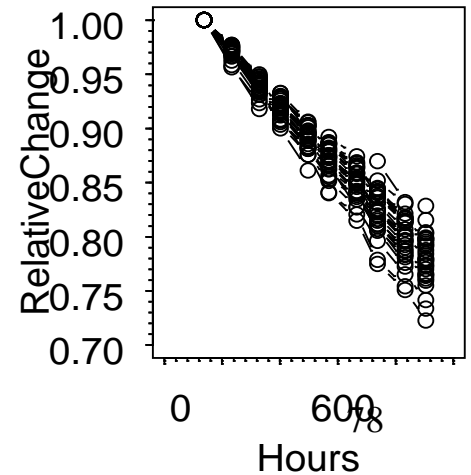
110JTemp;40Current



114JTemp;30Current

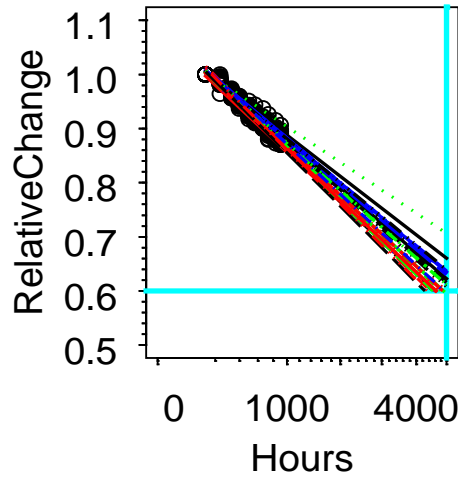


130JTemp;40Current

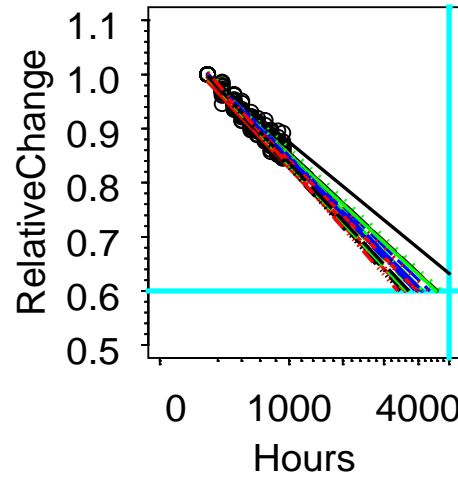


# LED Pseudo Failures F0.6C5000.XSquareroot.YLinear

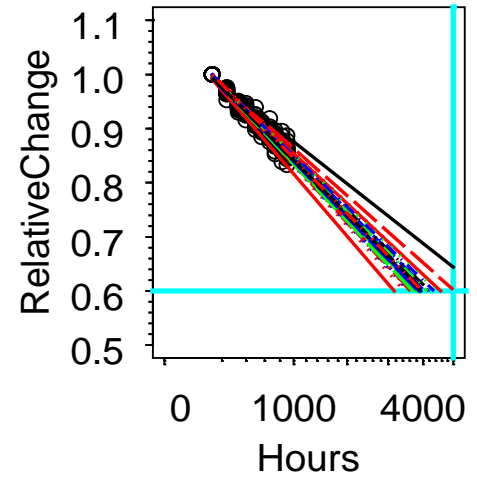
61JTemp;30Current



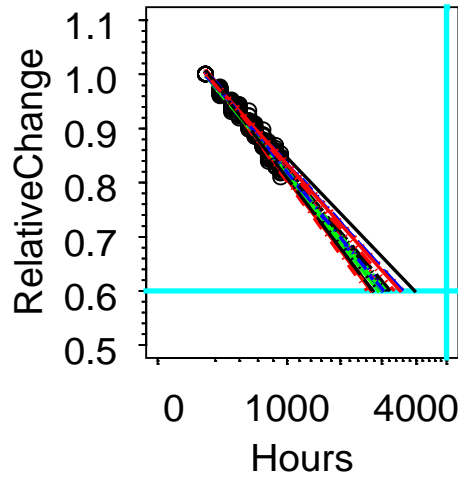
77JTemp;40Current



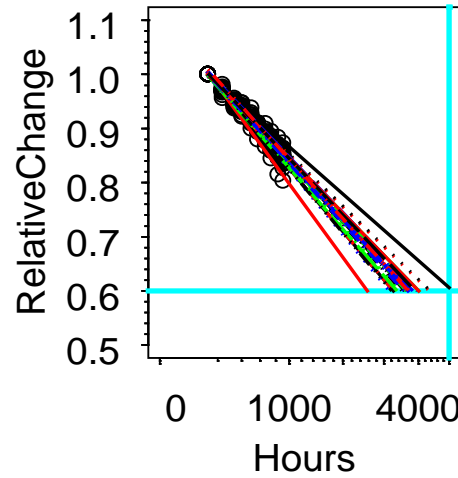
94JTemp;30Current



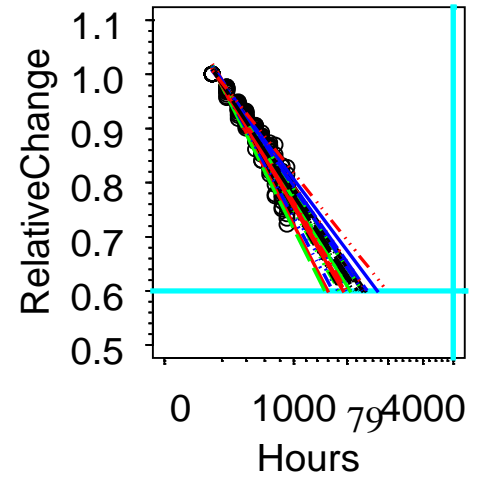
110JTemp;40Current



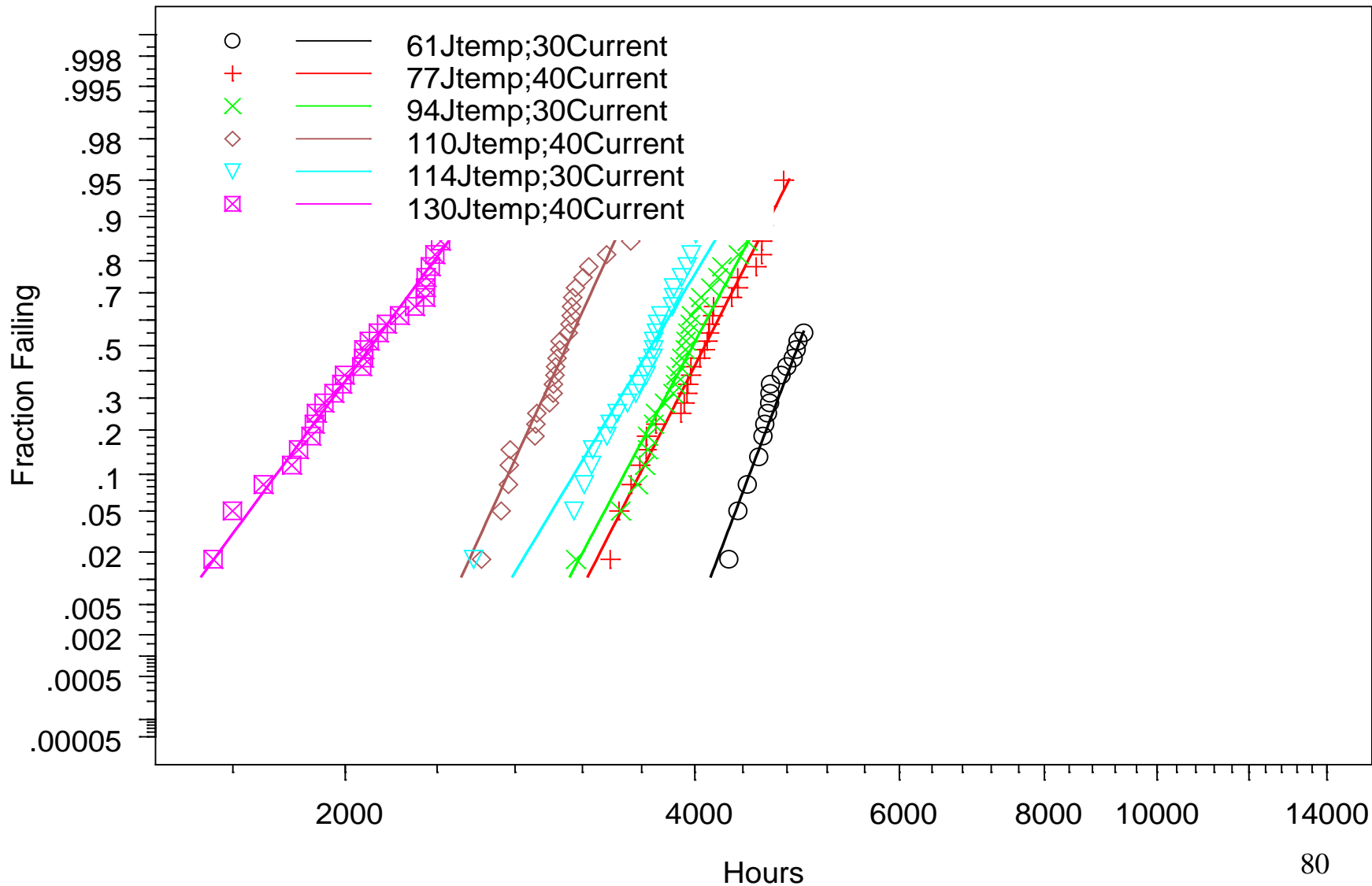
114JTemp;30Current



130JTemp;40Current

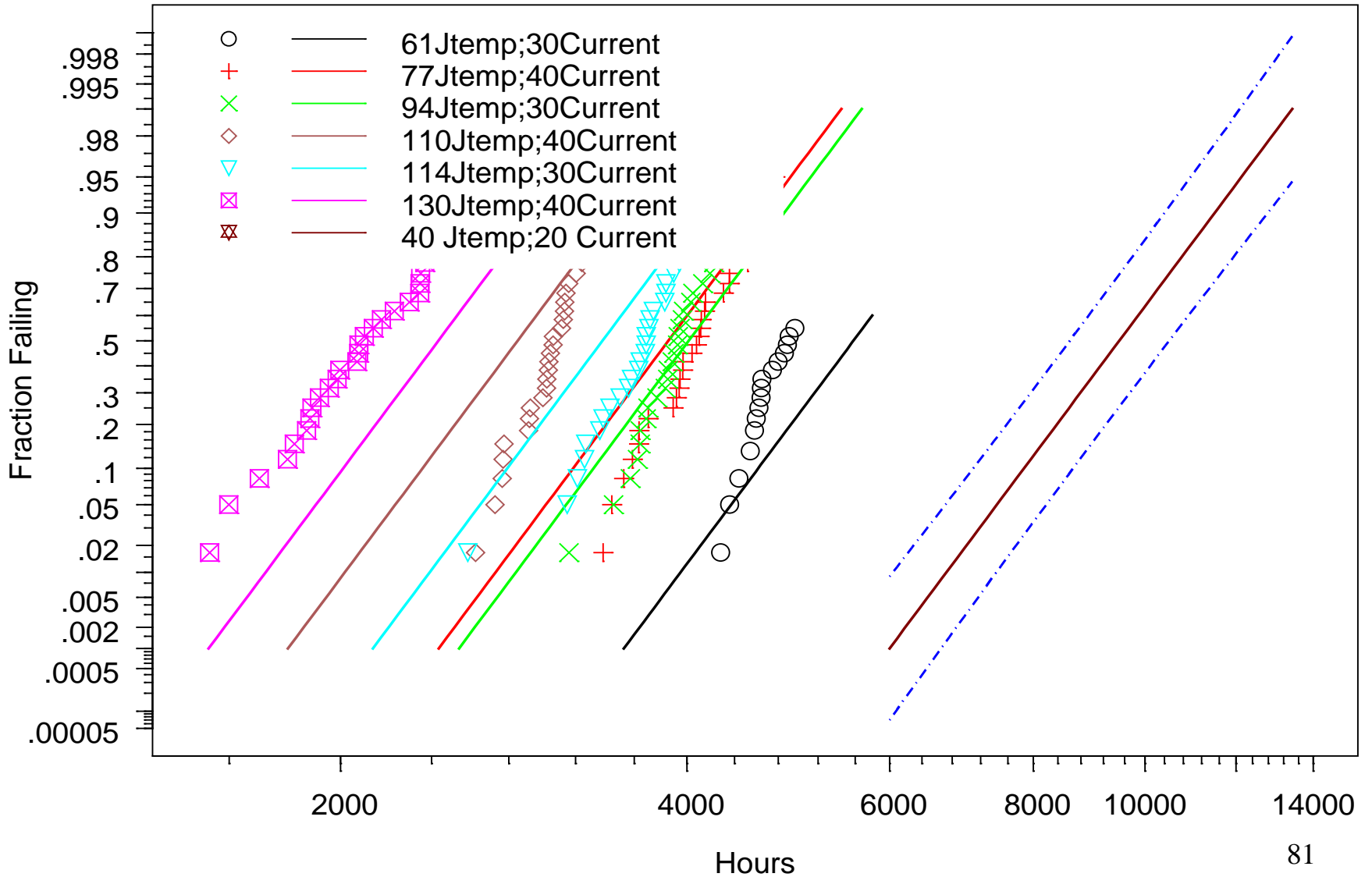


DeviceL Pseudo Failures F0.6C5000.XSquareeroot.YLinear  
With Individual Lognormal Distribution ML Estimates  
Lognormal Probability Plot

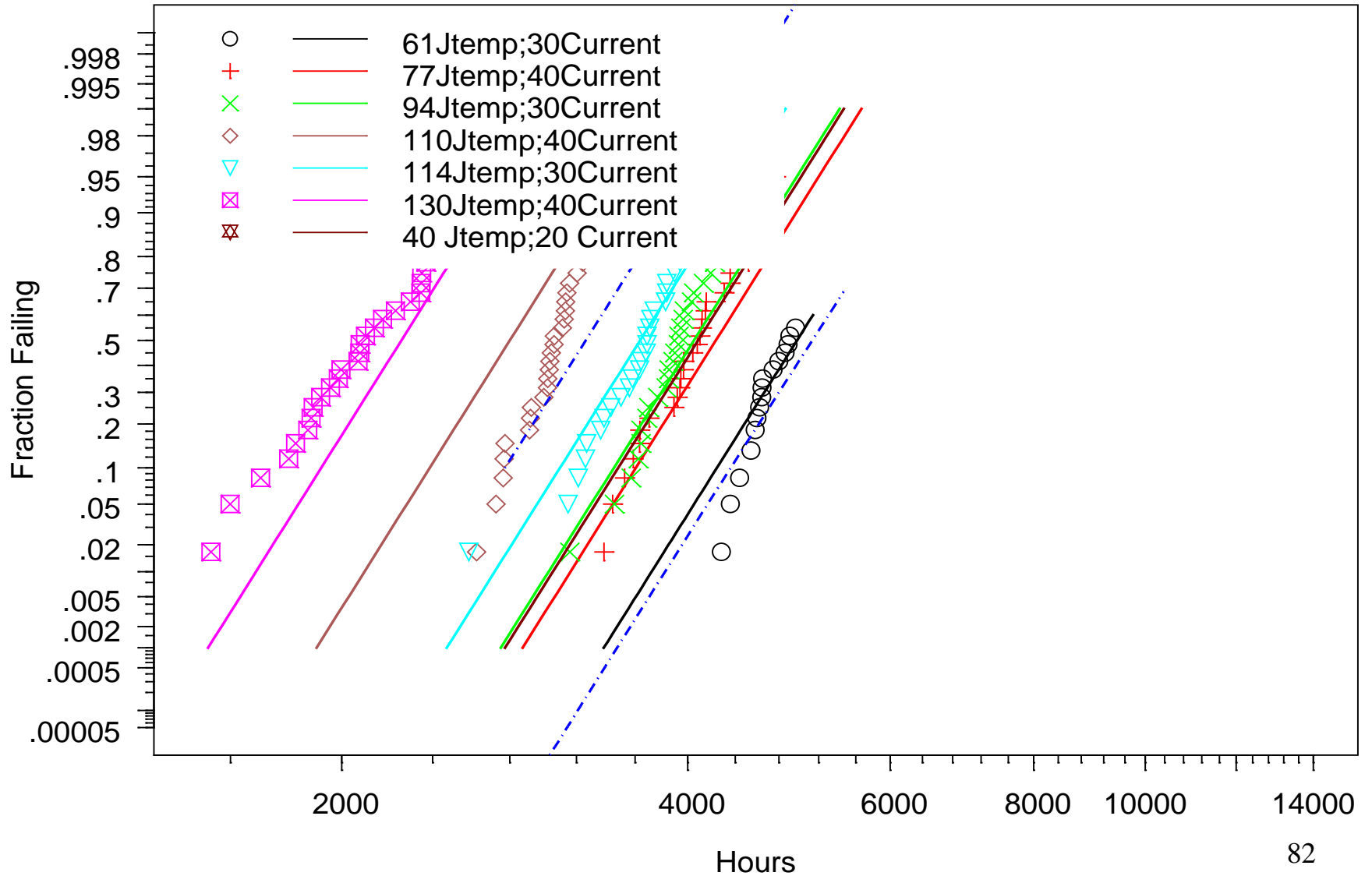




DeviceL Pseudo Failures F0.6C5000.XSquareroot.YLinear Model MLE  
 JtempArrhenius, CurrentLog, Dist:Lognormal  
 Lognormal Probability Plot



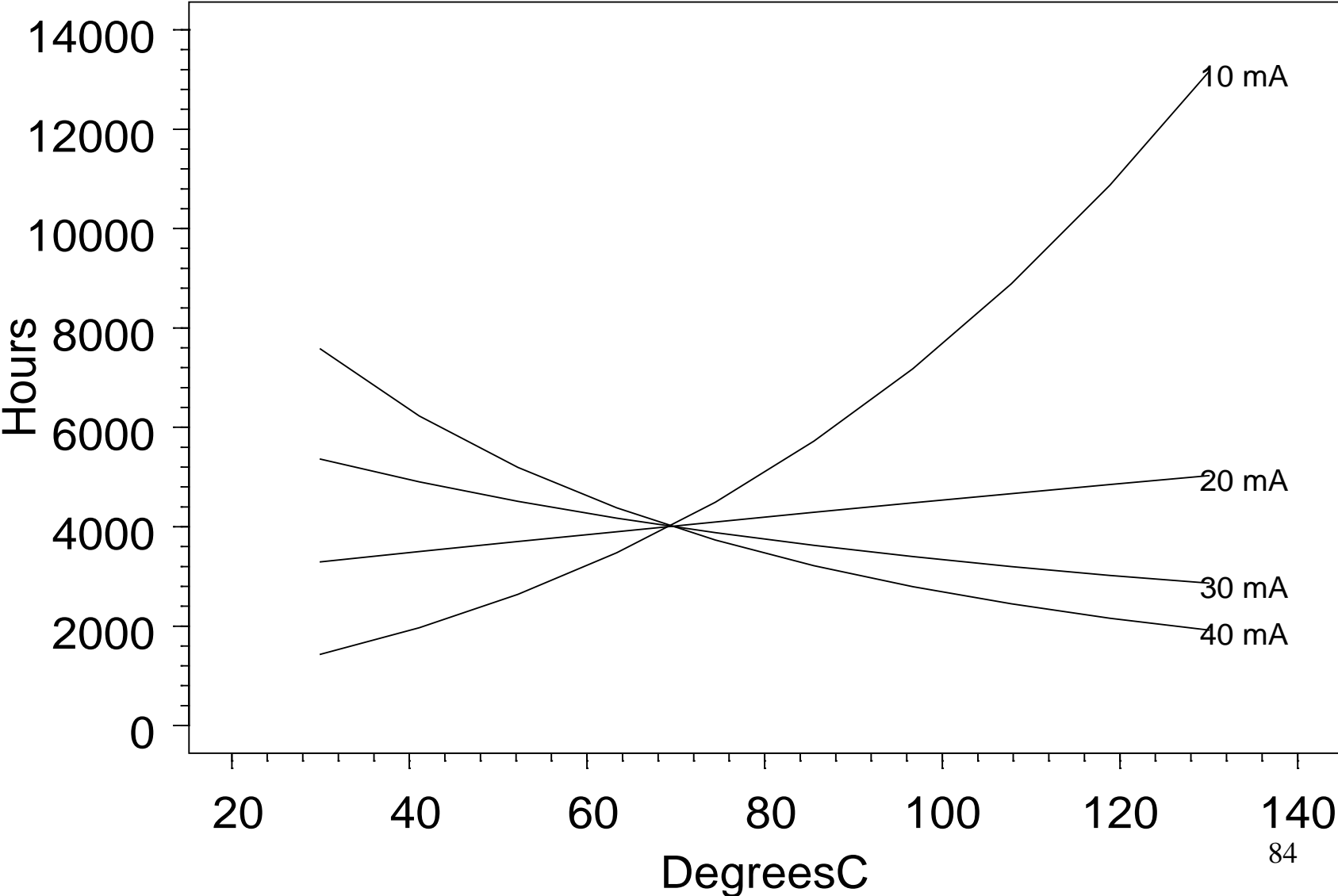
DeviceL Pseudo Failures F0.6C5000.XSquareroot.YLinear Model MLE  
 JtempArrhenius, CurrentLog, Dist:Lognormal  
 Lognormal Probability Plot



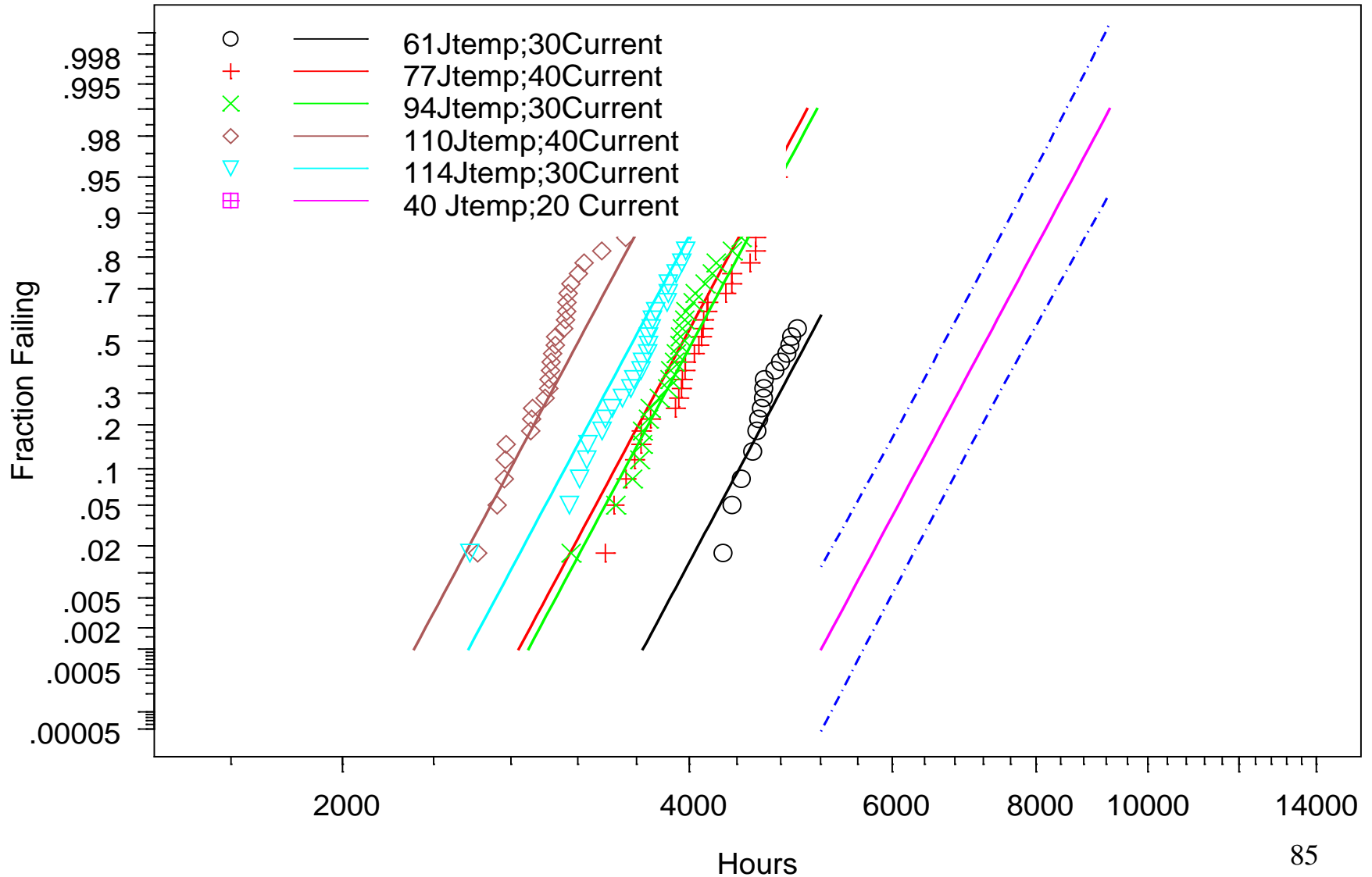


# Lifetime as a Function of Current and Junction Temperature

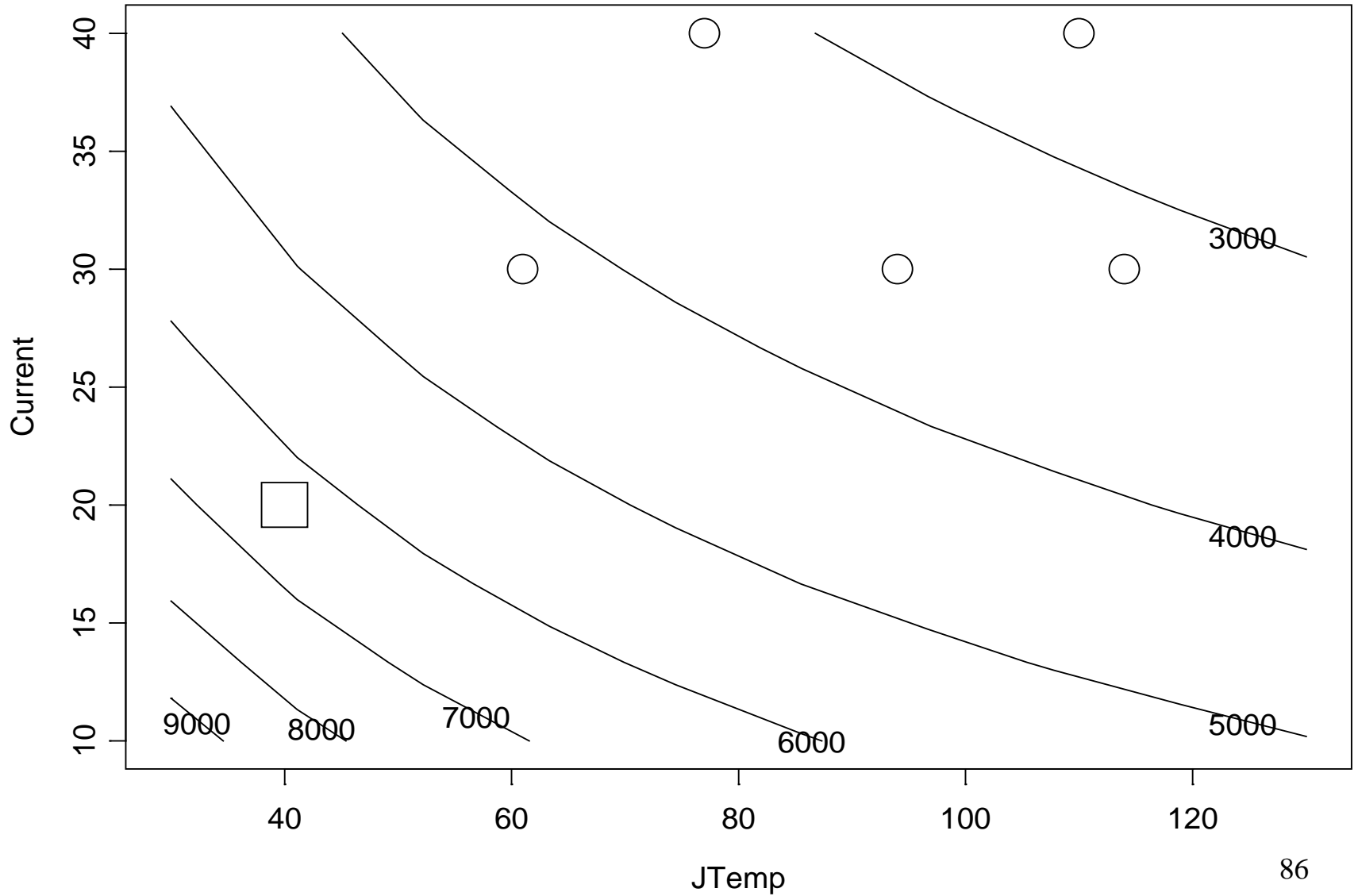
## Showing the Nonsensical Relationships for Low Current Values



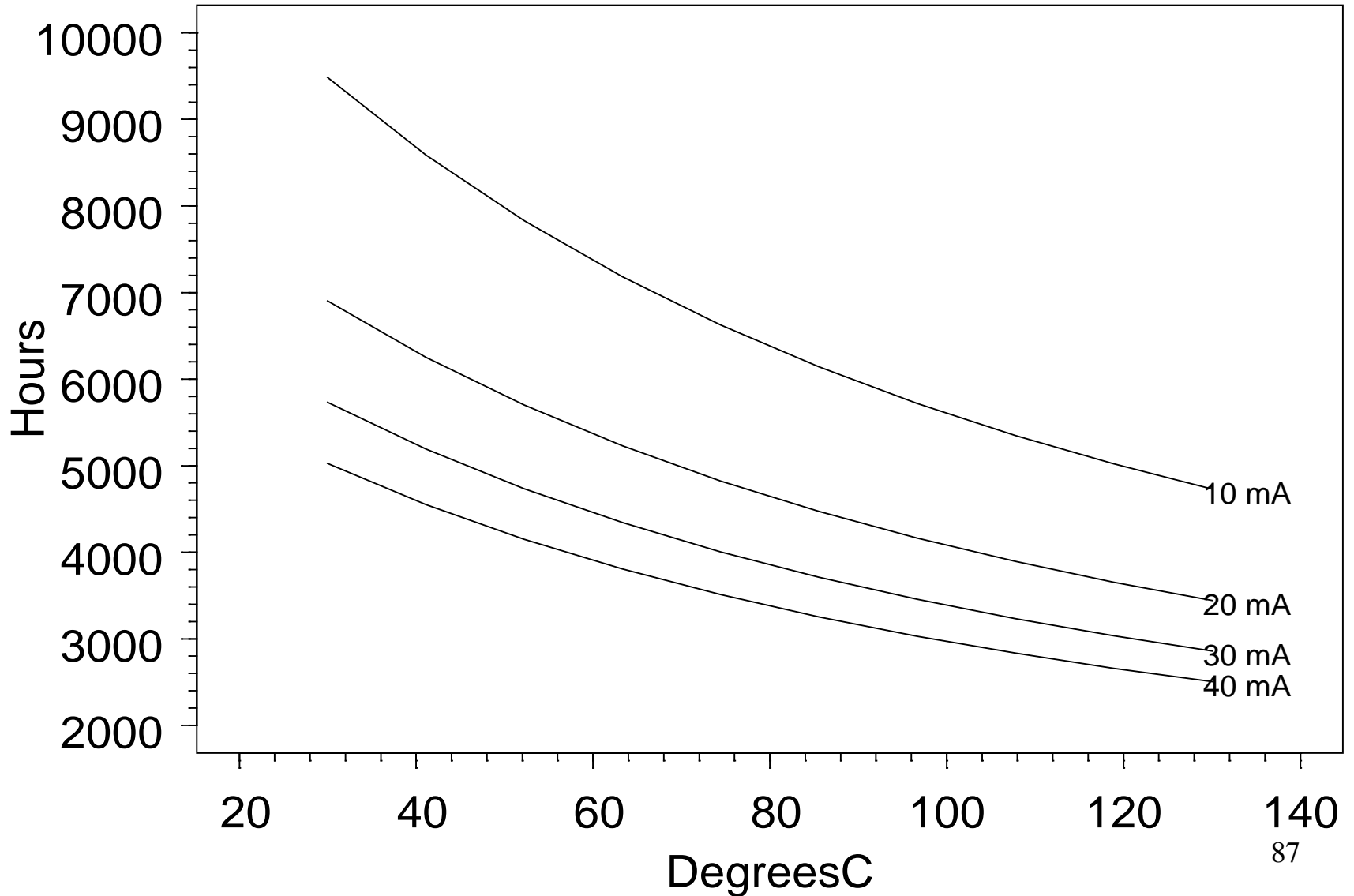
Fixed DeviceL Pseudo Failures F0.6C5000.XSquareroot.YLinear Model MLE  
 JtempArrhenius, CurrentLog, Dist:Lognormal  
 Lognormal Probability Plot



# Lifetime as a Function of Current and Junction Temperature After the Bad Data Was Removed



# Lifetime as a Function of Current and Junction Temperature After the Bad Data Was Removed



# Lessons Learned

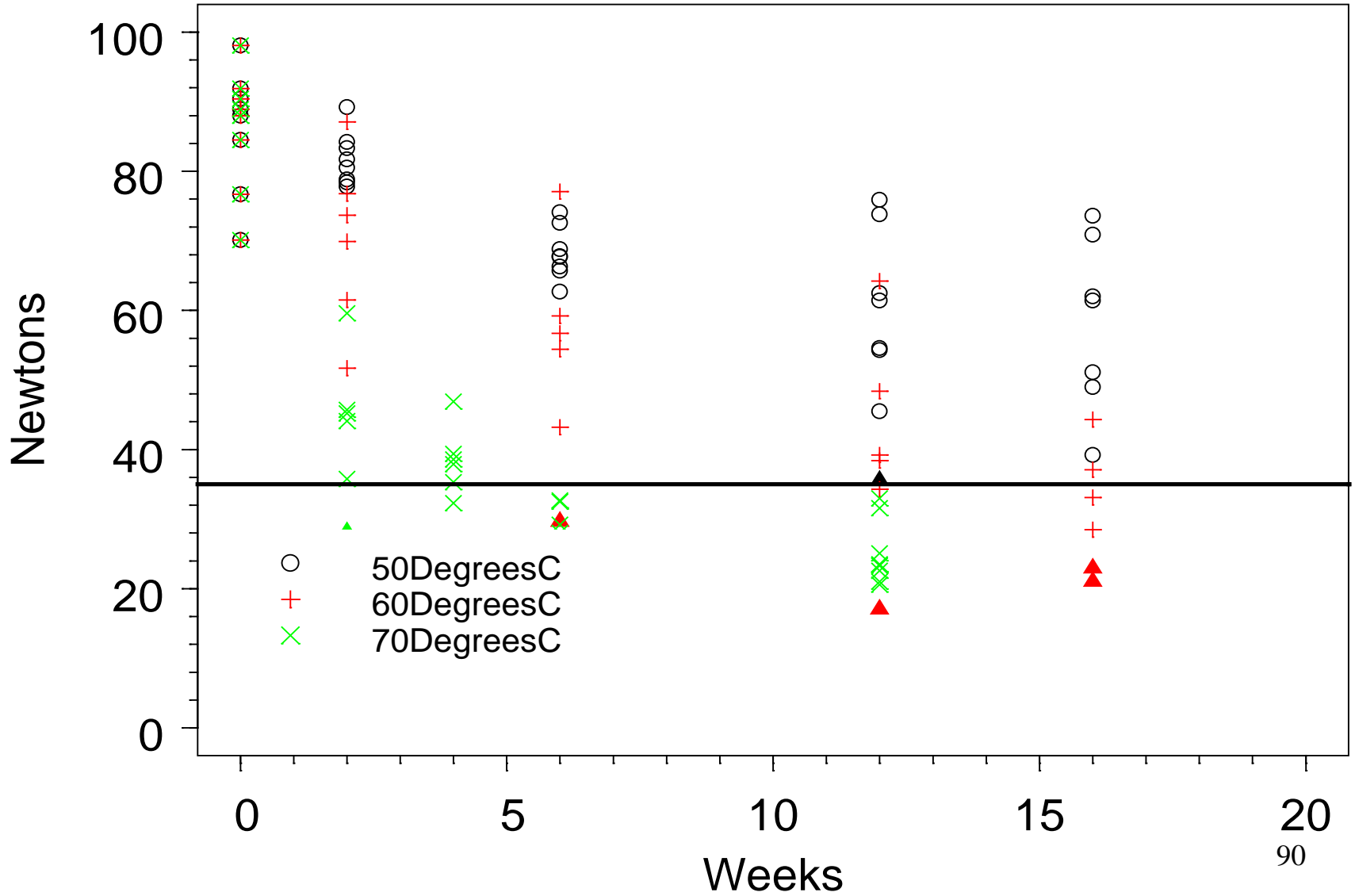
- Repeated measures degradation data can provide much more information than failure-time data
- Early part of degradation path may be complicated, but can be ignored.
- Testing at stress levels that are too high can cause new failure modes
- Modeling and extrapolation in two dimensions (two accelerating variables) can be more complicated and more risky



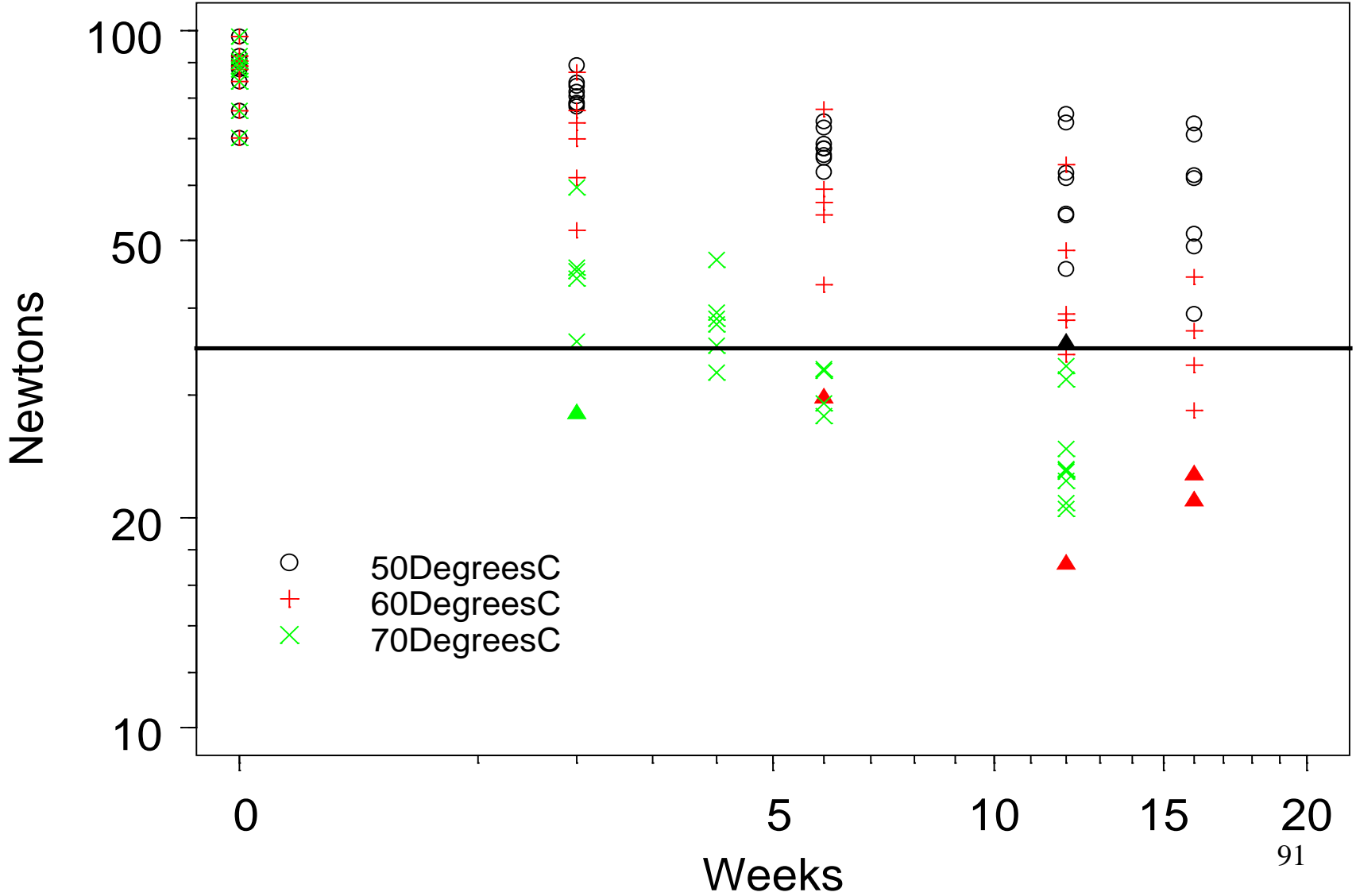
# Accelerated Destructive Degradation Test to Evaluate the Lifetime of an Adhesive Bond

- Some baseline units tested without aging
- Samples of units placed into chambers operating at 50, 60, and 70 degrees C
- Some units removed at specific times and destructively evaluated for strength
- Units with adhesive strength below 35 Newtons are considered to be failures

AdhesiveBondB data  
Destructive Degradation Scatter Plot  
Resp:Linear,Time:Linear

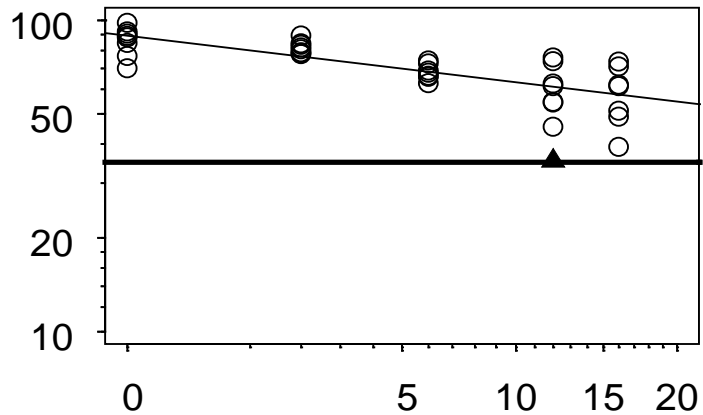


AdhesiveBondB data  
Destructive Degradation Scatter Plot  
Resp:Log,Time:Square root

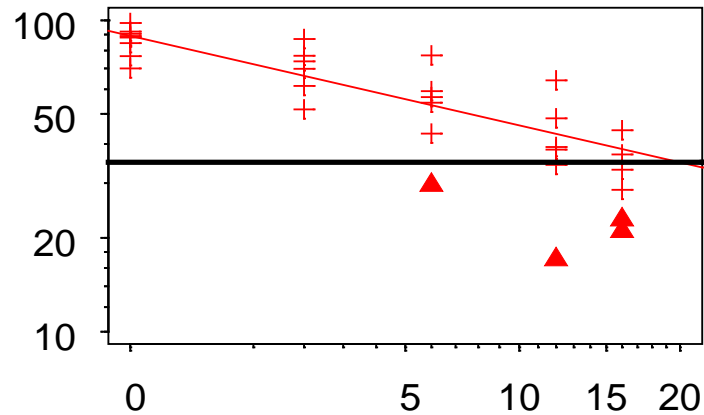


AdhesiveBondB data  
Resp:Log,Time:Square root, Dist:Normal

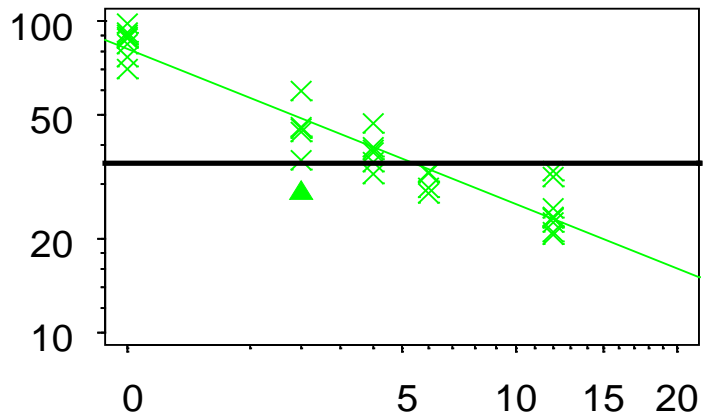
50DegreesC



60DegreesC



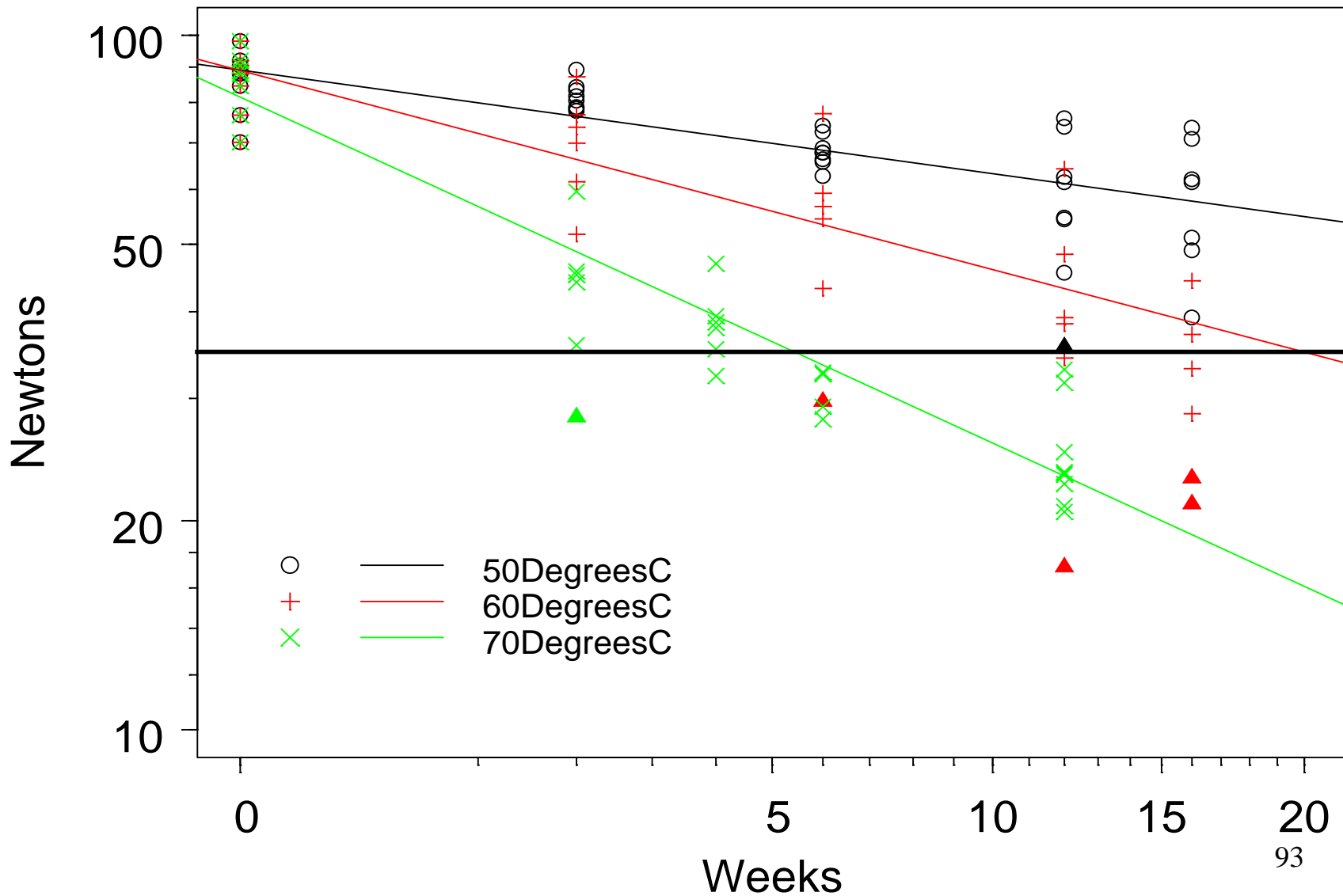
70DegreesC



Newtons

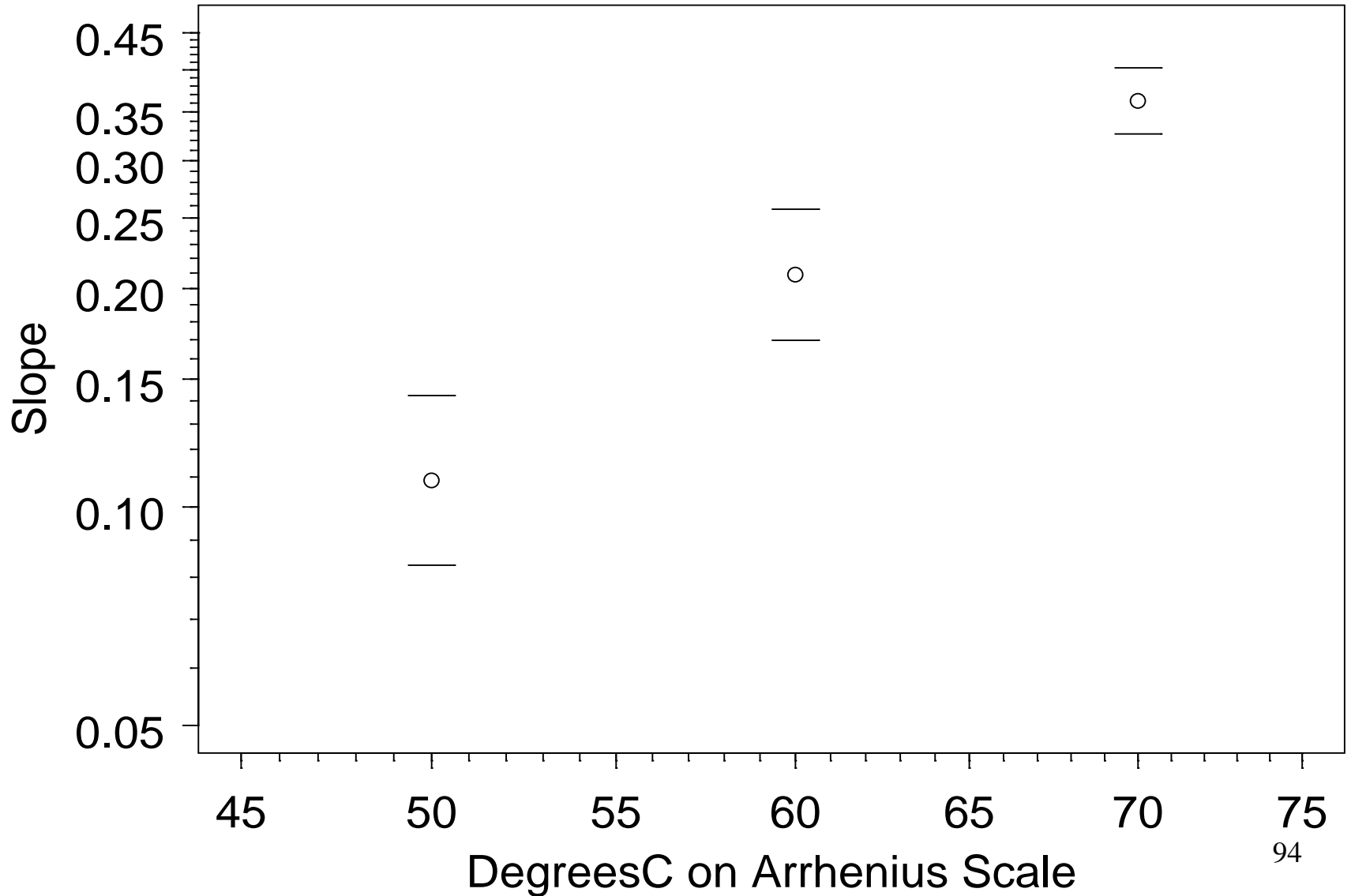
Weeks

AdhesiveBondB data  
Destructive Degradation Individual Regression Analyses  
Resp:Log,Time:Square root, Dist:Normal

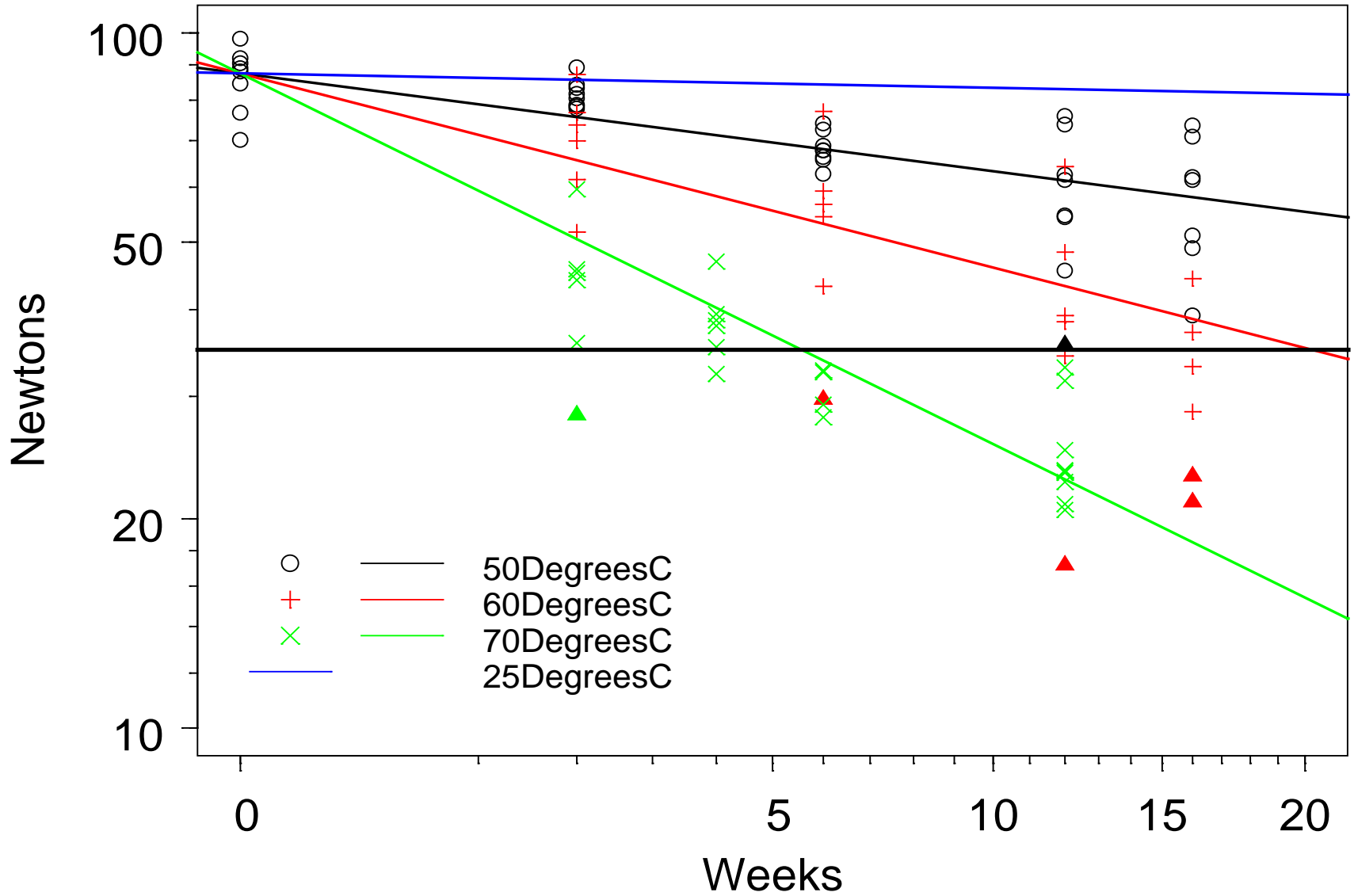


Degradation rate versus DegreesC on Arrhenius Scale for  
AdhesiveBondB data

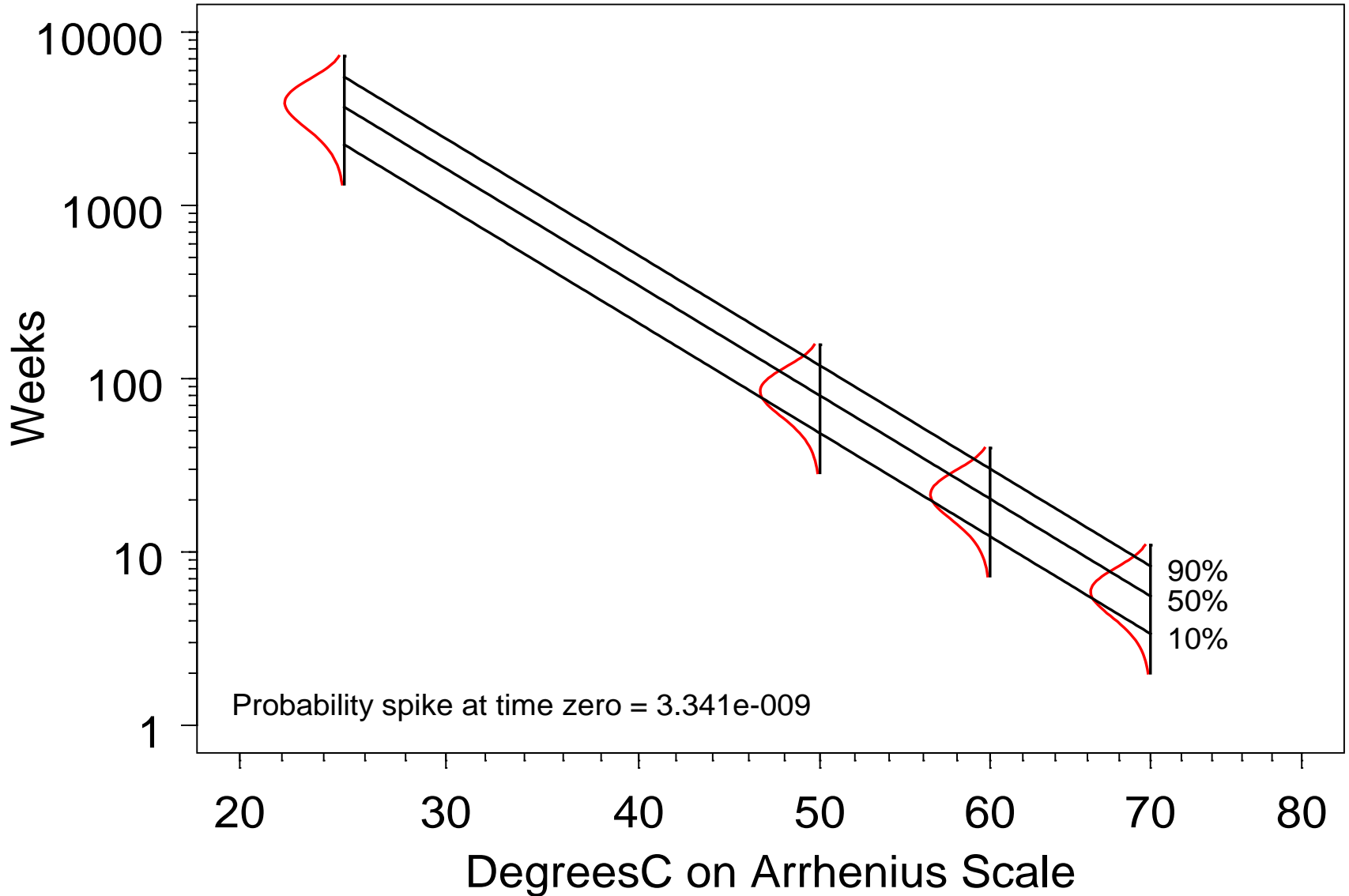
Resp:Log,Time:Square root,x:Arrhenius, Dist:Normal



AdhesiveBondB data  
 Destructive Degradation Regression Analyses  
 Resp:Log,Time:Square root,DegreesC:Arrhenius, Dist:Normal



Model plot for AdhesiveBondB data  
Resp:Log,Time:Square root,DegreesC:Arrhenius, Dist:Normal  
Failure-time distribution for degradation failure level of 35 Newtons





# Lessons Learned

- Destructive degradation data are also useful, but more units need to be tested
- Transformations of variables can sometimes simplify model assumptions
- One needs to understand the reason for anomalous observations before acting on them

# Concluding Remarks

- There are many kinds of reliability data: life, repeated measures degradation, destructive degradation, recurrence
- We often need to use available information outside of your data, but recognize uncertainty in that information.
- Divide and analyze (e.g., failure cause, stratification).
- Do not ignore model uncertainty, especially in extrapolation.
- There is no magic in accelerated testing or statistics
- Finding appropriate accelerating variables and a model adequate for extrapolation are critical concerns.
- Modern software can make the analysis easy, but answers may depend critically on assumptions that cannot be tested.

# Some Important References

- Meeker, W. Q., and L. A. Escobar (1998). *Statistical Methods for Reliability Data*, New York, NY: Wiley.
- Nelson, W. (1982). *Applied Life Data Analysis*, New York, NY: Wiley.
- Nelson, W. (1990). *Accelerated Testing: Statistical Models, Test Plans, and Data Analyses*, New York, NY: Wiley.
- Nelson, Wayne B. (2003). *Recurrent Events Data Analysis for Product Repairs, Disease Recurrences, and Other Applications*, ASA-SIAM Series on Statistics and Applied Probability
- Tobias, P. A., and D. C. Trindade (2011). *Applied Reliability*, Third Edition, New York, NY: Van Nostrand Reinhold.